Achievement emotions and academic performance: longitudinal models of reciprocal effects

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Achievement Emotions and Academic Performance:

Longitudinal Models of Reciprocal Effects

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Abstract

A reciprocal effects model linking emotion and achievement over time is proposed. The model was tested using five annual waves of the PALMA longitudinal study, which investigated adolescents' development in mathematics (grades 5-9; N=3,425 German students; mean starting age=11.7 years; representative sample). Structural equation modeling showed that positive emotions (enjoyment, pride) positively predicted subsequent achievement (math end-of-the-year grades and test scores), and that achievement positively predicted these emotions, controlling for students' gender, intelligence, and family socio-economic status. Negative emotions (anger, anxiety, shame, boredom, hopelessness) negatively predicted achievement, and achievement negatively predicted these emotions. The findings were robust across waves, achievement indicators, and school tracks, highlighting the importance of emotions for students' achievement and of achievement for the development of emotions.

Keywords: achievement emotion, anxiety, academic achievement, mathematics achievement, control-value theory

Research has shown that children's and adolescents' emotions are linked to their academic achievement. Typically, positive emotions such as enjoyment of learning show positive links with achievement, and negative emotions such as test anxiety show negative links (for overviews, see Goetz & Hall, 2013; Pekrun & Linnenbrink-Garcia, 2014; Zeidner, 1998). However, most of the available studies were correlational and do now allow any inferences about the causal ordering of emotion and achievement over time. As such, it remains unclear how the observed links should be interpreted. It is open to question if students' emotions impact their learning, if success and failure at learning influence the development of their emotions, if other variables cause the association, or if several of these possibilities are at work. Given the need to acquire knowledge about the antecedents of both students' achievement and their emotions, this is an issue of considerable theoretical and practical importance. To address this issue, the present investigation went beyond merely observing correlations at a single point in time and attempted to disentangle the causal ordering of these constructs across multiple waves of data collection and a developmental time span of several school years.

The investigation is based on a reciprocal effects model of emotion and achievement which posits that the two variables reciprocally influence each other over time. This stands in contrast to traditional unidirectional perspectives, which suggest that the link between emotion and achievement is simply due to effects of emotions on students' learning and performance. For example, correlations between test anxiety and students' achievement were interpreted as indicating that anxiety impacts achievement, and test anxiety theories put forward various suggestions about mediating mechanisms (e.g., cognitive interference, motivation; Zeidner, 1998, 2014). In a similar vein, in studies on affect and performance more generally, researchers have been interested in the impact of moods and emotions on cognitive performance and created

various theories targeting this influence (Clore & Huntsinger, 2009).

Certainly an analysis of the effects of emotions is important as it can document the functional relevance of emotions. However, what about the reverse causal direction, that is, the impact of achievement on the development of emotions? In other words, what about emotions as outcomes rather than causes of achievement? Herein we argue that this alternative causal direction is no less important. Beyond their functions, emotions are developmental outcomes that are in and of themselves important, because they are core components of identity, well-being, and health. By implication, researchers and practitioners alike should attend to the antecedents of students' emotions, and academic achievement is certainly one promising candidate---academic successes and failures possibly shape the development of emotions. As such, we concur with traditional perspectives in assuming that emotions impact achievement, but we also extend this notion and expect that achievement reciprocally influences emotion.

Empirical evidence on the causal ordering of students' emotions and their achievement is largely lacking, with a few exceptions pertaining to achievement-related anxiety. Specifically, longitudinal investigations suggested that K-12 students' test anxiety and academic achievement reciprocally influence each other (Meece, Wigfield, & Eccles, 1990; Pekrun, 1992). Furthermore, in a study of mathematics anxiety by Ma and Xu (2004), adolescents' achievement in mathematics had negative effects on their subsequent math anxiety, and anxiety had negative effects on subsequent achievement for two of the five time intervals included. The failure to find effects of anxiety on achievement for the other time intervals was likely due to the high stability of the achievement variable across waves (autogressive ßs > .95). For children's and adolescents' achievement emotions other than anxiety, evidence on reciprocal links with academic achievement is lacking.

In the following sections, we use Pekrun's (2006; Pekrun & Perry, 2014) control-value theory of achievement emotions to derive a theoretical framework for the reciprocal causation of emotion and achievement. This model expands upon previous models on the linkages of anxiety and boredom with achievement (Meece, Wigfield, & Eccles, 1990; Pekrun, 1992; Pekrun, Hall, Goetz, & Perry, 2014; Zeidner, 1998) by addressing not only negative emotions but positive emotions as well. We tested this model using a longitudinal dataset that examined adolescents' emotions and achievement in mathematics over a period of five school years.

A Reciprocal Effects Model of Emotion and Achievement

The control-value theory (Pekrun, 2006; Pekrun & Perry, 2014) integrates propositions from expectancy-value, attributional, and control approaches to achievement emotions (Folkman & Lazarus, 1985; Pekrun, 1992; Turner & Schallert, 2001; Weiner, 1985). Achievement emotions are defined as emotions related to achievement activities and their success and failure outcomes. The theory posits that these emotions are aroused by cognitive appraisals of control over, and the subjective value of, achievement activities and their outcomes. Control appraisals consist of perceptions of one's competence to successfully perform actions (i.e., academic self-concepts and self-efficacy expectations) and to attain outcomes (outcome expectations). Value appraisals pertain to the perceived importance of these activities and outcomes. Furthermore, the theory posits that these emotions, in turn, influence achievement behavior and performance. Since performance outcomes shape subsequent perceptions of control over performance, one important implication is that emotions, their appraisal antecedents, and their performance outcomes are linked by reciprocal causation. In terms of reciprocal causation, the theory is consistent with reciprocal effects models for variables such as students' self-concepts (Marsh & Craven, 2006; Marsh, Trautwein, Lüdtke, Köller, & Baumert, 2005), achievement goals

(Linnenbrink & Pintrich, 2002), and anxiety (Pekrun, 1992).

Effects of Emotion on Achievement

In the control-value theory, two dimensions describing human affect are used to distinguish types of emotions, namely valence (positive vs. negative or pleasant vs. unpleasant) and activation (activating vs. deactivating). Using these dimensions renders four broad groups of emotions: positive activating (e.g., enjoyment, hope, pride), positive deactivating (e.g., relaxation, relief), negative activating (e.g., anger, anxiety, shame), and negative deactivating (e.g., boredom, hopelessness). The theory proposes that these emotions influence students' cognitive resources, motivation to learn, and use of learning strategies, thus impacting their achievement (for an in-depth discussion, see Pekrun & Linnenbrink-Garcia, 2012).

Positive activating emotions (e.g., enjoyment of learning) are thought to preserve cognitive resources and focus attention on the learning task, support interest and intrinsic motivation, and facilitate deep learning. Accordingly, these emotions are expected to positively influence students' academic achievement under most task conditions. The opposite pattern of effects is proposed for negative deactivating emotions (boredom, hopelessness). These emotions are thought to reduce cognitive resources and task-related attention, to undermine both intrinsic and extrinsic motivation, and to promote shallow information processing. Accordingly, negative deactivating emotions are expected to negatively influence students' achievement.

Achievement effects are posited to be more variable for the remaining two categories of emotion. Deactivating positive emotions (relaxation, relief) are thought to reduce attention and effort in the moment, but they can strengthen long-term motivation to reengage with learning. Activating negative emotions (anger, anxiety, shame) are thought to reduce cognitive resources by inducing irrelevant thinking, such as worries about failure in test anxiety, and to undermine

intrinsic motivation. On the other hand, these emotions can trigger extrinsic motivation to invest effort to avoid failure. Furthermore, they can facilitate the use of more rigid learning strategies, such as rote memorization. However, notwithstanding individual differences regarding effects, we expect that the average overall influence of positive deactivating emotions on achievement is positive, and that the average overall influence of negative activating emotions is negative. For negative activating emotions such as anxiety, this hypothesis is consistent with the available evidence, which indicates that the correlations between these emotions and academic achievement are typically negative (Hembree, 1988; Zeidner, 1998, 2014).

Reverse Effects of Achievement on the Development of Emotion

Achievement reciprocally influences the appraisals that are considered to be proximal antecedents of emotion. As implied by the control-value theory as well as other models of achievement emotion (e.g., Folkman & Lazarus, 1985), positive emotions are thought to be promoted when perceived competence and control over achievement activities are high. For example, students should enjoy learning when they judge themselves competent to master the learning task, provided they are interested in the material. Negative emotions should result when perceived competence and control are low. For example, anxiety about an upcoming important exam should be high if students judge themselves incompetent to pass it. One possible exception is boredom, which could be promoted by high perceived competence if coupled with low task demands (i.e., under-challenge); however, in an academic context, boredom also has been found to be linked to students' lack of perceived competence and control (e.g., Pekrun et al., 2010). Perceived competence and control are thought to influence both students' momentary emotions within a specific situation and their habitual, re-occurring emotions, which are based on re-occurring appraisals and related control-value beliefs (for summaries of empirical evidence, see

Daniels & Stupnisky, 2012; Pekrun & Perry, 2014).

Perceived competence and control depend on students' individual achievement history, with success strengthening control and failure undermining it. Hence, achievement is expected to have positive effects on perceived control. Since achievement has positive effects on control, and control has positive effects on positive emotions, it follows that students' achievement should have positive effects on the development of positive emotions. Similarly, since achievement has positive effects on control, and control has negative effects on negative emotions, it follows that achievement should have negative effects on the development of negative emotions.

Feedback Loops of Emotion and Achievement over Time

Because emotions are posited to influence achievement and achievement, in turn, to influence emotion, the two constructs are thought to be linked by reciprocal causation over time. Both effects are expected to be positive for positive emotions, amounting to positive feedback loops, and both effects are expected to be negative for negative emotions, which also amounts to positive feedback loops. We acknowledge that there may be negative feedback loops for negative activating emotions in some students and under some conditions (e.g., failure on an exam instigating a student's anxiety, and anxiety eliciting effort to avoid failing the next exam; Pekrun, 1992). However, the existing evidence summarized above implies that negative activating emotions typically are aroused by failure and contribute to subsequent failure, suggesting that feedback loops should be positive for these emotions as well in the average student.

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Overview of the Present Research

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We tested the proposed reciprocal effects model using a longitudinal investigation of adolescents' development in mathematics (*Project for the Analysis of Learning and Achievement in Mathematics*, PALMA; see Frenzel, Goetz, Lüdtke, Pekrun, & Sutton, 2009; Frenzel, Pekrun,

Dicke, & Goetz, 2012; Marsh et al., in press; Murayama, Pekrun, Lichtenfeld, & vom Hofe,

2013; Murayama, Pekrun, Suzuki, Marsh, & Lichtenfeld, in press; Pekrun et al., 2007). To test

models of reciprocal causal linkages, designs are needed that assess both variables at multiple

points in time (Little, Preacher, Selig, & Card, 2007; McArdle, 2009; Rosel & Plewis, 2008).

Although such designs cannot fully rule out alternative causal explanations, they are better suited

to test causal propositions than cross-sectional designs or longitudinal designs that do not control

for prior levels of outcome variables. The PALMA study involved annual assessments of both

emotions and achievement, thus making it possible to conduct cross-lagged analyses examining

reciprocal causation. This study design made it possible to conduct multiple tests for the effects

of emotion on subsequent achievement, and of achievement on subsequent emotion, while

controlling for prior emotion and achievement levels.

For the present analysis, we used the grade 5 to 9 data from the PALMA study. As such,

the analysis involved five assessments for emotions and five assessments of achievement. These

assessments span the time from the beginning of secondary school (grade 5) to the end of

compulsory schooling in Germany (grade 9). At the start of secondary school, students are

selected into one of three tracks, including lower-track schools (Hauptschule), medium-track

schools (Realschule), and higher-track schools (Gymnasium), based on their elementary school

achievement. There is no additional school transition until the end of secondary school and

students usually remain in the same school.

As such, whereas math teachers and the specific classroom context can change, the broad

academic context for students' affective development remains relatively stable across this time

period. Specifically, contextual factors defining the emotional salience of achievement, such as

the visibility and frequency of feedback on achievement, remain stable during this period. The

stability of context does not preclude changes in individual levels of emotion (e.g., due to repeated success or failure and the influence of teachers and peers). However, given the stability of context, we expected relations between students' trait-like emotions considered in this study and their achievement to be stable as well, with effects of these emotions on achievement, and effects of achievement on emotions, showing equivalence (i.e., developmental equilibrium) across each of the one-year intervals included.

Seven distinct mathematics emotions were measured, including math-related enjoyment, pride, anger, anxiety, shame, boredom, and hopelessness. These emotions were selected based on their frequency and theoretical relevance (Pekrun et al., 2007). They were measured as trait-like variables, that is, students' habitual, re-occurring emotions in mathematics. Habitual emotions can influence learning and achievement over a longer time span, in contrast to momentary emotional episodes. In addition, we considered summary constructs of positive and negative affect derived from integrating scores for positive and negative emotions, respectively. As compared with multiple discrete emotions, these constructs render a more parsimonious description of students' affective development (Linnenbrink, 2007).

Achievement was assessed by students' end-of-the-year grades in mathematics, which are derived from multiple evaluations across the school year and represent students' cumulative performance. As such, these grades are suited to examining the impact of emotions on the long-term development of achievement. In addition, test scores from the PALMA mathematical achievement test (see Pekrun et al., 2007) were included to examine the generalizability of the findings across different achievement outcomes. These scores reflect generic mathematical competencies whereas grades represent students' curriculum-related achievement in the classroom, which should be more closely related to their emotions. Accordingly, we expected

effects to be stronger for grades than for the test scores.

Structural equation modeling was used to test the reciprocal effects model. To ensure that any observed relations were not mere artifacts of other plausible variables, we controlled for students' gender, intelligence, and family socio-economic status (SES) in the analysis. In addition, we examined the equivalence of relations across school tracks. We expected the effects linking emotion and achievement to be consistent over time and school tracks but modest in size due to controlling for autoregressive effects, intelligence, and demographic variables.

Method

Participants and Design

The sample consisted of German adolescents who participated in the PALMA longitudinal study (Pekrun et al., 2007). The study included annual assessments from grades 5 to 9 (2002-2006). Sampling and the assessments were conducted by the Data Processing and Research Center (DPC) of the International Association for the Evaluation of Educational Achievement (IEA). Samples were drawn from schools within the state of Bavaria and were representative of the student population of this state in terms of student characteristics such as gender, urban versus rural location, and family background (SES; for details, see Pekrun et al., 2007). At each grade level, the students answered the questionnaire towards the end of the school year. All instruments were administered in the students' classrooms by trained external test administrators.

At the first assessment (grade 5), the sample included 2,070 students from 42 schools (49.6% female, mean age = 11.7 years). The sample comprised students from all three school types within the Bavarian public secondary school system as described earlier, including lower-track schools (Hauptschule, 37.2%), intermediate-track schools (Realschule, 27.1%), and higher-track schools (Gymnasium, 35.7%). These three school types differ in average student

achievement due to the selection of students by entry-level achievement (see Murayama et al.,

2013). The distribution of students across tracks represents the distribution in the population. In

each subsequent year, the study not only tracked the students who had participated in the

previous assessment(s), but also incorporated those students who had not yet participated in the

study but had become members of PALMA classrooms at the time of the assessment (for details

on sampling procedures, see Pekrun et al., 2007). This strategy resulted in the following sample

sizes for the subsequent years: 2,059 students in grade 6 (50.0% female, mean age = 12.7 years);

2,397 students at grade 7 (50.1% female, mean age = 13.7 years); 2,410 students at grade 8

(50.5% female, mean age = 14.8 years); 2,528 students at grade 9 (51.1% female, mean age =

15.6 years). Across all five assessments (i.e., grades 5 to 9), a total of 3,425 students (49.7%

female) took part in the study. 38.7% of the total sample participated in all five assessments, and

9.0%, 18,9%, 15.1%, and 18.3% completed four, three, two, or one assessment(s), respectively.

Measures

  Emotions. Students' emotions in mathematics were measured using the Achievement

Emotions Questionnaire-Mathematics (AEQ-M; Pekrun, Goetz, Frenzel, Barchfeld, & Perry,

2011). The instructions for the instrument ask respondents to describe how they typically feel

when attending class, doing homework, and taking tests and exams in mathematics; in this way,

the AEQ-M assesses students' habitual, trait-like math-related emotions. The instrument

comprises seven scales measuring mathematics enjoyment (9 items, e.g., "I enjoy my math

class"), pride (8 items; e.g., "After a math test, I am proud of myself"), anger (8 items; e.g., "I

am annoyed during my math class"), anxiety (15 items; e.g., "I worry if the material is much too

difficult for me"), shame (8 items; e.g., "I am ashamed that I cannot answer my math teacher's

questions well"), hopelessness (6 items; e.g., "During the math test, I feel hopeless"), and

boredom (6 items; e.g., "My math homework bores me to death"). Participants responded on a 1 (*strongly disagree*) to 5 (*strongly agree*) scale, and the scores were summed to form the emotion indexes (Alpha range .86 to .92 across all scales and measurement occasions; see Table 1). The scores were also used to derive indexes for positive and negative affect factors combining positive and negative emotions, respectively (see Data Analysis section).

Achievement. Students' achievement was assessed by their end-of-the-year grades in mathematics as retrieved from school documents and by standardized test scores.

End-of-the-year grades. These grades are summative scores based on multiple exams within each school year; they represent students' achievement in the math curriculum for the respective year. Grades range from 1 (*excellent*) to 6 (*poor*). Grade scores were reversed prior to the analysis to ease interpretation.

Test scores. The test scores were derived from the PALMA Mathematics Achievement Test (Pekrun et al., 2007) which measures students' competencies in arithmetics, algebra, and geometry. The test includes different test forms for different grade levels and includes anchor items to allow for the linkage of test forms across assessments. The obtained scores were scaled using one-parameter logistic item-response theory (Rasch scaling; see Murayama et al., 2013).

Background variables. Demographic variables (gender and SES) and intelligence were included as covariates in the analysis. Gender was coded 1 = female, 2 = male.

Intelligence. Intelligence was measured at Time 1 (grade 5) using the 25-item nonverbal reasoning subtest of the German adaptation of Thorndike's Cognitive Abilities Test (Kognitiver Fähigkeitstest [KFT 4–12 + R]; Heller & Perleth, 2000).

Socio-economic status. SES was assessed by parent report using the EGP classification

(Erikson, Goldthorpe, & Portocarero, 1979), which consists of six ordered categories of parental

occupational status. Higher values represent higher SES.

Strategy of Data Analysis

Structural equation modeling (SEM; *Mplus*, Version 7; Muthén & Muthén, 2012) was

used to evaluate the reciprocal effects model. We estimated two sets of models. The first set used

grades, and the second set used test scores as the achievement measure. In both sets, eight

different models were estimated, including seven separate models for the discrete emotions and

one integrative model combining all emotions into two second-order positive and negative affect

factors. There was substantial multicollinearity between the emotion variables in the dataset

(Table 1). As such, the present analysis combines two strategies to deal with multicollinearity,

namely, using single variables (separate discrete emotion models) and combining them by

constructing summary variables (integrative affect models). The separate discrete emotion

models also served to examine if the links between emotion and achievement were sufficiently

similar to combine emotions into the summary positive and negative affect constructs.

All of the models represent a cross-lagged format, with emotion at each assessment

influencing subsequent achievement one year later, and achievement at each assessment

influencing subsequent emotion one year later (Figure 1). As such, the discrete emotion models

include four paths from emotion to achievement and four paths from achievement to emotion. In

the affect models, there were eight paths from positive and negative affect to achievement, eight

paths from achievement to positive and negative affect, as well as four paths from positive to

negative affect and four paths from negative to positive affect (Figure 1). The emotion variables

were modeled as latent constructs. The achievement measure and the three background measures

(gender, intelligence, and SES) were evaluated as manifest variables. The background variables were included as covariates; for each of these variables, directional paths to all of the emotion variables and to all of the achievement variables were included.

We estimated two versions for all of the 16 models. In the first version, autoregressive coefficients, cross-paths, and factor residual variances were freely estimated. In the second version, all three parameters were constrained to be invariant across time intervals (developmental equilibrium; e.g., the effects of Time n emotion on Time n+1 achievement were constrained to be the same from each wave to the next).

Measurement models for latent variables. The emotion scale items were used as indicators for each of the latent emotion variables. Following recommendations by Pekrun et al. (2011), a correlated uniqueness approach was used by including correlations between residuals for items representing the same setting (attending class, doing homework, and taking tests and exams in mathematics). In addition, correlations between residuals for identical emotion items across measurement occasions were included to control for systematic measurement error.

The latent affect factors were constructed in a two-step procedure. We first conducted separate confirmatory factor analyses for each of the seven emotions across the five assessments and derived emotion factor scores from these analyses (it was not possible to conduct a confirmatory factor analysis with all emotion items across all assessments, i.e., 60 x 5 = 300 items, due to computational limitations). We then used these factor scores to construct one integrative affect measurement model. For this model, factor scores for the positive emotions served as indicators for positive affect, and factor scores for the negative emotions served as indicators for negative affect. As such, the two affect constructs represent second-order factors.

Measurement equivalence across waves and school tracks. Prior to the main SEM analyses, we sought to establish measurement equivalence of the latent emotion and affect constructs over time and schools tracks. For each of the emotion and affect variables, we sequentially evaluated models of configural, metric, scalar, and residual invariance (Meredith, 1993). Configural invariance is defined by equal patterns of factor loadings. Metric invariance additionally requires equal factor loadings, scalar invariance requires equal factor loading and intercepts, and residual invariance requires equal factor loadings, intercepts, and residual variances. To establish equivalence of constructs for analyzing correlations and path coefficients, metric invariance is the minimum needed (Chen, 2007; Steenkamp & Baumgartner, 1998). To compare model fit, we followed recommendations by Chen (2007). Provided adequate sample size, for testing metric invariance, a change of $\geq$ -.010 in CFI, supplemented by a change of $\geq$ .015 in RMSEA or a change of $\geq$ .030 in SRMR would indicate noninvariance; for testing scalar or residual invariance, a change of $\geq$ -.010 in CFI, supplemented by a change of $\geq$ .015 in RMSEA or a change of $\geq$ .010 in SRMR would indicate noninvariance. As recommended, we did not use the χ^2 difference test because it is overly sensitive to sample size (Marsh, Balla, & McDonald, 1988).

Hierarchical data structure, estimator used, and missing values. As students were nested in schools, we corrected for the clustering of the data using the <type=complex> option implemented in Mplus (Muthén & Muthén, 2012). As noted, schools in the German public secondary school system differ in average student achievement due to the between-schools tracking based on achievement, indicating that nestedness within schools needs to be considered. The <type=complex> option corrects standard errors for nestedness while preserving use of the covariance matrix from the full sample to calculate parameters.

To estimate the model parameters, the robust maximum likelihood estimator (MLR) was employed which is robust to nonnormality of the observed variables. To make full use of the data from students with missing data, we applied the full information likelihood method (FIML; Enders, 2010). FIML has been found to result in trustworthy, unbiased estimates for missing values even in the case of large numbers of missing values (Enders, 2010) and to be an adequate method to manage missing data in longitudinal studies (Jeličič, Phelps, & Lerner, 2009). To examine the robustness of the analysis, we replicated the cross-lagged analyses for emotion and achievement with the subsample of students who participated in the study from the beginning (N = 2,070). As compared to the models using the full sample, there were no substantial differences in model fit (Δ CFI $\leq$ .007, Δ RMSEA $\leq$ .006, and Δ SRMR $\leq$ .007 for all of the models), and the substantive results were essentially the same (see Supplemental Material, Tables S6 and S7).

Goodness-of-fit indexes to evaluate model fit. We applied both absolute and incremental fit indices to evaluate the fit of the models, including the comparative fit index (CFI), the Tucker-Lewis index (TLI), the root-mean-square-error of approximation (RMSEA), and the standardized-root-mean residual (SRMR). Traditionally, values of CFI and TLI higher than .90 and close to .95, values of RMSEA lower than .06, and values of SRMR lower than .08 were interpreted as indicating good fit (Browne & Cudeck, 1993; Hu & Bentler, 1999). We report these fit indexes to make the present analysis comparable with previous research. However, it should be noted that the recommended cutoff values are often not met with datasets derived from more complex studies, suggesting that they should be used with caution (Heene, Hilbert, Draxler, Ziegler, & Bühner, 2011; Marsh, Hau, & Wen, 2004).

Results

Preliminary Analysis

Alpha coefficients for the emotion scales and manifest correlations for the emotions and achievement are outlined in Table 1 (for information about distributions, see Table S1). Correlations between the emotion measures indicated that enjoyment and pride were positively related, as were anger, anxiety, shame, hopelessness, and boredom. The correlations between positive and negative emotions were negative. Overall, this pattern of relations is consistent with previous evidence on the structures of students' academic emotions (e.g., Pekrun et al., 2011). Enjoyment and pride correlated positively with mathematics achievement in each year, whereas anger, anxiety, shame, hopelessness, and boredom correlated negatively with achievement.

Confirmatory Factor Analysis (CFA) for the Emotion Constructs

To further examine the relations between emotions, item-based CFA models including the seven emotions were estimated. This was done separately for the five measurement occasions. The models showed a good fit to the data (Supplemental Material, Table S2), supporting the measurement quality of the emotion variables. The latent correlations between the emotion variables showed the same pattern as the manifest correlations (Table 1). These correlations are corrected for measurement error and indicate that the latent emotion variables are closely related but nevertheless distinct (for similar findings with university students, see Pekrun et al., 2011). This is also true for emotions that might be presumed to constitute opposite ends of a bipolar continuum, such as enjoyment and boredom, which showed moderately negative relationships. The strongest correlations were found for neighboring, like-valenced emotions such as enjoyment and pride, and anxiety, shame, and hopelessness. In interpreting these correlations, it is important to note that the present study used the AEQ-M to assess students' trait-like emotions. As noted by Pekrun et al. (2011), like-valenced trait emotions are known to be strongly correlated, in contrast to state emotions which show more divergence.

For positive and negative affect based on the emotion factor scores, we conducted an integrative CFA including both constructs across all five measurement occasions. The fit for this CFA model was good (Supplemental Material, Table S3, configural invariance model). Latent correlations between the positive and negative affect factors were r = -.19, -.23, -.25, -.23, and -.21 (all ps < .01) for Times 1, 2, 3, 4, and 5, respectively, showing that the two affect constructs were sufficiently distinct.

Measurement Invariance of the Emotion Constructs over Time and School Tracks

Measurement invariance across waves was tested separately for the seven emotions and for positive and negative affect. The configural invariance models showed a good fit to the data, with CFI > .93, RMSEA < .03, and SRMR < .05 for all seven discrete emotion constructs (Supplemental Material, Table S3). As compared with these models, the loss of fit for the metric invariance models was Δ CFI $\leq$ -.004, Δ RMSEA $\leq$ .001, and Δ SRMR $\leq$ .006 for all models, indicating clear support for metric invariance for all of the emotions. The loss of fit for the scalar invariance models was Δ CFI $\leq$ -.007, Δ RMSEA $\leq$ .004, and Δ SRMR $\leq$ .007 for all of the emotions, documenting that scalar invariance was supported as well. The loss of fit for the residual invariance models was Δ CFI < -.010 for all emotions except shame, Δ CFI = -.010, as well as Δ RMSEA $\leq$ .003 and Δ SRMR $\leq$ .008 for all emotions, indicating support for residual invariance. For positive and negative affect, the loss of fit was Δ CFI $\leq$ .008, Δ RMSEA $\leq$ .004, and Δ SRMR $\leq$ .005 for the metric, intercept, and residual invariance models, demonstrating support for invariance for these second-order constructs as well. In sum, the findings show that the latent emotion and affect variables showed strong measurement equivalence over time, thus meeting the requirements to be included in longitudinal analysis. Furthermore, in supplemental analyses using multi-group analysis, the emotion constructs also showed strong measurement

equivalence across the three school tracks (see Supporting Information, Table S8).

Reciprocal Effects Models of Emotions and Achievement

The fit indexes provided support for the cross-lagged structural equation models for all seven emotions as well as positive and negative affect and across both measures of achievement. For all of the models freely estimating autoregressive effects, cross-lagged effects, and factor residual invariances, CFI was > .92, TLI > .90, RSMEA < .06, and SRMR < .08 (Table 2 and Supplemental Material, Table S4). When constraining autoregressive effects, cross-lagged effects, and factor residual variances to be equal across time intervals, the loss of fit was Δ CFI $\leq$ .003, Δ RMSEA $\leq$ .001, and Δ SRMR $\leq$ .003 for all of the models. These findings support the invariance of these parameters, suggesting developmental equilibrium in autoregressive stability and in the links of emotion and achievement across time. Accordingly, we adopted the constrained models for further interpretation, which have the additional advantage of providing more robust and precise parameter estimates (note that these constraints equalize unstandardized coefficients; to ease interpretation, we report standardized coefficients which can still differ due to the standardization procedure).

Emotions and grades. Factor loadings, path coefficients, and residual variances for the reciprocal effects models including grades are displayed in Table 3. In the enjoyment and pride models, both the emotion variables and students' achievement showed considerable stability over time, as indicated by the autoregressive effects for these variables. Furthermore, there were significant relations between the positive emotions and achievement at grade 5 in these models, latent rs = .26 and .26, ps < .001, for enjoyment and pride, respectively. Over and above these pre-existing relations, and despite autoregressive stability, results showed enjoyment and pride to positively predict each subsequent achievement outcome (β range .11 to .13, ps < .001) while

controlling for gender, intelligence, and SES. In addition, positive paths emerged from each achievement outcome to the subsequent enjoyment and pride variables (all βs = .11, ps < .001).

In the negative emotion models, there were substantial initial links between anger, anxiety, shame, boredom, and hopelessness at grade 5, latent rs = -.31, -.39, -.32, -.16, and -.37, respectively, ps < .001. Despite these links and the considerable stability of the emotion and achievement variables over time, anger, anxiety, shame, boredom, and hopelessness negatively predicted each subsequent achievement outcome (ß range -.08 to -.14, all ps < .001) while controlling for gender, intelligence, and SES. The effects were especially pronounced for anxiety and hopelessness (all ßs > -.11). In addition, negative paths from each achievement outcome to subsequent anger, anxiety, shame, boredom, and hopelessness were observed (ß range -.06 to -.14; all ps < .001).

These effects were similar across the two positive emotions, and similar across the five negative emotions, thus justifying their combination into positive and negative affect constructs. In the reciprocal effects model for positive and negative affect, the initial links with achievement were rs = .26 and -.33 for positive and negative affect, respectively, ps < .001. Despite these links and strong autoregressive coefficients for both positive and negative affect as well as achievement, positive affect positively predicted achievement, and negative affect negatively predicted achievement. Because both types of affect were included in the analysis, these findings indicate that positive and negative affect had independent predictive effects on achievement. Achievement, in turn, had positive predictive effects on positive affect and negative predictive effects on negative affect. Regarding cross-paths between positive and negative affect, we had not expected any effects of this type and none of the paths were significant.

Emotions and test scores. The findings for emotions and test scores replicated the results

for grades, demonstrating generalizability across different achievement measures (Supplemental Material, Table S5). As expected, however, the effects were weaker than for grades. Positive emotions were positive predictors of test scores, ß range = .04 to .05, and negative emotions were negative predictors, ß range = -.03 to -.08, all ps < .001. Test scores were a positive predictor of positive emotions, ß range = .05 to .07, and a negative predictor of negative emotions, ß range = -.04 to -.11, all ps < .001. In the positive and negative affect model, positive affect was not a significant predictor of test scores (all ßs = .01, *ns*), whereas negative affect predicted test scores, ß range = -.06 to -.07, ps < .001. Test scores, in turn, were a positive predictor of positive affect, ßs = .03, ps < .01, and a negative predictor of negative affect, ß range = -.04 to -.05, ps < .001.

Effects of the covariates. Intelligence had positive effects on grades and test scores as well as negative effects on students' anger, anxiety, shame, and hopelessness (Tables 3 and S5). SES also had positive, albeit weaker, effects on math achievement. Gender had significant effects on all of the emotions except anger, indicating that girls reported lower enjoyment, pride, and boredom, and higher anxiety, shame, and hopelessness in mathematics than boys.

Equivalence of effects across school tracks. In supplemental analyses, we used multi-group analysis to examine the equivalence of cross-paths, autoregressive effects, and effects of covariates across the three school tracks. Comparing models constraining versus not constraining these coefficients to be invariant (using Chen's, 2007, criteria outlined in the Data Analysis section), the findings provide robust support for invariance across tracks for all of the emotion and affect models and both math grades and test scores (see Tables S9, S10).

Discussion

The findings of this study provide robust evidence for the proposed reciprocal effects model of emotion and achievement. As indicated by longitudinal SEM, adolescents' math-

related positive emotions (enjoyment and pride) positively predicted their subsequent end-of-the-

year math grades, and grades, in turn, positively predicted the development of positive emotions.

Math-related negative emotions (anger, anxiety, shame, hopelessness, and boredom) were

negative predictors of subsequent math grades, and grades, in turn, were a negative predictor for

the development of negative emotions. Similar predictive effects were obtained for the

integrative constructs of positive and negative affect, respectively, and for test scores as a

measure of achievement. The findings were consistent across models for the seven discrete

emotions, the combined positive and negative affect model, four time intervals, two different

measures of achievement (grades, test scores), and the three school tracks while controlling for

students' gender, intelligence, and SES. All of the effects were significant with the single

exception of the effects of positive affect on test scores.

Because prior links between emotion and achievement as well as intelligence and

demographic background variables were controlled, the path coefficients are likely to represent

effects of emotion on achievement, and vice versa, rather than simply the influence of prior

emotion, prior achievement, gender, intelligence, or socio-economic status. As expected, the size

of these coefficients was modest. However, it is important to note that the coefficients represent

incremental predictive effects due to prior emotion and achievement being controlled. Thus, the

coefficients represent effects of each variable on change in the other from one assessment to the

next, rather than effects on the absolute levels of these variables. Furthermore, both emotion and

achievement showed considerable stability over time, leaving little variance to be explained and

making it difficult to detect the effects of additional variables. From this perspective, the

consistency of effects lends credibility to the notion that emotion and achievement are indeed

linked by reciprocal causation over time.

Reciprocal Effects Linking Emotion and Achievement

The findings are congruent with previous evidence showing that emotions and academic achievement are correlated (Goetz & Hall, 2013; Pekrun & Linnenbrink-Garcia, 2014; Zeidner, 1998). However, they go beyond correlational evidence by disentangling the directional effects underlying the emotion-achievement link. Specifically, the findings suggest that emotions indeed have an influence on adolescents' achievement, over and above the effects of general cognitive ability and prior accomplishments. These effects are in line with Pekrun's (2006) control-value theory which posits that emotions influence learning and achievement outcomes.

Of specific importance is the finding that adolescents' positive emotions in mathematics had positive predictive effects on their math grades over time. Previous research has produced mixed findings on the relation between students' positive affect and their learning, with most studies reporting positive relations (see Linnenbrink, 2007) but some others null findings (e.g., Pekrun, Elliot, & Maier, 2009). The present analysis suggests that positive emotions can have positive effects, in line with theory and the views of educational practitioners. However, the effects were weaker for positive emotion than for the negative emotion constructs, and did not reach significance for the predictive effect of positive affect on test scores. Future research should examine possible reasons why negative emotion is a stronger predictor of students' academic achievement than positive emotion. This difference may relate to general asymmetries in the impact of negative versus positive states and events on human memory and action (see e.g., Baumeister, Bratslavsky, Finkenauer, & Vohs, 2001).

The results also contribute to our understanding of the developmental origins of students' emotions. The findings suggest that achievement impacts the development of emotions. It appears that doing well in school can strengthen students' positive emotions and reduce their

negative emotions over time, whereas doing poorly in school undermines positive emotions and exacerbates negative emotions. These effects are likely mediated by students' perceptions of competence and control over achievement, with high control promoting enjoyment and pride and low control leading to negative emotions (e.g., Pekrun et al., 2010).

Taken together, these effects amount to positive developmental feedback loops linking emotions and achievement. As noted, a few longitudinal studies have found that students' test anxiety and their achievement were linked by positive feedback loops (Meece, Wigfield, & Eccles, 1990; Pekrun, 1992). The present research adds to this literature by showing that emotions other than anxiety share similar links with achievement. As such, it would appear that unidirectional models are unable to adequately capture the complex reality of students' emotions. Rather, systems-oriented perspectives are needed that take more complex patterns of causal links into account, including feedback loops between emotions, their antecedents, and their effects.

Discrete Emotions versus General Affect

It is noteworthy that the cross-paths were similar across different discrete emotions. For effects of achievement on emotion, this is to be expected, as success and failure are thought to impact the development of different positive and negative emotions in similar ways. As outlined in our reciprocal effects model, success is expected to generally increase perceived control, thus enhancing positive emotions, and failure is expected to decrease control, leading to negative emotions. However, regarding effects of emotion on achievement, emotion theories such as the control-value theory (Pekrun, 2006) imply that the effects of some emotions (e.g., deactivating negative emotions such as boredom) may be more consistent than the effects of other emotions (e.g., activating negative emotions such as anxiety). Instead, the findings clearly indicate that the predictive effects of emotions on students' long-term achievement were also similar across

different emotions. Accordingly, whereas constructs of discrete emotions are needed to explain the impact of emotions on functional mechanisms and different types of cognitive performance, parsimonious summary constructs of positive and negative affect may be sufficient to explain their relations with overall academic achievement. This possibility is underscored by the robust findings for positive and negative affect documented in the present analysis.

Effects of Gender, Intelligence, and SES

The findings on gender differences are consistent with previous evidence showing that girls report less enjoyment and more anxiety and shame in mathematics even if they perform as well as boys. Lower competence beliefs and perceived values in mathematics may be possible explanations (Goetz, Bieg, Lüdtke, Pekrun, & Hall, 2013). However, girls reported less boredom than boys, in line with previous evidence (Pekrun et al., 2010). As such, the findings suggest that girls exhibit a more maladaptive profile of math emotions, except for boredom.

As expected, intelligence had substantial predictive effects on the achievement variables. Furthermore, intelligence had negative effects on math-related anger, anxiety, shame, and hopelessness. Given that students' mathematics achievement was included in the analysis, this finding suggests that higher general cognitive ability can help to reduce negative mathematics emotions, above and beyond any effects of students' academic success in mathematics. Finally, SES also had positive, albeit weaker, effects on math achievement, suggesting that the family exerts an influence on students' achievement, over and above any effects of cognitive ability.

Limitations, Suggestions for Future Research, and Implications for Practice

The present study represents a significant advancement over previous research, because it documents reciprocal effects of emotion and achievement over time while controlling for general cognitive ability and critical demographic background variables. Nevertheless, several

limitations should be considered when interpreting the study findings and can be used to suggest

directions for future research.

Methodological considerations. As compared with experimental studies, the power of

non-experimental field studies to derive causal conclusions is limited. As such, although the

present analysis used multi-wave longitudinal structural equation modeling and controlled for

related variables and autoregressive effects, the possibility still exists that our findings are

attributable to other variables that were not included in the study. On the other hand, field studies

may be more ecologically valid than experimental emotion studies, which are limited in terms of

situational representativeness and ethical concerns about experimentally manipulating emotions.

Furthermore, statistical power is higher in field studies such as the present one due to large

sample size. To balance the benefits and drawbacks of different methodologies and make

headway in this avenue of research, future studies should further pursue the approach taken

herein while complementing this approach with experimental studies.

Achievement was assessed by students' end-of-year grades and test scores. By using

grades, we sought to employ an ecologically valid measure of student achievement (for a similar

procedure, see Pekrun et al., 2014). As is typical for grades, more detailed information about

reliability was not available; as such, it was not possible to disattenuate the link between

emotions and grades for potential unreliability of this achievement measure. However, in

German secondary schools, end-of-the-year grades are summative scores based on multiple

exams within each school year, which may boost their reliability in comparison to grades on

single exams. In the present study, this is supported by the stability of grades across years (all ßs

> .50), which could be considered as a lower bound to reliability. Furthermore, from the

perspective of grades as sources of students' emotional development, they could be seen as

having almost perfect reliability---grades, rather than objective achievement, provide the feedback that shapes students' perceptions of success and failure and any development based on these perceptions. In addition, an advantage of grades is that they represent achievement in terms of the math curriculum taught in students' classes. They represent the specific contents learned by students and may be superior to alternative measures in terms of curricular validity. Finally, the findings based on grades proved to be generalizable, as the results were essentially the same for test scores.

  Substantive issues. The present research examined achievement emotions as experienced by adolescents in the domain of mathematics. It is open to question whether the present findings would generalize to other age groups, such as elementary school children or post-secondary students. Furthermore, it is possible that there is individual variation in the link between emotions and achievement. To examine such variation, within-person analyses of the relations between emotion and achievement over time are needed (e.g., by using experience sampling methodology; Goetz, Sticca, Pekrun, Murayama, & Elliot, 2016). Because the present research involved samples of German adolescents, it also remains an open question as to whether the findings would generalize to students in other cultures. Additionally, future research should explore if these findings generalize to emotions in achievement domains other than mathematics,

  The study considered a broad range of important mathematics emotions but did not include an exhaustive list of emotions. It is open to question whether the observed reciprocal effects would also occur for emotions not assessed herein. Specifically, the study did not include students' deactivating positive emotions, such as relief and relaxation. Future studies could explore how these emotions are linked to students' academic achievement. Furthermore, the present study examined students' trait-like emotions which are known to be highly correlated

(Pekrun et al., 2011), which makes it difficult to determine unique variance in achievement

attributable to different emotions. Future research should examine the unique impact of multiple

state emotions, which are less correlated (Goetz et al., 2016), on students' learning.

Finally, the study addressed the overall developmental relations between emotion and

achievement but did not examine the mechanisms that mediate the observed links. In the

proposed model of reciprocal effects, it is posited that effects of emotion on achievement are due

to the influence of emotions on cognitive resources, motivation, and strategy use. The effects of

achievement outcomes on the development of emotion are thought to be mediated by perceptions

of competence and control over performance, and could additionally be mediated by value

appraisals. More research on the link between emotion and achievement as mediated by these

cognitive and motivational mechanisms is needed to better understand students' emotions and

their relations with important school outcomes.

Implications for educational practice. Two important messages follow from the present

research. First, the results suggest that emotions have effects on adolescent students' academic

achievement, and that these effects are not merely an epiphenomenon of prior performance---

more likely, they represent a true causal influence of students' emotion experiences. By

implication, the findings suggest that educators, administrators, and parents alike should consider

intensifying efforts that strengthen adolescents' positive emotions and minimize their negative

emotions. Second, the results imply that achievement outcomes reciprocally influence students'

emotions, suggesting that successful performance attainment and positive achievement feedback

can facilitate the development of positive emotions, and failure experiences can contribute to the

development of negative emotions. Accordingly, providing students with opportunities to

experience success (e.g., using intrapersonal standards to evaluate achievement; emphasizing

mastery over competition goals) may help to promote positive emotions and prevent negative

emotions (also see Pekrun, Cusack, Murayama, Elliot, & Thomas, 2014). By documenting the

influence of achievement outcomes on students' emotions, the present findings elucidate one

important factor that can be targeted by educators to reduce students' negative affect and

facilitate the development of emotional well-being.

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Table 1

Alpha Coefficients and Pearson Product-Moment Correlations for Emotions and Achievement

	Enjoyment	Pride	Anger	Anxiety	Shame	Boredom	Hopelessness
Enjoyment	(.87) [a]	.83	-.63	-.53	-.36	-.60	-.48
	(.87)	.84	-.65	-.51	-.33	-.63	-.51
	(.88)	.86	-.65	-.48	-.30	-.62	-.49
	(.85)	.86	-.61	-.46	-.30	-.57	-.49
	(.89)	.88	-.56	-.42	-.23	-.50	-.46
Pride	.73	(.87)	-.42	-.37	-.25	-.39	-.38
	.74	(.88)	-.51	-.42	-.27	-.50	-.44
	.75	(.88)	-.50	-.40	-.26	-.47	-.43
	.76	(.89)	-.48	-.37	-.25	-.47	-.43
	.78	(.89)	-.46	-.35	-.18	-.43	-.39
Anger	-.55	-.35	(.87)	.88	.76	.84	.93
	-.55	-.40	(.88)	.86	.73	.82	.82
	-.56	-.39	(.87)	.86	.69	.79	.83
	-.53	-.39	(.87)	.86	.68	.72	.85
	-.49	-.37	(.88)	.87	.68	.75	.84
Anxiety	-.41	-.29	.74	(.90)	.92	.67	.90
	-.39	-.31	.74	(.90)	.92	.60	.91
	-.35	-.29	.74	(.91)	.87	.53	.92
	-.33	-.26	.73	(.91)	.88	.51	.92
	-.32	-.26	.73	(.92)	.87	.55	.91
Shame	-.27	-.19	.65	.78	(.86)	.55	.82
	-.23	-.18	.62	.77	(.88)	.48	.79
	-.20	-.16	.58	.74	(.87)	.37	.78
	-.19	-.16	.57	.75	(.87)	.36	.78
	-.14	-.09	.58	.74	(.89)	.42	.78
Boredom	-.51	-.27	.70	.44	.37	(.86)	.63
	-.53	-.35	.70	.39	.31	(.89)	.60
	-.52	-.33	.66	.33	.25	(.90)	.54
	-.48	-.32	.61	.29	.23	(.90)	.56
	-.41	-.29	.64	.32	.28	(.90)	.57
Hopelessness	-.41	-.34	.72	.83	.74	.43	(.86)
	-.43	-.38	.74	.86	.73	.42	(.88)
	-.42	-.37	.74	.86	.71	.37	(.88)
	-.43	-.37	.75	.86	.70	.37	(.87)
	-.43	-.37	.76	.86	.68	.38	(.83)
Achievement (end-of-year grades)	.20	.18	-.30	-.37	-.33	-.13	-.38
	.25	.22	-.30	-.38	-.34	-.11	-.40
	.34	.29	-.34	-.37	-.29	-.17	-.42
	.41	.36	-.36	-.37	-.29	-.16	-.41
	.45	.38	-.42	-.40	-.29	-.24	-.46

Note. [a] 1st, 2nd, 3rd, 4th, 5th coefficient in each column: Grade 5, 6, 7, 8, and 9, respectively. Coefficients below main diagonal are manifest correlations. Coefficients above main diagonal are latent correlations based on confirmatory factor analyses for each wave. Coefficients in parentheses are Cronbach's Alphas. $p < .01$ for all coefficients.

Table 2

Reciprocal Effects Models for Emotion and Grades: Fit Indexes

	χ^2	*df*	CFI	TLI	RMSEA	SRMR
	Cross-paths, autoregressive effects, and residual variances					
Model			*freely estimated*			
Enjoyment	4125.280**	1147	.940	.928	.027	.052
Pride	2729.201**	722	.940	.928	.028	.048
Anger	3238.875**	918	.941	.927	.027	.049
Anxiety	9091.434**	2992	.920	.909	.024	.050
Shame	2168.850**	907	.965	.957	.020	.044
Boredom	1384.409**	532	.974	.966	.021	.038
Hopelessness	2018.158**	562	.959	.949	.027	.055
Positive and negative affect	6837.618**	685	.947	.930	.051	.075
	Cross-paths, autoregressive effects, and residual variances					
			invariant across waves			
Enjoyment	4210.435**	1165	.938	.927	.027	.053
Pride	2794.131**	740	.942	.930	.028	.049
Anger	3285.829**	936	.940	.928	.027	.050
Anxiety	9148.887**	3010	.920	.909	.024	.050
Shame	2244.200**	925	.964	.956	.020	.045
Boredom	1500.094**	550	.971	.963	.022	.041
Hopelessness	2058.064**	580	.959	.950	.027	.055
Positive and negative affect	6976.520**	721	.946	.933	.050	.078

** *p* < .01.

Table 3

Reciprocal Effects Models for Emotion and Grades: Standardized Factor Loadings, Path Coefficients, and Residual Variances

	Enjoyment model		Pride model		Anger model		Anxiety model		Shame model	
	Enjoyment	Grades	Pride	Grades	Anger	Grades	Anxiety	Grades	Shame	Grades
Factor loadings	.37-.81[a]		.55-.77 [a]		.58-.77 [a]		.44-.77 [a]		.48-.78 [a]	
Autoregressive effects										
T1 → T2	.67***	.57***	.62***	.57***	.58***	.57***	.60***	.56***	.62***	.58***
T2 → T3	.66***	.59***	.64***	.59***	.61***	.59***	.64***	.58***	.61***	.60***
T3 → T4	.66***	.61***	.65***	.61***	.62***	.60***	.66***	.60***	.60***	.62***
T4 → T5	.65***	.59***	.65***	.59***	.62***	.58***	.68***	.58***	.60***	.60***
	Grades →	*Enjoyment*	*Grades →*	*Pride*	*Anger →*	*Grades*	*Grades→*	*Anxiety*	*Grades →*	*Shame*
Cross-lagged effects	*Enjoyment*	*→ Grades*	*Pride*	*→ Grades*	*Grades*	*→ Anger*	*Anxiety*	*→ Grades*	*Shame*	*→ Grades*
T1 → T2	.11***	.13***	.11***	.11***	-.12***	-.10***	-.08***	-.11***	-.06***	-.09***
T2 → T3	.11***	.13***	.11***	.12***	-.13***	-.10***	-.08***	-.13***	-.06***	-.09***
T3 → T4	.11***	.13***	.11***	.12***	-.14***	-.10***	-.07***	-.14***	-.06***	-.09***
T4 → T5	.11***	.12***	.11***	.12***	-.13***	-.10***	-.07***	-.14***	-.06***	-.08***
Effects of Covariates at T1										
Gender	.14***	.02	.17***	.02	-.03	.02	-.16***	.02	-.09**	.02
Intelligence	-.02	.40***	-.00	.40***	-.12***	.40***	-.18***	.40***	-.17***	.40***
SES	-.05**	.09***	.05*	.09***	.03	.09***	-.04	.09***	-.03	-.09***
Residual Variances										
T1	.98	.82	.97	.82	.98	.82	.94	.82	.96	.82
T2	.50	.57	.57	.58	.62	.57	.59	.57	.55	.58
T3	.51	.56	.54	.56	.59	.56	.53	.56	.58	.56
T4	.52	.58	.53	.58	.57	.57	.50	.58	.60	.58
T5	.52	.56	.52	.56	.57	.55	.50	.56	.61	.56

Table 3 (continued)

	Boredom model		Hopelessness model		Positive and negative affect model		
	Boredom	Grades	Hopelessn.	Grades	Pos. affect [b]	Neg. affect [b]	Grades
Factor loadings	.56-.77 [a]		.63-.85 [a]		.77-.96 [a]	.41-.93 [a]	
Autoregressive effects							
T1 → T2	.63***	.59***	.53***	.56***	.80***	.74***	.54***
T2 → T3	.65***	.61***	.57***	.59***	.81***	.76***	.56***
T3 → T4	.66***	.63***	.58***	.60***	.82***	.78***	.57***
T4 → T5	.66***	.61***	.59***	.58***	.82***	.79***	.56***
	Grades → *Boredom*	*Boredom* *→ Grades*	*Grades →* *Hopelessn.*	*Hopelessn.* *→ Grades*	*Grades →* *Pos. affect*	*Grades →* *Neg. affect*	*Pos. affect* *→ Grades*	*Neg. affect* *→ Grades*
Cross-lagged effects								
T1 → T2	-.06***	-.08***	-.11***	-.11***	.05***	-.04***	.10***	-.08***
T2 → T3	-.06***	-.08***	-.12***	-.12***	.05***	-.04***	.10***	-.08***
T3 → T4	-.06***	-.09***	-.12***	-.13***	.05***	-.04***	.10***	-.09***
T4 → T5	-.06***	-.09***	-.11***	-.13***	.05***	-.04***	.10***	-.09***
Effects of Covariates at T1								
Gender	.09**	.02	-.16***	.02	.15***	-.13***	.02	
Intelligence	.00	.40***	-.13***	.40***	-.02	-.15***	.40***	
SES	-.03	.09***	-.04	.09***	-.05**	-.03	.09***	
Residual Variances								
T1	.99	.82	.95	.82	.97	.96	.82	
T2	.59	.58	.66	.58	.34	.41	.58	
T3	.56	.56	.61	.58	.33	.36	.57	
T4	.54	.57	.60	.56	.32	.35	.59	
T5	.53	.55	.59	.56	.32	.33	.57	

Note. [a] Range of factor loadings. $p < .001$ for all loadings. [b] Cross-paths between positive and negative affect were not significant (all ps > .05).

* $p < .05$. ** $p < .01$. *** $p < .001$.

Figure 1. Basic structure of cross-lagged reciprocal effects models. Upper part: emotion and achievement. Lower part: positive affect, negative affect, and achievement. The models include cross-lagged effects, autoregressive effects, and directional paths from the covariates to emotion or affect and achievement at all waves. Correlations between the covariates and between residuals are not displayed.
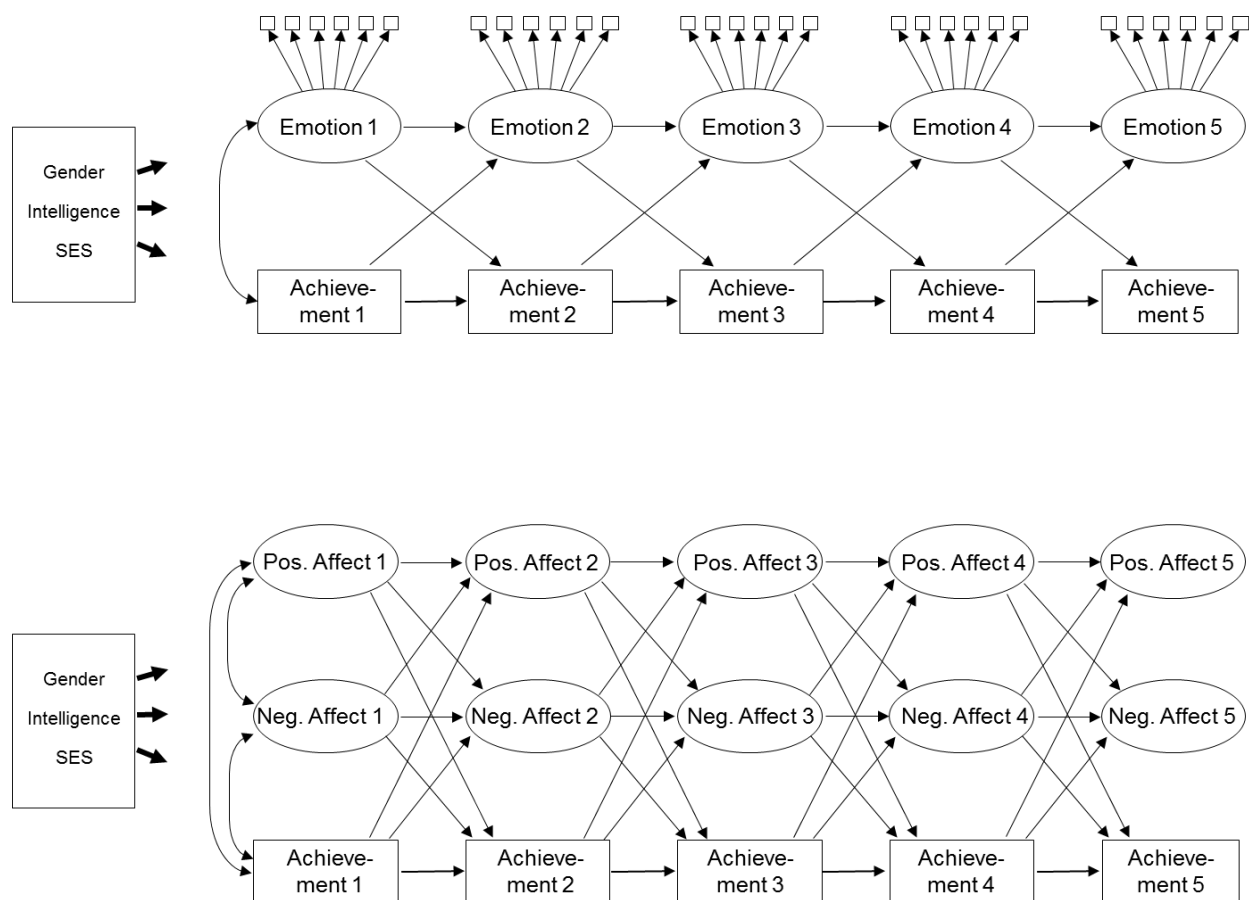
Supporting Information

Table S1

Descriptive Statistics for Emotions and Achievement: Means, Standard Deviations, Skewness, and Kurtosis

	Time 1		Time 2		Time 3		Time 4		Time 5	
	M / SD	Skew/ Kurt.	M / SD	Skew/ Kurt.	M / SD	Skew/ Kurt.	M / SD	Skew/ Kurt.	M / SD	Skew/ Kurt.
Enjoyment	29.90	0.09	26.83	0.17	24.56	0.30	23.99	0.24	23.71	0.27
	7.63	0.55	7.65	0.37	7.40	0.19	7.11	0.20	6.99	0.00
Pride	22.55	0.05	20.86	0.05	19.17	0.24	18.78	0.25	18.53	0.23
	6.54	0.54	6.56	0.49	6.37	0.32	6.32	0.16	6.13	0.22
Anger	16.03	1.03	17.73	0.75	19.57	0.52	19.33	0.56	19.40	0.55
	7.35	0.42	7.78	0.17	7.78	0.42	7.69	0.31	7.54	0.30
Anxiety	34.00	0.64	34.76	0.61	35.31	0.59	33.85	0.66	33.95	0.67
	12.31	0.15	12.66	0.18	12.90	0.19	12.49	0.01	12.40	0.04
Shame	14.99	1.17	15.30	1.12	15.03	1.10	14.48	1.22	14.36	1.25
	6.85	0.91	7.14	0.72	6.82	0.63	6.74	1.14	6.59	1.18
Hopelessn.	12.15	1.15	12.86	0.77	13.53	0.42	13.41	0.43	13.44	0.51
	5.84	0.65	6.20	0.22	6.30	0.69	6.36	0.52	6.22	0.36
Boredom	11.73	1.00	13.66	0.91	15.39	0.78	15.55	0.78	15.54	0.76
	5.77	0.26	6.37	0.11	6.47	0.16	6.24	0.23	6.07	0.17
Grades	3.09	0.18	3.16	-0.16	3.36	-0.09	3.29	-0.16	3.23	-0.23
	0.91	-0.24	0.96	0.03	0.94	-0.20	0.95	-0.32	0.99	.42
Test scores	a	0.08	a	0.25	a	-0.06	a	0.04	a	-0.39
		0.65		0.30		0.22		-0.29		0.79

Note. Times 1-5 = Grades 5-9. Emotion scores are sum scores of manifest items.

[a] Test scores were Rasch-scaled with $M = 1,000$, $SD = 100$ at all waves.

Table S2

Confirmatory Factor Analyses for the Discrete Emotion Constructs

Model	χ^2	*df*	CFI	TLI	RMSEA	SRMR
Time 1	3131.430**	1081	.957	.932	.030	.043
Time 2	3443.127**	1081	.955	.929	.033	.048
Time 3	3997.959**	1081	.953	.925	.034	.050
Time 4	4381.458**	1081	.946	.915	.036	.053
Time 5	4413.424**	1081	.95	.92	.035	.052

Note. Separate confirmatory factor analyses for the five waves including enjoyment, pride, anger, anxiety, shame, boredom, and hopelessness.

** $p < .01$.

Table S3

Measurement Equivalence of Emotion Constructs Across Waves

Model	Configural Invariance				Metric Invariance				Scalar Invariance				Residual Invariance			
	CFI	TLI	RMSEA	SRMR	CFI	TLI	RMSEA	SRMR	CFI	TLI	RMSEA	SRMR	CFI	TLI	RMSEA	SRMR
Enjoyment	.968	.961	.022	.036	.964	.957	.023	.042	.957	.950	.025	.049	.950	.945	.026	.057
Pride	.979	.973	.020	.025	.978	.973	.020	.028	.974	.969	.021	.030	.967	.963	.023	.036
Anger	.967	.958	.023	.032	.966	.959	.022	.034	.960	.953	.024	.035	.956	.951	.024	.037
Anxiety	.936	.927	.023	.043	.935	.927	.023	.045	.930	.923	.024	.045	.923	.917	.024	.048
Shame	.987	.983	.014	.026	.986	.982	.014	.027	.980	.976	.016	.028	.970	.966	.019	.034
Boredom	.991	.987	.015	.021	.989	.986	.016	.026	.983	.978	.020	.031	.979	.975	.021	.033
Hopelessness	.988	.984	.018	.020	.986	.982	.018	.023	.983	.981	.019	.024	.979	.977	.021	.028
Positive and negative affect	.957	.940	.054	.077	.949	.931	.058	.082	.949	.935	.057	.082	.942	.929	.059	.083

Table S4

Reciprocal Effects Models for Emotion and Test Scores: Fit Indexes

Model	χ^2	*df*	CFI	TLI	RMSEA	SRMR
			Cross-paths, autoregressive effects, and residual variances freely estimated			
Enjoyment	3998.214**	1147	.950	.940	.027	.050
Pride	2590.262**	722	.958	.947	.027	.045
Anger	3268.875**	918	.950	.939	.027	.048
Anxiety	9206.366**	2992	.925	.915	.024	.053
Shame	2314.749**	907	.968	.960	.021	.043
Boredom	1596.453**	532	.974	.966	.024	.038
Hopelessness	1842.295**	562	.971	.964	.025	.049
Positive and negative affect	6479.718**	685	.954	.940	.050	.073
			Cross-paths, autoregressive effects, and residual variances invariant across waves			
Enjoyment	4136.124**	1165	.948	.938	.027	.052
Pride	2711.883**	740	.955	.946	.027	.046
Anger	3370.445**	936	.948	.938	.027	.048
Anxiety	9311.381**	3010	.924	.915	.024	.053
Shame	2428.962**	925	.966	.958	.021	.045
Boredom	1761.501**	550	.971	.963	.025	.041
Hopelessness	1939.106**	580	.970	.963	.026	.049
Positive and negative affect	6659.495**	721	.953	.942	.049	.075

** $p < .01$.

Table S5

Reciprocal Effects Models for Emotion and Test Scores: Standardized Factor Loadings, Path Coefficients, and Residual Variances

	Enjoyment model		Pride model		Anger model		Anxiety model		Shame model	
	Enjoyment	Test	Pride	Test	Anger	Test	Anxiety	Test	Shame	Test
Factor loadings	.33-.82 [a]		.56-.77 [a]		.59-.77 [a]		.43-.77 [a]		.47-.78 [a]	
Autoregressive effects										
T1 → T2	.68***	.70***	.63***	.70***	.58***	.68***	.59***	.69***	.62***	.69***
T2 → T3	.68***	.70***	.66***	.71***	.61***	.69***	.65***	.69***	.61***	.70***
T3 → T4	.68***	.69***	.67***	.69***	.63***	.67***	.67***	.68***	.60***	.68***
T4 → T5	.68***	.70***	.67***	.70***	.63***	.68***	.68***	.69***	.60***	.69***
	Test →	*Enjoyment*	*Test →*	*Pride*	*Test →*	*Anger*	*Test →*	*Anxiety*	*Test →*	*Shame*
Cross-lagged effects	*Enjoyment*	*→ Test*	*Pride*	*→ Test*	*Anger*	*→ Test*	*Anxiety*	*→ Test*	*Shame*	*→ Test*
T1 → T2	.07***	.04***	.06***	.04***	-.11***	-.07***	-.09***	-.06***	-.08***	-.06***
T2 → T3	.07***	.04***	.06***	.04***	-.10***	-.07***	-.09***	-.06***	-.08***	-.06***
T3 → T4	.07***	.04***	.05***	.04***	-.10***	-.08***	-.08***	-.07***	-.08***	-.06***
T4 → T5	.07***	.04***	.05***	.04***	-.10***	-.08***	-.08***	-.07***	-.09***	-.06***
Effects of Covariates at T1										
Gender	.14***	.13***	.17***	.13***	-.03	.13***	-.16***	.13***	-.09**	.13***
Intelligence	-.02	.56***	-.00	.56***	-.12***	.56***	-.17***	.56***	-.17***	.56***
SES	-.06**	.12***	-.05*	.12***	-.03	.12***	-.03	.12***	-.03	.12***
Residual Variances										
T1	.98	.62	.97	.62	.98	.62	.94	.62	.96	.62
T2	.51	.30	.58	.30	.63	.30	.61	.30	.56	.30
T3	.52	.31	.54	.31	.59	.31	.54	.31	.59	.31
T4	.52	.30	.54	.30	.58	.30	.50	.30	.59	.30
T5	.53	.30	.53	.30	.57	.30	.50	.30	.61	.30

Table S5 *(continued)*

	Boredom model		Hopelessness model		Positive and negative affect model		
	Boredom	Test	Hopelessn.	Test	Pos. Affect[b]	Neg. Affect[b]	Test
Factor loadings	.57-.77[a]		.59-.85[a]		.77-.97[a]	.42-.93[a]	
Autoregressive effects							
T1 → T2	.64***	.70***	.54***	.69***	.81***	.75***	.68***
T2 → T3	.66***	.70***	.58***	.69***	.82***	.77***	.69***
T3 → T4	.67***	.69***	.60***	.68***	.82***	.79***	.67***
T4 → T5	.67***	.70***	.61***	.69***	.82***	.80***	.68***

Cross-lagged effects	Test → Boredom	Boredom → Test	Test → Hopelessn.	Hopelessn. → Test	Test → Pos. Affect	Test → Neg. Affect	Pos. Affect → Test	Neg. Affect → Test
T1 → T2	-.04*	-.05***	-.11***	-.06***	.03**	-.05***	.01	-.06***
T2 → T3	-.04*	-.05***	-.11***	-.07***	.03**	-.04***	.01	-.06***
T3 → T4	-.04*	-.06***	-.10***	-.07***	.03**	-.04***	.01	-.06***
T4 → T5	-.04*	-.06***	-.11***	-.07***	.03**	-.04***	.01	-.07***

Effects of Covariates at T1	Boredom	Test	Hopelessn.	Test	Pos. Affect	Neg. Affect	Test
Gender	.09**	.13***	-.16***	.13***	.15***	-.13***	.13***
Intelligence	-.01	.56***	-.13***	.56***	-.01	-.15***	.56***
SES	-.02	.12***	-.04	.12***	-.05**	-.03	.12***
Residual Variances							
T1	.99	.62	.96	.62	.98	.96	.62
T2	.59	.30	.66	.30	.34	.40	.30
T3	.57	.31	.61	.31	.33	.36	.31
T4	.54	.30	.59	.30	.32	.34	.30
T5	.53	.30	.59	.30	.32	.33	.30

Note. [a] Range of factor loadings. $p < .001$ for all loadings. [b] Cross-paths between positive and negative affect were not significant (all ps > .05).
* $p < .05$. ** $p < .01$. *** $p < .001$.

Table S6

Fit Indexes of Reciprocal Effects Models for Emotion and Grades:

Subsample of Students who Entered the Study at Grade 5 (N = 2,070)

Model	χ^2	*df*	CFI	TLI	RMSEA	SRMR
Enjoyment	3479.354**	1165	.937	.926	.031	.060
Pride	2319.701**	740	.941	.928	.032	.054
Anger	2384.452**	936	.939	.926	.034	.053
Anxiety	7538.112**	3010	.919	.909	.027	.054
Shame	1922.145**	925	.962	.954	.023	.049
Boredom	1265.447**	550	.970	.962	.025	.043
Hopelessness	1691.283**	580	.957	.948	.030	.061
Positive and negative affect	5086.566**	721	.939	.923	.054	.080

Note. Cross-paths, autoregressive effects, and residual variances invariant across waves.

** $p < .01$.

Table S7

Reciprocal Effects Models for Emotion and Grades: Subsample of Students who Entered the Study at Grade 5 (N = 2070)

	Enjoyment model		Pride model		Anger model		Anxiety model		Shame model	
	Enjoyment	Test	Pride	Test	Anger	Test	Anxiety	Test	Shame	Test
Factor loadings	.35-.83 [a]		.55-.77 [a]		.59-.77 [a]		.43-.77 [a]		.47-.78 [a]	
Autoregressive effects										
T1 → T2	.67***	.59***	.62***	.59***	.58***	.58***	.59***	.58***	.62***	.59***
T2 → T3	.67***	.61***	.65***	.61***	.62***	.60***	.65***	.60***	.61***	.62***
T3 → T4	.67***	.63***	.66***	.63***	.63***	.62***	.67***	.62***	.60***	.64***
T4 → T5	.67***	.62***	.66***	.61***	.63***	.61***	.69***	.61***	.60***	.62***
	Grades → *Enjoyment*	*Enjoyment* *→ Grades*	*Grades →* *Pride*	*Pride* *→ Grades*	*Grades →* *Anger*	*Anger* *→Grades*	*Grades →* *Anxiety*	*Anxiety* *→Grades*	*Grades →* *Shame*	*Shame* *→Grades*
Cross-lagged effects										
T1 → T2	.08***	.09***	.09***	.09***	-.07***	-.09***	-.07***	-.08***	-.06***	-.08***
T2 → T3	.09***	.09***	.09***	.10***	-.07***	-.10***	-.07***	-.10***	-.07***	-.07***
T3 → T4	.09***	.09***	.09***	.10***	-.07***	-.10***	-.07***	-.10***	-.07***	-.07***
T4 → T5	.09***	.09***	.09***	.10***	-.07***	-.11***	-.07***	-.11***	-.07***	-.07***
Effects of Covariates at T1										
Gender	.14***	.01	.17***	.01	-.01	.04	-.15***	.02	-.07*	.01
Intelligence	-.03	.38***	-.02	.38***	-.11**	.39***	-.16***	.38***	-.16***	.38***
SES	-.06**	.08***	-.05*	.08***	-.03	.08**	-.03	.08***	-.03	.08**
Residual Variances										
T1	.98	.84	.97	.84	.99	.83	.95	.84	.97	.84
T2	.51	.58	.57	.58	.64	.59	.61	.58	.58	.58
T3	.51	.56	.54	.56	.60	.56	.54	.56	.59	.56
T4	.52	.57	.53	.57	.58	.58	.51	.57	.59	.57
T5	.52	.57	.52	.56	.57	.57	.50	.56	.60	.56

Table S7 *(continued)*

	Boredom model		Hopelessness model		Positive and negative affect model			
	Boredom	Test	Hopelessn.	Test	Pos. Affect [b]	Neg. Affect [b]	Test	
Factor loadings	.56-.76 [a]		.59-.85 [a]		.76-.98 [a]	.42-.93 [a]		
Autoregressive effects								
T1 → T2	.62***	.61***	.54***	.58***	.81***	.75***	.56***	
T2 → T3	.64***	.62***	.58***	.60***	.80***	.75***	.58***	
T3 → T4	.65***	.64***	.59***	.62***	.80***	.75***	.60***	
T4 → T5	.65***	.63***	.60***	.61***	.79***	.76***	.59***	
	Grades → *Boredom*	*Boredom* *→ Grades*	*Grades →* *Hopelessn.*	*Hopelessn.* *→ Grades*	*Grades →* *Pos. affect*	*Grades →* *Neg. affect*	*Pos. affect* *→ Grades*	*Neg. affect* *→ Grades*
Cross-lagged effects								
T1 → T2	-.05*	-.06***	-.10***	-.09***	.04***	-.03***	.07***	-.08***
T2 → T3	-.06*	-.06***	-.11***	-.10***	.04***	-.04***	.06***	-.08***
T3 → T4	-.06*	-.07***	-.11***	-.10***	.04***	-.04***	.06***	-.08***
T4 → T5	-.05*	-.07***	-.11***	-.10***	.04***	-.05***	.06***	-.08***
Effects of Covariates at T1								
Gender	.09**	.02	-.15***	.02	.17***	-.12***	.02	
Intelligence	.01	.38***	-.12***	.38***	-.03	-.14***	.38***	
SES	-.02	.08***	-.03	.08***	-.06**	-.04	.08***	
Residual Variances								
T1	.99	.84	.96	.84	.97	.96	.84	
T2	.61	.59	.66	.58	.33	.39	.58	
T3	.57	.56	.62	.56	.34	.39	.56	
T4	.55	.57	.60	.57	.36	.39	.58	
T5	.54	.56	.60	.56	.36	.39	.57	

Note. [a] Range of factor loadings. $p < .001$ for all loadings. [b] Cross-paths between positive and negative affect were not significant (all ps > .05).
* $p < .05$. ** $p < .01$. *** $p < .001$.

Table S8

Measurement Equivalence of Emotion Constructs Across School Tracks

Model	Configural Invariance				Metric Invariance				Scalar Invariance				Residual Invariance			
	CFI	TLI	RMSEA	SRMR	CFI	TLI	RMSEA	SRMR	CFI	TLI	RMSEA	SRMR	CFI	TLI	RMSEA	SRMR
Enjoyment	.960	.951	.026	.044	.958	.949	.027	.051	.953	.946	.027	.053	.939	932	.031	.065
Pride	.972	.963	.024	.035	.970	.963	.024	.042	.968	.962	.024	.043	.956	950	.028	.052
Anger	.961	.950	.026	.041	.960	.951	.026	.046	.952	.943	.028	.047	.943	935	.030	.053
Anxiety	.921	.909	.027	.050	.919	.908	.028	.055	.910	.900	.029	.056	.905	895	.029	.057
Shame	.980	.974	.018	.037	.978	.973	.018	.054	.974	.968	.022	.055	.954	947	.026	.066
Boredom	.987	.982	.019	.031	.986	.982	020	.038	.983	.979	.021	.039	.973	967	.026	.048
Hopelessness	.982	.977	.023	.032	.982	978	.022	.037	.979	.976	.023	.038	.964	960	.030	.047
Positive and negative affect	.955	.937	.059	.075	.954	.939	.058	.078	.953	.940	.057	.078	.953	943	.056	.079

Table S9

Multi-Group Reciprocal Effects Models for Emotion and Grades:

Fit Indexes for Invariance across School Tracks

Model	χ^2	*df*	CFI	TLI	RMSEA	SRMR
	Cross-paths, autoregressive effects, and effects of covariates					
	allowed to vary across tracks					
Enjoyment	7556.258**	3575	.928	.916	.031	.063
Pride	4969.021**	2280	.932	.919	.032	.059
Anger	6020.910**	2878	.929	.917	.031	.060
Anxiety	17819.289**	9170	.901	.890	.029	.059
Shame	4791.526**	2845	.952	.944	.024	.057
Boredom	2995.170**	1700	.966	.957	.026	.054
Hopelessness	3833.084**	1790	.950	.941	.032	.063
Positive and negative affect	9845.060**	2243	.941	.929	.055	.080
	Cross-paths, autoregressive effects, and effects of covariates					
	invariant across tracks					
Enjoyment	7798.508**	3663	.925	.915	.031	.065
Pride	5231.097**	2368	.927	.917	.033	.064
Anger	6179.622**	2966	.928	.918	.031	.062
Anxiety	18095.470**	9258	.899	.889	.029	.061
Shame	4981.714**	2933	.950	.942	.025	.060
Boredom	3217.265 **	1788	.962	.955	.026	.059
Hopelessness	4130.255**	1878	.945	.939	.032	.073
Positive and negative affect	10209.853**	2381	.940	.932	.054	.084

Note. The analysis is based on the final reciprocal effects models for emotion and grades (see main text, results section).

** $p < .01$.

Table S10

Multi-Group Reciprocal Effects Models for Emotion and Test Scores:

Fit Indexes for Invariance across School Tracks

Model	χ^2	*df*	CFI	TLI	RMSEA	SRMR
			Cross-paths, autoregressive effects, and effects of covariates allowed to vary across tracks			
Enjoyment	7451.591**	3575	.932	.922	.031	.068
Pride	4880.764**	2280	.938	.926	.032	.068
Anger	5950.733**	2878	.934	.923	.031	.066
Anxiety	17700.078**	9167	.905	.894	.029	.061
Shame	4769.388**	2845	.955	.947	.024	.064
Boredom	3249.428**	1700	.961	.952	.028	.067
Hopelessness	3497.301**	1790	.960	.953	.020	.071
Positive and negative affect	9372.345**	2243	.945	.934	.053	.086
			Cross-paths, autoregressive effects, and effects of covariates invariant across tracks			
Enjoyment	7803.200**	3663	.928	.918	.031	.076
Pride	5238.465**	2368	.931	.922	.033	.081
Anger	6233.918**	2966	.930	.920.	.031	.075
Anxiety	18058.194**	9255	.901	.89	.029	.067
Shame	5068.827**	2933	.950	.953	.025	.075
Boredom	3617.542**	1788	.954	.946	.030	.082
Hopelessness	3858.138**	1878	.954	.948	.030	.089
Positive and negative affect	9856.236**	2381	.943	.935	.052	.099

Note. The analysis is based on the final reciprocal effects models for emotion and test scores

(see main text, results section).

** *p* < .01.

Table S11

Sample Mplus Input Syntax to Demonstrate Use of <TYPE = COMPLEX > Option:

Confirmatory Factor Analysis for Enjoyment

```
TITLE: ENJOYMENT CFA
!Specification of data file to be used for the analysis
DATA: FILE IS "PALMA Crosslagged_08.08.13.dat";
!List of all variables contained in the dataset
VARIABLE: NAMES ARE
 vpnr school fges_1 fges_2 fges_3 fges_4 fges_5 fges_6
 gma_jz4 gma_jz5 gma_jz6 gma_jz7 gma_jz8 gma_jz9 gma_zz10
 jo_1 pr_1 ax_1 ag_1 hl_1 bo_1 sh_1 flow_1 jo_2 pr_2 ax_2
 ag_2 hl_2 bo_2 sh_2 flow_2 jo_3 pr_3 ax_3 ag_3 hl_3 bo_3
 sh_3 flow_3 jo_4 pr_4 ax_4 ag_4 hl_4 bo_4 sh_4 flow_4
 jo_5 pr_5 ax_5 ag_5 hl_5 bo_5 sh_5 flow_5 jo_6 pr_6 ax_6
 ag_6 hl_6 bo_6 sh_6 flow_6 clnr_6 clnr_1 clnr_2
 agemon ageyear sex
 sctyp_1 sctyp_2 sctyp_3 sctyp_4 sctyp_5 ag1_1 ag3_1
 ag2_1 ag4_1 ag7_1 ag8_1 ag5_1 ag6_1 ax1_1 ax2_1
 ax4_1 ax3_1 ax12_1 ax13_1 ax14_1 ax15_1 ax5_1
 ax6_1 ax7_1 ax8_1 ax9_1 ax10_1 ax11_1 bo1_1 bo2_1
 bo3_1 bo4_1 bo5_1 bo6_1 hl1_1 hl2_1 hl3_1 hl4_1
 hl5_1 hl6_1 jo1_1 jo2_1 jo3_1 joengp_1 jogerp_1
 jo7_1 jo8_1 jo9_1 jo4_1 jo5_1 jo6_1 pr1_1 pr2_1
 pr6_1 pr7_1 pr8_1 pr3_1 pr4_1 pr5_1 sh1_1 sh2_1
 sh7_1 sh8_1 sh3_1 sh4_1 sh5_1 sh6_1 kftviq_1
 kftniq_1 kft_iq_1 jo1_2 ax1_2 ax3_2 ax4_2 jo2_2
 bo2_2 ax2_2 ag1_2 sh2_2 bo1_2 jo3_2 ag2_2 bo3_2
 ag3_2 sh1_2 ag4_2 pr1_2 pr2_2 ax5_2 jo6_2 hl1_2
 ax7_2 hl3_2 ax10_2 hl4_2 ax9_2 jo4_2 ax6_2 ag5_2
 hl2_2 sh4_2 ax11_2 hl5_2 ag6_2 sh5_2 jo5_2 ax8_2
 hl6_2 sh6_2 pr3_2 pr4_2 sh3_2 pr5_2 bo4_2 ax14_2
 jo7_2 ax15_2 ag7_2 bo6_2 ax12_2 sh8_2 jo8_2 ax13_2
 bo5_2 pr8_2 ag8_2 jo9_2 pr6_2 sh7_2 pr7_2 kftviq_2
 kftniq_2 kftiq_2 clnr_3 kftniq_3 kftviq_3 jo1_3 ax1_3
 ax3_3 ax4_3 jo2_3 bo2_3 ax2_3 ag1_3 sh2_3 bo1_3
 jo3_3 ag2_3 bo3_3 ag3_3 sh1_3 ag4_3 pr1_3
 pr2_3 ax5_3 jo6_3 hl1_3 ax7_3 hl3_3 ax10_3
 hl4_3 ax9_3 jo4_3 ax6_3 ag5_3 hl2_3 sh4_3
 ax11_3 hl5_3 ag6_3 sh5_3 jo5_3 ax8_3 hl6_3
 sh6_3 pr3_3 pr4_3 sh3_3 pr5_3 bo4_3 ax14_3
 jo7_3 gma_zz7 ax15_3 ag7_3 bo6_3 ax12_3
 sh8_3 jo8_3 ax13_3 bo5_3 pr8_3 ag8_3 jo9_3
 pr6_3 sh7_3 pr7_3 kftiq_3 joc_1 jot_1 jol_1 prc_1
 prt_1 prl_1 axc_1 axt_1 axl_1 agc_1 agt_1 agl_1
 boc_1 bol_1 shc_1 sht_1 shl_1 joc_2 jot_2 jol_2
 prc_2 prt_2 prl_2 axc_2 axt_2 axl_2 agc_2 agt_2
 agl_2 boc_2 bol_2 shc_2 sht_2 shl_2 joc_3 jot_3
 jol_3 prc_3 prt_3 prl_3 axc_3 axt_3 axl_3 agc_3
```

```
 agt_3 agl_3 boc_3 bol_3 shc_3 sht_3 shl_3 clnr_4
 jo1_4 ax1_4 ax3_4 ax4_4 jo2_4 bo2_4 ax2_4 ag1_4
 sh2_4 bo1_4 jo3_4 ag2_4 bo3_4 ag3_4 sh1_4 ag4_4
 mbunt1_4 mbueb2_4 mbueb1_4 mbunt2_4 pr1_4
 pr2_4 ax5_4 jo6_4 hl1_4 ax7_4 hl3_4 ax10_4 hl4_4
 ax9_4 jo4_4 ax6_4 ag5_4 hl2_4 sh4_4 ax11_4 hl5_4
 ag6_4 sh5_4 jo5_4 ax8_4 hl6_4 sh6_4 pr3_4 pr4_4
 sh3_4 pr5_4 bo4_4 ax14_4 jo7_4 ax15_4 ag7_4
 bo6_4 ax12_4 sh8_4 jo8_4 ax13_4 bo5_4 pr8_4
 ag8_4 jo9_4 pr6_4 sh7_4 pr7_4 joc_4 jot_4 jol_4
 prc_4 prt_4 prl_4 axc_4 axt_4 axl_4 agc_4 agt_4
 agl_4 boc_4 bol_4 shc_4 sht_4 shl_4 kftniq_4 kftviq_4
 kftiq_4 laeng12345 clnr_5 kftniq_5 kftviq_5 kftiq_5
 jo1_5 ax1_5 ax3_5 ax4_5 jo2_5 bo2_5 ax2_5 ag1_5
 sh2_5 bo1_5 jo3_5 ag2_5 bo3_5 ag3_5 sh1_5 ag4_5
 mbunt1_5 mbueb2_5 mbueb1_5 mbunt2_5 pr1_5
 pr2_5 ax5_5 jo6_5 hl1_5 ax7_5 hl3_5 ax10_5 hl4_5
 ax9_5 jo4_5 ax6_5 ag5_5 hl2_5 sh4_5 ax11_5 hl5_5
 ag6_5 sh5_5 jo5_5 ax8_5 hl6_5 sh6_5 pr3_5 pr4_5
 sh3_5 pr5_5 bo4_5 ax14_5 jo7_5 ax15_5 ag7_5
 bo6_5 ax12_5 sh8_5 jo8_5 ax13_5 bo5_5 pr8_5
 ag8_5 jo9_5 pr6_5 sh7_5 pr7_5 joc_5 jot_5 jol_5
 prc_5 prt_5 prl_5 axc_5 axt_5 axl_5 agc_5 agt_5
 agl_5 boc_5 bol_5 mbueb_5 mbunt_5 shc_5 sht_5
 shl_5 sctyp_6 jo1_6 ax1_6 ax3_6 ax4_6 jo2_6
 bo2_6 ax2_6 ag1_6 sh2_6 bo1_6 jo3_6 ag2_6
 bo3_6 ag3_6 sh1_6 ag4_6 mbunt1_6 mbueb2_6
 mbueb1_6 mbunt2_6 pr1_6 pr2_6 ax5_6 jo6_6
 hl1_6 ax7_6 hl3_6 ax10_6 hl4_6 ax9_6 jo4_6 ax6_6
 ag5_6 hl2_6 sh4_6 ax11_6 hl5_6 ag6_6 sh5_6 jo5_6
 ax8_6 hl6_6 sh6_6 pr3_6 pr4_6 sh3_6 pr5_6 bo4_6
 ax14_6 jo7_6 ax15_6 ag7_6 bo6_6 ax12_6 sh8_6
 jo8_6 ax13_6 bo5_6 pr8_6 ag8_6 jo9_6 pr6_6 sh7_6
 pr7_6 joc_6 jot_6 jol_6 prc_6 prt_6 prl_6 axc_6 axt_6
 axl_6 agc_6 agt_6 agl_6 boc_6 bol_6 mbueb_6
 mbunt_6 shc_6 sht_6 shl_6 kftniq_6 kftviq_6 kftiq_6
 egp6f_ges egp6m_ges egp6_ges egp11f_ges egp11m_ges;
!Definition of cluster variable to account for nestedness of students within schools
 CLUSTER = SCHOOL;
!Variables used in the CFA: Jo1_1=Joy Item 1 at Wave 1 to Jo1_5=Joy Item 5 at Wave 5_
 USEVARIABLES ARE
 jo1_1 jo2_1 jo3_1 jo4_1 jo5_1 jo6_1 jo7_1 jo8_1 jo9_1
 jo1_2 jo2_2 jo3_2 jo4_2 jo5_2 jo6_2 jo7_2 jo8_2 jo9_2
 jo1_3 jo2_3 jo3_3 jo4_3 jo5_3 jo6_3 jo7_3 jo8_3 jo9_3
 jo1_4 jo2_4 jo3_4 jo4_4 jo5_4 jo6_4 jo7_4 jo8_4 jo9_4
 jo1_5 jo2_5 jo3_5 jo4_5 jo5_5 jo6_5 jo7_5 jo8_5 jo9_5;
!Definition of missing values for all variables in the dataset
MISSING ARE ALL (-99);
!Command to consider nestedness by using the Mplus complex design
ANALYSIS: TYPE = COMPLEX;
MODEL:
```

!Measurement model defining latent variables enjoy_1 (enjoyment Wave 1) to enjoy_5 (enjoyment Wave 5) by items as manifest indicators
 enjoy_1 by jo1_1 jo2_1 jo3_1 jo4_1 jo5_1 jo6_1 jo7_1 jo8_1 jo9_1;
 enjoy_2 by jo1_2 jo2_2 jo3_2 jo4_2 jo5_2 jo6_2 jo7_2 jo8_2 jo9_2;
 enjoy_3 by jo1_3 jo2_3 jo3_3 jo4_3 jo5_3 jo6_3 jo7_3 jo8_3 jo9_3;
 enjoy_4 by jo1_4 jo2_4 jo3_4 jo4_4 jo5_4 jo6_4 jo7_4 jo8_4 jo9_4;
 enjoy_5 by jo1_5 jo2_5 jo3_5 jo4_5 jo5_5 jo6_5 jo7_5 jo8_5 jo9_5;
!Correlated uniquenesses within waves for items measuring class-related enjoyment
 jo1_1-jo3_1 with jo1_1-jo3_1;
 jo1_2-jo3_2 with jo1_2-jo3_2;
 jo1_3-jo3_3 with jo1_3-jo3_3;
 jo1_4-jo3_4 with jo1_4-jo3_4;
 jo1_5-jo3_5 with jo1_5-jo3_5;
!Correlated uniquenesses within waves for items measuring test-related enjoyment
 jo4_1-jo6_1 with jo4_1-jo6_1;
 jo4_2-jo6_2 with jo4_2-jo6_2;
 jo4_3-jo6_3 with jo4_3-jo6_3;
 jo4_4-jo6_4 with jo4_4-jo6_4;
 jo4_5-jo6_5 with jo4_5-jo6_5;
!Correlated uniquenesses within waves for items measuring learning-related enjoyment
 jo7_1-jo9_1 with jo7_1-jo9_1;
 jo7_2-jo9_2 with jo7_2-jo9_2;
 jo7_3-jo9_3 with jo7_3-jo9_3;
 jo7_4-jo9_4 with jo7_4-jo9_4;
 jo7_5-jo9_5 with jo7_5-jo9_5;
!Correlated uniquenesses of identical items across waves
 jo1_1-jo9_1 pwith jo1_2-jo9_2;
 jo1_1-jo9_1 pwith jo1_3-jo9_3;
 jo1_1-jo9_1 pwith jo1_4-jo9_4;
 jo1_1-jo9_1 pwith jo1_5-jo9_5;
 jo1_2-jo9_2 pwith jo1_3-jo9_3;
 jo1_2-jo9_2 pwith jo1_4-jo9_4;
 jo1_2-jo9_2 pwith jo1_5-jo9_5;
 jo1_3-jo9_3 pwith jo1_4-jo9_4;
 jo1_3-jo9_3 pwith jo1_5-jo9_5;
 jo1_4-jo9_4 pwith jo1_5-jo9_5;
!Request to provide standardized STDYX solution in addition to default unstandardized solution
 OUTPUT: STDYX;