Estimating total heliospheric magnetic flux from single-point in situ measurements

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A fraction of the total photospheric magnetic flux opens to the heliosphere to form the interplanetary magnetic field carried by the solar wind. While this open flux is critical to our understanding of the generation and evolution of the solar magnetic field, direct measurements are generally limited to single-point measurements taken in situ by heliospheric spacecraft. An observed latitude invariance in the radial component of the magnetic field suggests that extrapolation from such single-point measurements to total heliospheric magnetic flux is possible. In this study we test this assumption using estimates of total heliospheric flux from well-separated heliospheric spacecraft and conclude that single-point measurements are indeed adequate proxies for the total heliospheric magnetic flux, though care must be taken when comparing flux estimates from data collected at different heliocentric distances.


1. Introduction

Line-of-sight photospheric magnetic flux is routinely measured by ground- and space-based magnetograms. A significant fraction of this flux is “closed,” meaning that it forms loops below the height at which gas pressure exceeds magnetic pressure and thus does not contribute to the interplanetary magnetic field carried by the solar wind. The foot points of “open” magnetic field lines, which extend high enough to be dragged out by the solar wind and contribute to the heliospheric magnetic flux, are strongly associated with coronal holes. Direct measurement of this open magnetic field component is generally limited to single-point heliospheric measurements taken in situ spacecraft, from which total heliospheric flux is then deduced.

On the basis of such heliospheric flux estimates, a number of models for the evolution of the heliospheric magnetic field have been put forward. Fisk et al. (1999) suggest that the Sun’s open flux tends to be conserved, with “interchange reconnection” between open and closed fields resulting in an effective diffusion of open flux across the solar surface, without any net change in the total open flux. This allows the heliospheric field to evolve as a simple rotation of regions of positive and negative polarity separated by a single, large-scale heliospheric current sheet [Fisk and Schwadron, 2001], which is one explanation for the available observations [Jones et al., 2003]. Alternatively, it has been argued that emerging midlatitude bipoles cause closed coronal loops to rise and destroy or create open flux in such a way as to reverse the coronal field [Babcock, 1961; Wang and Sheeley, 2003]. Transient events may also have a significant role in the evolution of the heliospheric magnetic field [Low, 2001]. Indeed, Owens et al. (2007) suggest that the migration of open flux is facilitated by reconnection with the magnetic field systems of coronal mass ejections (CMEs).

The validity of the single-point approximation rests largely on Ulysses observations of a latitude invariance in $R^2|B_R|$ [Smith and Balogh, 2003; Lockwood et al., 2004], where $R$ is the heliocentric distance and $B_R$ is the radial component of the magnetic field. Thus, at any point in the heliosphere $4nR^2|B_R|$ should be representative of the total heliospheric flux. Only data from 2-year periods covering Ulysses perihelion passes were considered in the latitude invariance reported by Smith and Balogh [2003] and Lockwood et al. [2004], as flux estimates at large heliocentric distance are complicated by a reduced “signal to noise” (E. Smith,
personal communication, 2008): as $R$ increases, the magnetic field becomes increasingly azimuthal, increasing the uncertainty in the estimated flux. Smith and Balogh [2003] also reported little difference in $R^2 |B_R|$ between the solar minimum (1994–1996) and maximum (2000–2002) perihelion passes, contrary to the in-ecliptic observed solar cycle variation in flux [e.g., Richardson et al., 2002], but ascribed this apparent time invariance to the solar maximum observation occurring during a temporary, global decrease. This temporary solar maximum drop in heliospheric flux was also seen in near-Earth data (the so-called “Gnevyshev gap” [Gnevyshev, 1977]). In general, we note that identification of solar cycle variations in the Ulysses data are complicated by the Ulysses orbit, which results in a radial distance variation almost in phase with the solar cycle.

[5] Estimates of total heliospheric flux are possible using models constrained by the observed photospheric magnetic field. Potential field [e.g., Schatten et al., 1969; Ailschuler and Newkirk, 1969] and magnetohydrodynamic solutions [e.g., Linker et al., 1999; Mikić et al., 1999] of total heliospheric flux generally show reasonable agreement with single-spacecraft measurements [Wang and Sheeley, 2003; Owens et al., 2008; Lepri et al., 2008]. However, uncertainties in the systematic offsets in the magnetograms [Svalgaard et al., 1978; Ulrich, 1992; Wang and Sheeley, 1995], as well as the underlying model assumptions and tuning, mean that such modeling may not provide an adequate or independent test of the single-point assumption [Lockwood et al., 2004]. Estimates of heliospheric magnetic flux based upon geomagnetic indices [e.g., Lockwood et al., 1999; Svalgaard and Cliver, 2007] are generally derived from single-point magnetic field measurements and thus do not provide an independent test.

[6] In this study, we directly test the assumption that single-point measurements are sufficient to estimate total heliospheric flux by comparing the estimates by well-separated spacecraft in the heliosphere. The inclination of the ecliptic plane to the heliographic equator allows sampling of latitudinal separations up to $\sim 14.5^\circ$ with a variety of spacecraft over long time periods. Longitudinal and radial variations in $B_R$ are assumed to be averaged out by considering time periods longer than a solar rotation. This assumption is valid if total heliospheric flux is not varying on timescales less than a solar rotation, which is tested by using spacecraft at large longitudinal and radial separations.

### 2. Methodology

#### 2.1. Flux Calculation

[7] We consider the total heliospheric flux content to be the unsigned flux content threading a heliocentric sphere [e.g., Smith and Balogh, 2003]. Note that some studies [e.g., Lockwood et al., 1999] instead compute the amount of flux of a single polarity, a factor 2 lower than the total unsigned flux. If $R^2|B_R|$ is invariant throughout the heliosphere, the calculation of total heliospheric flux, $\Phi_{\text{TOTAL}}$, from single-spacecraft observations is straightforward:

$$\Phi_{\text{TOTAL}} = 4\pi R^2 |B_R|.$$

[8] Care must be taken, however, in the calculation of the time average of the radial field $\langle |B_R| \rangle$, as the bipolar nature of $B_R$ means that $|B_R| \neq |B_R|$. Smith and Balogh [2003] showed that this effect is probably insignificant if longer-term averages are based on $|B_R|$ over shorter intervals (an hour was deemed sufficient. For the Ulysses data set, we too find little difference in Carrington rotation flux estimates based on 5-min and 1-h data). Thus, to compare total flux computed from different data sets, which frequently have different intrinsic time resolutions, we first compute $\langle |B_R| \rangle_{1h}$ for all data sets. All subsequent calculations of $\langle |B_R| \rangle$ are based on these 1-h averaged time series. We do, however, note that for the OMNI data set the field magnitude computed using the field vectors is approximately 10% lower than the measured scalar magnetic field, suggesting that high-frequency fluctuations do have an effect on the
Figure 1. A plot of 3-Carrington-rotation averages of $\Delta \Phi$ (the difference between the near-Earth and far-Earth total heliospheric flux estimates) as a function of $R$ (the heliocentric distance of the fE spacecraft). The color code for the various spacecraft is listed in Figure 2. Past $R = 2.5$ AU, the black dashed vertical line, there is a clear radial trend in $\Delta \Phi$. 
measured radial field. Thus, the flux calculated on the basis of \( R^2 \langle |B_R| \rangle \) may be somewhat below the “true” value. By ensuring that all time averages are performed in the exact same manner, this effect will be the same for all the data sets considered and thus does not affect our assessment of single-point extrapolation to total heliospheric flux. We assume that all systematic instrumental offsets are well below the magnetic field variations under study.

2.2. Data Selection

In order to compare estimates of total heliospheric flux from well-separated spacecraft in the heliosphere, we first use the OMNI data set (available from the National Space Science Data Center (NSSDC) at http://omniweb.gsfc.nasa.gov/) of spacecraft in near-Earth (nE) space to estimate the total heliospheric flux from 1963 through 2008. This nE flux estimate is compared to independent estimates from spacecraft well separated from Earth in heliocentric distance, latitude, or longitude, referred to as the far-Earth (fE) data points. Beginning with the NSSDC data sets, we select all available heliospheric magnetic field measurements from spacecraft at least 10 \( \times 10^4 \) separated from Earth in heliolongitude and heliolatitude but within 20 AU. In addition to the NSSDC data, we also use near-Earth asteroid rendezvous (NEAR) magnetometer data, obtained from the Small Bodies Node of the Planetary Data System. The left-hand side of Table 1 lists the spacecraft fulfilling these criteria.

To compare heliospheric flux estimates, we calculate the parameter \( \Delta \Phi = \frac{A}{U} R^2 \langle |B_R| \rangle_{nE} - R^2 \langle |B_R| \rangle_{fE} \), where \( R \) is the heliocentric distance of the fE spacecraft. Figure 1 shows \( \Delta \Phi \) as a function of \( R \). The color code used to identify the different spacecraft is given in Figure 2. No correction for the solar wind transit time has been performed, but data points are 3-Carrington-rotation (i.e., ~80-day) averages, so the effect should be insignificant except at the largest \( R \) values. Also, since it is the difference between the nE and fE flux estimate that is plotted, any global temporal variation should be subtracted out. Thus, the increase in \( \Delta \Phi \) with \( R \) is a true, pronounced, radial variation (linear correlation coefficient of 0.87 beyond \( R = 2.5 \) AU). This trend is likely due to a reduced signal-to-noise ratio at large heliocentric distance (Smith, personal communication, 2008): the measured magnetic field will contain a noise contribution from fluctuations in the field, which for the radial component of the field arises from fluctuations in the azimuthal and meridional components. For simplicity, consider a Parker spiral magnetic field, in which there is no meridional component: \( B_R \) falls off as \( 1/R^2 \), but the noise in \( B_R \) falls off as the azimuthal component of \( \mathbf{B} \), which for a Parker spiral field is \( (1/R) \cos \theta \), where \( \theta \) is the heliolatitude. Thus, the noise contribution to the estimated total heliospheric flux, \( 4\pi R^2 |B_R| \), will vary as \( R \cos \theta \). For the remainder of this study we only use data within 2.5 AU. The choice of this cut-off distance is somewhat arbitrary, but we note that below \( R = 2.5 \) AU the \( R \) dependence in \( \Delta \Phi \) is less apparent.

2.3. Data Used

To avoid the strong radial variation in the estimated heliospheric flux shown in Figure 1, the remainder of this study uses a subset of those data (listed in the right-hand side of Table 1) with the further constraint of \( R < 2.5 \) AU. Figure 2 shows histograms of the heliocentric distance and
angular separation from Earth (in heliographic longitude and latitude) at which the magnetic field measurements were made. Different spacecraft are identified by the colors shown to the right of the plots. While there is good coverage in heliocentric distance and heliographic longitude, coverage in heliographic latitude is generally limited to within $\pm 14^\circ$, with only Ulysses providing observations at more than $20^\circ$ latitudinal separation from Earth.

3. Results

In order to compare the total heliospheric flux observed by the spacecraft listed in Table 1 over a range of heliocentric latitudes and longitudes and within 2.5 AU, we plot Carrington rotation averages of total heliospheric flux estimates in Figure 3. Carrington rotation averages are used, as Lockwood et al. [2004] found no significant improvement in the correlation between ACE and Ulysses observations of $R[B_B]$ for longer averaging intervals. The color code is the same as in Figure 2. Error bars are standard errors on the mean. Connected lines (dots) show Carrington rotations with greater than one-third (one-fifth) data coverage. For the 1965–2008 period, near-Earth (far-Earth) spacecraft provide at least one-fifth data coverage for 93% (44%) of the Carrington rotations considered.

It can immediately be seen that there is good qualitative agreement between flux estimates made by well-separated spacecraft. The solar cycle variation in heliospheric flux inferred from single-point observations at L1 [e.g., Richardson et al., 2002] is prevalent at all longitudes, latitudes, and heliocentric distances sampled, suggesting that it is indeed indicative in a change in the total heliospheric flux content. Even at solar maximum, the temporal changes in the Sun’s magnetic field do not result in different flux estimates from longitudinally separated spacecraft. The latitude invariance in $R[B_B]$ found during limited periods by comparing Ulysses and near-Earth observations [Smith and Balogh, 2003; Lockwood et al., 2004] appears to hold for the extended time period, but smaller heliographic
latitude excursions, additionally considered in this study. Furthermore, Figure 3 confirms that the time invariance in the Ulysses perihelion passes [Smith and Balogh, 2003] is the result of sampling the solar maximum flux during the Gnevyshev gap [Gnevyshev, 1977] and that the most recent (2008) perihelion pass shows a reduced flux, in agreement with the nE observations.

Figure 4 shows a scatterplot of nE- and fE-derived total heliospheric flux estimates. The dashed line shows \( y = x \), i.e., the same flux estimated near Earth and at large separations from Earth. As in Figure 3, there is good agreement between the nE and fE estimates of heliospheric flux. While there is considerable scatter about the \( y = x \) line, the linear correlation coefficient (a linear relationship is expected between these parameters) is 0.65. For 371 data points involved in the correlation calculation, the null hypothesis that there is no correlation between the total flux estimates made by far-Earth and near-Earth spacecraft can be rejected above the 99% confidence level.

Figure 5 shows scatterplots of \( \Delta \Phi \), the difference between flux estimates made at nE and fE spacecraft, as a function of radial, longitudinal, and latitudinal separation from Earth. Top plots show the raw Carrington rotation averages, with spacecraft color codes as per Figure 2. Bottom plots show the data binned by \( R \), latitude, and longitude. To highlight the smaller latitudinal separations, a logarithmic scale is used for the x axis of the latitude plot. There appears to be a weak trend (correlation coefficient 0.41) between \( \Delta \Phi \) and \( R \), passing through \( \Delta \Phi = 0 \) at \( R = 1 \) AU. This trend is the same as that shown in Figure 1. It suggests that total heliospheric flux estimates based on \( B_R \) measurements 1 AU apart can differ by \( \sim 10\% \). Latitude and longitude scatterplots, however, are centered on \( \Delta \Phi = 0 \) with no obvious trends (the slight increase in \( \Delta \Phi \) for latitudes greater than 20° is due to only Ulysses data being considered and therefore skewed toward larger \( R \)). This suggests longitude and latitude invariance in flux, at least over these long (Carrington rotation) averages.

4. Conclusion

We have estimated the total heliospheric flux at a number of well-separated points in the heliosphere, over four solar cycles. While large separations in heliographic latitude are only possible with perihelion passes of the Ulysses spacecraft, we are able to sample smaller latitudinal separations on a more routine basis by using the inclination of the ecliptic plane to the heliographic equator. For Carrington rotation averages, we find good agreement for all radial, longitudinal, and latitudinal separations throughout the solar cycle. The latitude invariance in \( R^2 |B_R| \), demonstrated during limited periods by the Ulysses observations [Smith and Balogh, 2003; Lockwood et al., 2004], appears to hold for the expanded time period considered in this study. As might be expected for such long time averages, we found longitudinal invariance in the estimated flux. For radial separations, however, there does still seem to be a weak trend for larger total heliospheric flux to be estimated on the basis of \( B_R \) observations at larger distances from the Sun. We suggest that this trend is due to the increasingly azimuthal field. Thus, we conclude that extrapolation of single-point measurements of the radial compo-
component of the heliospheric magnetic field is a valid mean of estimating the total heliospheric magnetic flux in the inner heliosphere (inside ~2.5 AU), though care should be taken when comparing flux estimates at different heliocentric distances.

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References

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Figure 5. Scatterplots of $\Delta \Phi$, the difference between the total heliospheric flux estimates based on nE and fE observations, as a function of radial, longitudinal, and latitudinal separation. Top plots show the raw Carrington rotation averages, with spacecraft color code as per Figure 2. Bottom plots show the data binned by $R$, latitude, and longitude. To highlight the smaller latitudinal separations, a logarithmic scale is used for the $R$ axis of the latitude plot. There are no obvious trends in the latitude or longitude scatterplots, but there does appear to be a weak correlation between estimated flux and heliocentric distance.


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