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OMIP contribution to CMIP6: experimental and diagnostic protocol for the physical component of the Ocean Model Intercomparison Project


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Abstract. The Ocean Model Intercomparison Project (OMIP) is an endorsed project in the Coupled Model Intercomparison Project Phase 6 (CMIP6). OMIP addresses CMIP6 science questions, investigating the origins and consequences of systematic model biases. It does so by providing a framework for evaluating (including assessment of systematic biases), understanding, and improving ocean, sea-ice, tracer, and biogeochemical components of climate and earth system models contributing to CMIP6. Among the WCRP Grand Challenges in climate science (GCs), OMIP primarily contributes to the regional sea level change and near-term (climate/decadal) prediction GCs.

OMIP addresses the above aims in two complementary ways.

1. OMIP as an experimental MIP: OMIP provides an experimental protocol for global ocean/sea-ice simulations forced with common atmospheric data sets. OMIP ocean/sea-ice simulations include physical, inert chemical, and interactive biogeochemical components, thus bringing together a broad community of ocean and climate scientists making use of global ocean/sea-ice models. OMIP offers an opportunity for contributions from a wide number of groups capable of running and analysing global ocean/sea-ice models. For the physical portion of OMIP, there is one Tier 1 experiment described in this paper. The biogeochemical portion offers an additional Tier 2 experiment (Orr et al., 2016).

2. OMIP as a diagnostics MIP: OMIP provides a diagnostics protocol to coordinate and rationalize ocean diagnostics for CMIP6 simulations that include an ocean component, including the following.

- a. CMIP6 DECK (Diagnostic, Evaluation and Characterization of Klima) experiments, including piControl, abrupt4xCO2, 1pctCO2, as well as the historical simulations (Eyring et al., 2016)
- b. FAFMIP (Flux Anomaly Forced MIP) (Gregory et al., 2016)
- c. C4MIP (Coupled Carbon Cycle Climate MIP) (Jones et al., 2016)
- d. DAMIP (Detection and Attribution MIP) (Gillett and Shiogama, 2016)
- e. DCPP (Decadal Climate Prediction Project) (Boer et al., 2016)
- f. ScenarioMIP (Scenario MIP) (O’Neill et al., 2016)
- g. HighResMIP (High Resolution Model Intercomparison Project) (Haarsma et al., 2016)
- h. OMIP ocean/sea-ice simulations (this paper and Orr et al., 2016).

In this paper, we detail the physical portion of OMIP, including the experimental protocol and diagnostics protocol. The chemical and biogeochemical portions of OMIP are detailed in the companion paper by Orr et al. (2016).

1.1 A mandate based on enhanced observational and modelling capabilities

Observational oceanography continues to experience a growth in measurement capability that supports critical insights into the changing earth climate system. For in situ
measurements, this growth largely results from the Argo Program (Riser et al., 2016). Since 2005, Argo has revolutionized physical oceanography by providing comprehensive temperature and salinity profiles for the upper 2000 m with near-global coverage. Most centrally for studies of the earth’s climate, Argo has enabled revised assessments of ocean heat content (e.g. Roemmich et al., 2012, 2015; von Schuckmann et al., 2016), documenting the ongoing and unabated ocean warming. These measurements also point to persistent salinity changes (e.g. Hosoda et al., 2009; Durack and Wijffels, 2010; Helm et al., 2010; Skliris et al., 2014), hypothesized to result from water cycle amplification (Stott et al., 2008; Durack et al., 2012; Pierce et al., 2012; Terray et al., 2012). Measurements furthermore suggest that the Southern Hemisphere is responsible for 67–98% of the global ocean heating during 2006 to 2013 (Roemmich et al., 2015).

Additional deep ocean measurements and analysis (e.g. Purkey and Johnson, 2010, 2012, 2013; Kouketsu et al., 2011) suggest further changes in the global energy budget as well as ongoing sustained contributions to sea level rise. Satellite altimetry measurements of sea level have also revolutionized our understanding of the changing ocean climate, in particular regional patterns of sea level change (e.g. Fu and Haines, 2013; Ablain et al., 2015). Further augmentations by space-borne ocean observations include ocean salinity, thanks to the SMOS (Berger et al., 2002), Aquarius (Lagerloef et al., 2008), and SMAP (Piepmeier et al., 2015) satellites, which complement the longer-standing ocean surface temperature measurements.

Global ocean/sea-ice and climate models are powerful tools to help mechanistically interpret ocean measurements, and in some cases to identify key limitations of the measurements (Durack et al., 2014a; Wunsch, 2016). Conversely, ocean measurements, particularly those maintained over many decades, offer the means to assess simulation fidelity. As noted by Durack et al. (2016), we cannot presume measurements will continue indefinitely. It is therefore critical that we further the relationship between modelling and observations, as doing so supports both. A grounding in ocean and climate science, in the midst of enhanced capabilities in observations, modelling, and synthesis (e.g. Wunsch and Heimbach, 2013), enables the Ocean Model Intercomparison Project.

1.2 Uses of global ocean/sea-ice models

Although the bulk of CMIP6 involves coupled climate and earth system models, it is useful to complement these more comprehensive modelling systems with a hierarchy of model configurations aiming to uncover mechanisms and understand biases. Global ocean/sea-ice models provide a tool for doing so, in a manner motivated by similar efforts in other climate components, particularly the Atmosphere Model Intercomparison Project (AMIP) (Gates, 1993). OMIP experiments and diagnostics provide a framework for the following types of research studies.

1. To investigate oceanic physical, chemical, and biogeochemical mechanisms that drive seasonal, interannual, and decadal variability;
2. To assess and understand biases in the ocean/sea-ice component of coupled climate models;
3. To attribute ocean climate variations to boundary forced (including volcanoes) versus internal to the climate system (without volcanoes);
4. To evaluate robustness of mechanisms across models and forcing data sets;
5. To bridge observations and modelling by providing a complement to ocean reanalysis from data assimilation (Karspeck et al., 2015; Stammer et al., 2016);
6. To provide consistent ocean and sea-ice states useful for initialization of decadal predictions (Taylor et al., 2012; Yeager et al., 2012).

Further specific examples of recent global ocean/sea-ice studies are noted in Sect. 2 where we discuss the Coordinated Ocean-ice Reference Experiments (CORE), the predecessor to OMIP.

1.3 Content of this paper

We start the main portion of this paper in Sect. 2 by defining the OMIP experimental protocol for the physical components of ocean/sea-ice simulations. We introduce OMIP as a diagnostics MIP in Sect. 3, reserving the bulk of that discussion for appendices. We then close the main portion of the paper with a brief summary in Sect. 4.

Various appendices specify the OMIP diagnostics protocol. In Appendix A we provide an overview of OMIP as a diagnostics MIP, and summarize many of the related issues. In Appendix B we detail grid cell volume and area; in Appendix C we discuss spatial sampling; in Appendix D we summarize elements of seawater thermodynamics of relevance for sampling the temperature and salinity fields; in Appendix E we show that the evolution of ocean heat content is invariant when changing temperature scales; and in Appendix F we summarize elements of a finite volume formulation of the tracer equation.

The remaining appendices detail the various diagnostics. In Appendix G we describe the static fields and functions to define the particular ocean model configuration. In Appendix H we provide details for the scalar fields such as tracers, and in Appendix I we discuss the requested components of vector fields such as velocity and transport. In Appendix J we describe the requested mass transports through a suite of pre-defined straits and throughflows. We describe the requested boundary fluxes of mass, heat, salt, and momentum...
in Appendix K. In Appendix L we formulate the diagnostics for examining three-dimensional heat and salt budgets. Finally, in Appendices M and N we detail the requests for vertical and lateral subgrid-scale parameters.

2 OMIP as a global ocean/sea-ice MIP

The physical component of the OMIP experiment follows the protocol of the Coordinated Ocean-ice Reference Experiments (CORE) (Griffies et al., 2009b, 2012; Danabasoglu et al., 2014) interannually varying experiment (CORE-II). This OMIP experiment represents a CMIP6 Tier 1 experiment (the biogeochemical portion of OMIP offers an additional Tier 2 experiment detailed in Orr et al., 2016). The interannual CORE-II experimental protocol shares much with the Normal Year Forcing (NYF) protocol of CORE-I (Griffies et al., 2009b), with CORE-I making use of an idealized repeating annual cycle rather than the interannual variations of CORE-II. The interannual variations allow CORE-II simulations to be directly compared to observation-based measures, especially on interannual to decadal timescales.

The CORE-II experiment (and by extension, the OMIP/Version1 experiment described here) forces physical ocean fields through use of the interannually varying atmospheric state of Large and Yeager (2009), along with river runoff data based on modifications of Dai and Trenberth (2002) and Dai et al. (2009). The forcing data set covers the 62-year period from 1948 to 2009, and it is collaboratively supported by the U.S. National Center for Atmospheric Research (NCAR) and the NOAA Geophysical Fluid Dynamics Laboratory (NOAA/GFDL). All data sets, codes for the bulk flux formulae, technical reports, and other support codes along with the release notes are available at the CLIVAR Ocean Model Development Panel (OMDP) webpage http://www.clivar.org/omdp/core.

Importantly, groups should make use of the “corrected” forcing data set available from the website, since these files incorporate modifications from Large and Yeager (2009) aiming to address biases in the reanalysis product. The “uncorrected” data that are also available represent the raw fields without the Large and Yeager (2009) modifications. These raw fields should be used only for those who have coded the Large and Yeager (2009) modifications directly into their flux coupler.

Within the CMIP6 lexicon of experiment names, the identification for the OMIP/Version1 experiment is

experiment_id = omipl1.

Preliminary plans for OMIP/Version2 are mentioned in Sect. 2.4.

2.1 CORE-II analysis papers

A broad community of scientists have provided a thorough analysis for an ensemble of 13 to 20 CORE-II simulations making use of CMIP5-class ocean/sea-ice models. This work has been documented in the following research papers.

1. Danabasoglu et al. (2014): North Atlantic mean
2. Griffies et al. (2014): Global and regional sea level
5. Danabasoglu et al. (2016): North Atlantic variability
6. Wang et al. (2016a): Arctic sea ice and solid freshwater
7. Wang et al. (2016b): Arctic liquid freshwater
8. Ilicak et al. (2016): Arctic hydrography

These papers help to define the state-of-the-science in forced global ocean/sea-ice simulations. They furthermore identify model diagnostics and metrics useful for evaluating the ocean component of all CMIP6 simulations.

Scientific and practical limitations of forced global ocean/sea-ice simulations are important to acknowledge (e.g. Sect. 3 of Griffies et al., 2009b), though such models have their advantages, particularly in their ability to help interpret the observational record. In general, the utility of forced global ocean/sea-ice models depends on the scientific questions to be addressed. The above papers detail their limitations and exemplify their scientific value across a broad suite of processes and ocean basins. By extension, these studies provide a compelling case for both the limitations and potentials for OMIP simulations included as part of CMIP6.

2.2 OMIP/CORE-II experimental protocol

The experimental protocol for the physical component of OMIP is detailed in Griffies et al. (2009b), Griffies et al. (2012), and Danabasoglu et al. (2014), with a summary provided here.

– Initialization
Forcing

- Potential temperature and practical salinity are initialized in the upper 1500 m using January observational-based climatology from version 2 of Locarnini et al. (2013) for temperature and Zweng et al. (2013) for salinity. We refer to these data as WOA13v2. The January fields from WOA13v2 stop at 1500 m. We filled deeper depths with the mean from January/February/March (winter in the north and summer in the south). Initial conditions are provided at the OMIP website, with both 1° and 1/4° versions. Interpolation should be made to the respective model grid. Conversion to Conservative Meridional Circulation (e.g., sections of Wang et al. (2016b)).

- Velocity starts from a state of rest, i.e., all three velocity components start with zero values.

- Sea-ice fields are generally initialized from an existing state taken from another simulation, set to the January mean state from that simulation.

- There is no recommended protocol for solid land-ice calving. Iceberg models are generally disabled in OMIP experiments, though some groups are exploring their use for future OMIP protocols.

2.3 Comments on surface salinity restoring

The real climate system has no direct feedback between sea surface salinity (SSS) and surface water fluxes (see Durack et al., 2013, for further discussion). Correspondingly, there is no direct feedback in coupled climate models. However, there is a need to introduce a feedback via a surface salinity restoring boundary condition in OMIP. The reason is that in the absence of some form of restoring, global ocean/sea-ice models typically drift over decadal timescales. Such drift can reduce the physical utility of the simulations, particularly for studies of the high-latitude circulation in the Atlantic and Southern oceans. The key reason for salinity restoring relates to high-latitude thermohaline and ocean/sea-ice processes that impact on the meridional overturning circulation (see Sect. 3 of Griffies et al., 2009b, as well as Behrens et al., 2013).

Details of the salinity restoring appropriate to reduce thermohaline drift are sensitive to model details and the prescribed precipitation and river runoff data. Consequently, a single salinity restoring boundary condition for all models (i.e., a common piston velocity) has proven elusive. Example settings for a suite of CORE-II simulations can be found in Table 2 of Danabasoglu et al. (2014), including whether there is any restoring under sea ice and/or normalization of the restoring flux over the globe. A full examination of model sensitivity to the salinity restoring has not been published. However, specific models are examined in Sect. 16 of Griffies et al. (2009b), Appendix C of Danabasoglu et al. (2014), and Appendix B of Wang et al. (2016b).

There is no proven correlation between model physical integrity, from a process perspective, and the strength of the salinity boundary condition required to stabilize the simulated overturning circulation. Claims that a “perfect” ocean/sea-ice model should be able to make use of zero surface salinity restoring ignore the many uncertainties in the prescribed precipitation and river runoff. More fundamentally, such claims ignore the otherwise undamped thermohaline feedbacks that emerge in the absence of an interactive atmosphere model that responds to changes in the ocean and sea-ice state. Salinity restoring is thus a stop-gap measure aimed at reducing runaway feedbacks that can arise in the global ocean/sea-ice models run with a prescribed atmospheric state.
It remains an ongoing research task to examine suitable salinity boundary conditions for global ocean/sea-ice models. Consequently, we do not offer protocol specifications. Rather, we recommend that modellers consult Appendix C in Danabasoglu et al. (2014) to see what has worked for other models. Choosing a weak salinity restoring is generally preferred to reduce the impact on variability.

2.4 Plans for OMIP/Version2

The present document focuses on Version 1 of OMIP, which is a straightforward extension of the CORE-II project making use of the Large and Yeager (2009) atmospheric state. This experiment has the CMIP6 experiment identification experiment_id = omip1. In addition, there is ongoing research coordinated through the CLIVAR Ocean Model Development Panel (OMDP) to develop a Phase 2 experiment for OMIP. The OMIP/Version2 experiment has the following CMIP6 identification:

experiment_id = omip2.

This experiment will use an atmospheric state and runoff data set based on the JRA-55 reanalysis (Kobayashi et al., 2015). JRA-55 has a finer spatial resolution, starts at year 1958, and remains updated to recent months. More details will be released when available.

3 OMIP as a diagnostics MIP

The diagnostic portion of OMIP coordinates ocean diagnostics for CMIP6 experiments involving an ocean component. The diagnostic suite is an updated and revised version of the CMIP5 ocean diagnostics detailed in Griffies et al. (2009a). We here outline some of the elements of ocean analysis. In the appendices, we provide a scientific rationale and details for each of the ocean diagnostics. These diagnostics are coordinated with the CMIP6 data request organized by the WGCM Infrastructure Panel (Martin Juckes, personal communication, 2016). We also detail the protocol for sampling the physical ocean fields used to create the diagnostics. Orr et al. (2016) focus on the chemical and biogeochemical tracers. Diagnostics for the sea-ice component are coordinated by the CMIP6 Sea-ice Model Intercomparison Project (SIMIP) (Notz et al., 2016).

3.1 The general needs of analysis

Comparative ocean analysis involves computing differences between two realizations of a particular diagnostic. One can then compute statistics, such as the mean square difference, thus rendering quantitative measures of the distance between model realizations (model–model comparisons), or between a model realization and an observation-based realization. Such metric-based analyses are the dominant means for quantifying accuracy of CMIP simulations.

In addition to metric-based analysis, analysts sometimes aspire for more complex analysis, such as the examination of terms in a tracer budget (e.g. Appendix L). There may not be an observational estimate of such terms, thus precluding the computation of a model–observation metric. Nonetheless, comparing budget terms across models offers insight into mechanisms acting in the models. Such budget analyses generally must be based on diagnostics computed online during the model integration and using the model native grid. Offline estimates are generally less accurate, as such terms generally involve products of time-dependent fields. Reasons for the loss of accuracy concern missing temporal correlations and/or offline numerical methods that only approximate online numerics.

In designing the diagnostics protocol, we kept in mind the needs of both metric-based analysis and budget-based analysis. We hope that the protocol proves suitable for the diverse needs of those analysing CMIP6 output.

3.2 Sponsors for diagnostics and plans for analysis

Our recommended suite of OMIP diagnostics reflect the needs and interests of numerous analysts, including the authors of this document and their extended network of collaborators. The recommendations generally resulted from surveys and discussions within the ocean and climate community, with particular feedback from the CMIP5 process. Furthermore, the list reflects our judgement regarding what diagnostics can be useful for scientifically assessing the simulations, and for providing mechanistic understanding of various physical processes. Archiving these diagnostics will greatly enhance the value of the many CMIP6 simulations, and offer opportunities for both planned (e.g. assessments) and unplanned (e.g. PhD theses) research, thus advancing the science of ocean and climate modelling.

It is tempting to ask for an extensive suite of diagnostics that allow for complete process-based examination of the simulations. Nonetheless, any diagnostic request must confront the reality of finite archive space and limited human resources. Furthermore, CMIP6 diagnostics should have a sponsor, such as a WCRP science panel or a CMIP6 MIP. Sponsors are expected to lead in the coordination of analyses that result in peer-review publications. Note, however, that diagnostics are in no way owned by the sponsor, as the CMIP6 archive is open to anyone. It is with this background in mind that we aimed to be true to the needs of analysts who will mine the CMIP6/OMIP model data. We also aimed to design a diagnostic suite attractive to process physicists who wish to look “under the hood” of the models.

Various CMIP6 sanctioned MIPs have directly sponsored ocean diagnostics listed in this document. These MIPs re-
quire OMIP diagnostics for many facets of their research aims.

1. CMIP6 DECK (Diagnostic, Evaluation and Characterization of Klima experiments) includes experiments piControl, abrupt4xCO2, and 1pctCO2 (Eyring et al., 2016). Additionally, as part of the entry card into CMIP6 MIPs, groups will run a historical simulation. The ocean plays a central role in each of these experiments, in which case it is important to archive OMIP diagnostics.

2. OMIP, as represented by the authors of this document, is the sponsor for the bulk of the diagnostics requested here. These diagnostics serve many needs of CMIP6 related to ocean climate science, including an assessment and understanding of model biases. Among the WCRP Grand Challenges in climate science (GCs), OMIP primarily contributes to the regional sea level change and near-term (climate/decadal) prediction GCs. Studies planned with the OMIP diagnostics include mechanisms for changes in global and regional sea level, including heat content changes; elements of how subgrid-scale parameterizations affect simulation integrity; the ability of climate models to represent the observed state of the ocean during the 20th and 21st centuries; mechanisms for model biases, and more.

3. FAFMIP (Flux-Anomaly-Forced Model Intercomparison Project) (Gregory et al., 2016) supports the WCRP Grand Challenge on sea level change and regional impacts, with particular interest in identifying mechanisms for regional sea level variations/projections. Critical needs for this MIP include budget terms for heat and salt summarized by Table L1. These terms will help to understand mechanisms for the large spread in ocean heat uptake efficiency found in CMIP5 simulations (Kuhlbrodt and Gregory, 2012), which in turn impact on the spread in projected sea level rise (Slangen et al., 2012; Church et al., 2013b; Hallberg et al., 2013; Slangen et al., 2014; Melet and Meyssignac, 2015).

4. C4MIP (Coupled Climate Carbon Cycle Model Intercomparison Project) (Jones et al., 2016) aims to improve and accelerate development of global-scale, three-dimensional, coupled earth system models that include the carbon cycle and related biogeochemical and ecosystem components. C4MIP is a co-sponsor of chemical and biogeochemical tracers discussed in Orr et al. (2016).

5. HighResMIP (High Resolution Model Intercomparison Project) (Haarsma et al., 2016) aims to assess the robustness of improvements in the representation of important climate processes with “weather-resolving” global model resolutions (roughly 25 km or finer), within a simplified framework using the physical climate system with constrained aerosol forcing.

6. DCPP (Decadal Climate Prediction Project) (Boer et al., 2016) is a WCRP project and a CMIP6 MIP that aims to improve and accelerate development of global climate prediction systems on annual, multi-annual, and decadal timescales.

The following communities have provided input to the OMIP diagnostics and have a direct interest in analysing these diagnostics for peer-review studies.

1. GSOP (Global Synthesis and Observational Panel) is a CLIVAR panel that has encouraged analysis of various physical processes, such as those proposed by FAFMIP in support of understanding the role of physical processes in heat and salt budgets (Table L1).

2. The AMOC (Atlantic Meridional Overturning Circulation) community, as represented by the U.S. CLIVAR AMOC Science Team, has emphasized the needs for diagnostics measuring the mass, heat, and salt transport in the Atlantic. The budget terms in Table L1 will also be of prime interest for regional AMOC and Arctic analysis, with particular use for diagnosing the role of ocean processes impacting the AMOC (Roberts et al., 2013, 2014).

3. Southern Ocean. The Southern Ocean community, as represented by members of the CLIVAR/CliC/SCAR Southern Ocean Region Panel, has a particular interest in the detailed workings of mesoscale eddy parameterizations, particularly as they impact on vertical heat transport (e.g. Gregory, 2000), and the response of the Antarctic Circumpolar Current (ACC) and Southern Ocean meridional overturning circulation (MOC) to changes in surface forcing (e.g. Downes and Hogg, 2013; Downes et al., 2015; Farneti et al., 2015).

4. Ecosystem Community. Certain physical fields are of direct use for assessing the impacts of physical climate on ecosystems (Stock et al., 2010). Bottom temperature and salinity fields are of particular interest (Sects. H16 and H21).

5. Ocean mixing community: focusing on ocean subgrid-scale processes, the mixing community is served by documenting model parameterizations. In CMIP5, there were numerous fields requested to serve this community. Unfortunately, few model submissions were made, thus leading to little published analysis of these fields.3

3Downes and Hogg (2013) characterize the Southern Ocean in CMIP5 simulations in terms of the ocean mesoscale eddy parameterizations. Unfortunately, few models submitted the relevant eddy diffusivities and overturning streamfunctions.
For CMIP6, we recommend a subset of the CMIP5 diagnostics in hopes that more model groups will submit the reduced number of fields, thus better serving the needs of subgrid-scale parameterization studies.

3.3 Diagnostics for ocean spin-up

The deep ocean is ventilated on multi-centennial timescales (Sen Gupta and England, 2004; Stouffer, 2004) which can lead to drifts in many ocean properties on long timescales (Banks et al., 2007). Drift needs to be taken into account when analysing ocean diagnostics from CMIP6.

Five cycles of OMIP atmospheric forcing are insufficient to reach full equilibration of the full ocean (Danabasoglu et al., 2014, and Griffies et al., 2014). Nonetheless, model-to-model comparison is meaningful when sampled at the same point after initialization, whether that be in the first or fifth forcing cycle. That is, model comparison is meaningful since all OMIP ocean/sea-ice models are integrated for the same time starting from the same initial conditions (see the simulation length discussed in Sect. 2.2).

In contrast, many of the other CMIP6/MIPs are run relative to the CMIP DECK piControl experiment. The piControl experiment is itself initialized from piControl spin-up, which has an unspecified length (Eyring et al., 2016). The spin-up length determines the residual drift in ocean properties from ocean temperature and salinity (Pardaens et al., 2003) to biogeochemistry (Séférian et al., 2015), with shorter spin-up generally exhibiting larger drifts.

The CMIP6 DECK experiments (piControl, abrupt4xCO2, 1pctCO2), historical simulation, FAFMIP, C4MIP, and ScenarioMIP are all concerned with the ocean response to forcing. In these cases, the underlying climate drift from piControl should be subtracted from the response. If absolute quantities are required for analysis, it is recommended that the underlying climate drift in piControl be analysed and the length and details of the spin-up in piControl spin-up be considered. To help with this analysis of spin-up, we recommend that all Priority = 1 diagnostics in Tables H1, I1, K1, K2, and K3 be saved as decadal time means at decadal intervals.

4 Summary and closing comments

OMIP has two components: an experimental protocol and a diagnostics protocol. The experimental protocol, detailed in Sect. 2, follows from the interannual Coordinated Ocean-ice Reference Experiments (CORE-II) (Sect. 2.1). The Large and Yeager (2009) atmospheric state used for CORE-II is used here for OMIP/Version1. Additionally, we are in the process of developing OMIP/Version2 that aims to overcome some limitations of the Large and Yeager (2009) state, with OMIP/Version2 making use of the JRA-55 reanalysis (Kobayashi et al., 2015).

The OMIP diagnostic protocol is built from the CMIP5 ocean diagnostics of Griffies et al. (2009a). Describing the diagnostics forms the bulk of this paper, with this material largely within various appendices. A key goal for this OMIP diagnostic suite is that it enables a wide suite of ocean-related research emerging from CMIP6. Analysis plans for this research take various shapes, including projects led by various CMIP6 MIPs and related science communities. Additionally, we anticipate that some of the best science from CMIP6 will emerge from questions yet to be asked, particularly as they relate to studies from students and post-doctoral researchers. We trust that these diagnostics will enable extensive ongoing and new science, and will nurture improvements to the model tools central to climate science.

It will take years to determine the success of OMIP as an experimental protocol and as a diagnostic protocol. Regardless, it is our hope that this document will serve as a useful reference point for further endeavours such as this one. Quite generally, global models are firmly embedded in the science of oceanography and climate. Careful design of experiments and diagnostics, with correspondingly thorough and creative analysis of their output across a suite of models, offers ongoing opportunities for novel scientific insights, robust predictive skill, and continued improvement to the model tools.

5 Data availability

The model output from simulations described in this paper will be distributed through the Earth System Grid Federation (ESGF) with digital object identifiers (DOIs) assigned. The model output will be freely accessible through data portals after registration. In order to document CMIP6’s scientific impact and enable ongoing support of CMIP, users are obligated to acknowledge CMIP6, the participating modelling groups, and the ESGF centres. Details can be found on the CMIP Panel website at http://www.wcrp-climate.org/index.php/wgcm-cmip/about-cmip.

Further information about the infrastructure supporting CMIP6, the metadata describing the model output, and the terms governing its use are provided by the WGCM Infrastructure Panel (WIP) in their invited contribution to this Special Issue (Balaji et al., 2016).
Appendix A: Surveying technical aspects of OMIP diagnostics

In this appendix, we discuss various technical aspects of generating the OMIP diagnostics.

A1 Specifications for time sampling

There are three time-sampling periods requested for various OMIP diagnostics: day, month, and year. Each period is sampled as a time average. Time averages include all model time steps over the given period; there is no sub-sampling. Products of time-dependent fields are time-averaged as a product, again using all model time steps to build the average.

Additionally, we request the maximum and minimum mixed layer depths over each monthly period (Sect. H24). These diagnostics are computed as the maximum and minimum of the mixed layer depth for any given snapshot within the month.

A2 Specifications for spatial sampling

Spatial integrals for regional diagnostics or transports across lines are computed using all grid points within the region or line. There is no sub-sampling.

A3 Specifications for horizontal gridding

In designing a protocol for horizontal gridding of ocean model diagnostics, we are wedged between two conflicting aims. The first aim is to offer two-dimensional and three-dimensional diagnostics that can be readily mapped and differentiated for metric-based analyses (see Sect. 3.1). This aim is facilitated by providing output on a spherical grid. Indeed, the simplest case is for all output to be on the same spherical grid.

The second aim is to archive diagnostics that respect properties of the numerical model, such as conservation of scalar fields (e.g. heat and salt), thus serving the needs of budget analyses (see Sect. 3.1). Unfortunately, regridding from model native grids to spherical grids generally involves a land–sea mask distinct from the model native mask. When changing the land–sea mask it is difficult to ensure conservation even when using “conservative” regridding methods. For example, mass will generally differ when changing the land–sea mask. The absence of conservation may be of minor consequence for many metric-based analysis purposes. However, it sacrifices the needs of budget analyses.

Given these conflicting needs, it is no surprise that the community remains without a firm consensus on specifications for the horizontal grid. We offer a compromise proposal that aims to facilitate both metric-based and budget-based analyses of the OMIP diagnostics.

A3.1 Native horizontal grids and regridding to spherical grids

Spherical latitude–longitude grids are rarely used as the native grid for global ocean simulations. The reason for non-spherical grids is to remove the North Pole spherical coordinate singularity from the ocean domain. More generally, the native ocean model grids span a wide spectrum, from general orthogonal (e.g. Smith et al., 1995; Murray, 1996; Madec and Imbard, 1996), unstructured finite volume (e.g. Ringler et al., 2013), to unstructured finite element (e.g. Danilov, 2013). This wide suite of grids makes it difficult to prescribe a single protocol for ocean diagnostics in CMIP.

For some purposes, analysts can ignore the non-spherical coordinate nature of native grid output. The reason is that many software packages have regridding methods to support visualization and difference mapping. Two common examples are the tripolar grids of Murray (1996) and Madec and Imbard (1996) and the displaced bipolar grid of Smith et al. (1995). Both grids are commonly used in the community, so that experience makes the data little more complex than when placed on a spherical latitude–longitude grid.

In contrast, unstructured grids generally require regridding to spherical coordinates for analysis, since native unstructured diagnostics are unlikely to be analysed by CMIP6 analysts. We therefore recommend that all unstructured model diagnostics be mapped to a spherical coordinate grid. This recommendation in fact has long been followed by the unstructured mesh community. Consequently, this community has in large part taken the lead in developing and using regridding tools. For example, the unstructured finite volume module of Ringler et al. (2013) makes use of tools detailed in Ullrich and Taylor (2015) for both scalars and vectors (Todd Ringler, personal communication, 2016).

Even so, there is no community consensus on the best method to regrid ocean model fields. Different applications require different approaches. Furthermore, the ocean presents a particularly challenging problem for regridding, given the complexity of the land–sea boundaries.

A3.2 Area information to facilitate regridding to standard spherical grids

In some cases, regridded diagnostics are needed merely for visualization purposes and/or to produce difference maps. Problems with non-conservation can often be ignored in this case. Furthermore, since horizontal grid cell dimensions are static in CMIP models, regridding from native horizontal grids to a spherical grid can be performed offline.

Regridding requires area information about the native model source grid and the target grid. The WGCM Infrastructure Panel (WIP) contribution to this CMIP6 Special Issue (Balaji et al., 2016) requires that all native grid data have an external_variables attribute that points to a weights field in a standard format. These weights facilitate regridding to
one of two standard grids, either the 1° or 1/4° spherical grids from Levitus (1982) and Locarnini et al. (2013). The format should be the ESMF/SCRIP format for weights. Regridding to a sphere is arguably more trustworthy if performed by the respective modelling centres prior to submitting data to the CMIP archives. We therefore request that certain Priority = 1 tracer and boundary flux fields be submitted both on the native grids (just for structured mesh models) as well as on a spherical grid. Acknowledging that some modelling groups will not supply both native and spherical fields, we request the above-noted horizontal area grid weights for all diagnostics.

A3.3 Summary of the horizontal grid specifications

Here is a summary of the specifications for horizontal gridding of ocean diagnostics in CMIP6.

- All two-dimensional and three-dimensional diagnostic fields produced by structured grid models should be archived on the model native grid. Native grid diagnostics serve the needs of budget analysis.

- All two-dimensional and three-dimensional diagnostic fields produced by unstructured grid models should be archived on a spherical grid.

- To serve the needs of metric-based analysis (i.e. mapping and differencing), we recommend the following.
  - All native grid diagnostics should have an external_variables attribute that points to a weights field (Balaji et al., 2016). These weights facilitate regridding of native fields to standard spherical grids.
  - We recommend that the following tracer-related diagnostics be archived on both the native and spherical grids. Doing so removes the need for analysts to regrid these fields.
    - Two-dimensional Priority = 1 tracer field diagnostics and their corresponding surface fluxes
    - Three-dimensional Priority = 1 tracer fields
    - The spherical grid should be the standard 1° or 1/4° grid from Levitus (1982) and Locarnini et al. (2013) (see more discussion in Appendix C).
    - Diagnostics stored in either native or spherical grids should have the same standard name and the same CMIP/CMOR (Climate Model Output Rewriter) name. Within files, the gridded fields should be distinguished by the cell_measures, coordinates, and auxiliary CF (Climate and Forecast) attributes. The same variable in native and spherical form can never coexist in the same file. The WGCM Infrastructure Panel (WIP) will provide means to distinguish the gridded fields (Balaji et al., 2016).

- Refer to Appendix B for further details of grid cell volume and area, and Appendix C for details of spatial sampling.

A3.4 A case in point

For many CMIP6 simulations, GFDL is developing a 1/4° tripolar ocean grid, with 75 levels in the vertical down to the 5500 m bottom. To reduce archive burden, GFDL will coarsen the ocean diagnostics to a 1° spherical grid with 33 levels in the vertical, with this grid defined by the World Ocean Atlas (Levitus, 1982; Locarnini et al., 2013). Besides reducing archive space, this approach greatly facilitates the use of model diagnostics across a broad element of the analysis community.

A4 Specifications for vertical gridding

There are three general paradigms of vertical coordinates in use by the ocean model community (Griffies et al., 2000), with the choice guided by the scientific use of the model. The traditional geopotential coordinate has dominated ocean climate modelling since the pioneering work of Bryan (1969). This choice matches well to the predominant means for mapping observation-based data, which typically occurs on geopotential or pressure levels. However, the alternative paradigms of terrain-following coordinates and isopycnal coordinates are gaining traction in the climate community, along with even more general features offered by the arbitrary Lagrangian–Eulerian (ALE) method (e.g. Bleck, 2002; Donea et al., 2004; Adcroft and Hubert, 2006; Petersen et al., 2015). Following the CMIP5 protocol, the CMIP6 ocean diagnostics should be regridded to depth/pressure vertical levels for those models not based on one of the vertical coordinates \( z, z^*, p, \) or \( p^* \), with details of these vertical coordinates provided in Appendix C2.\(^5\)

- Three-dimensional diagnostics should be archived on one of the depth- or pressure-based vertical coordinates \( z, z^*, p, \) or \( p^* \) (Sect. C2).

- Models making use of alternative vertical coordinates should regrid diagnosed fields to one of the coordinates \( z, z^*, p, \) or \( p^* \). Vertical regridding should be conservative and performed online each model time step so as to ensure scalar content (e.g. heat, salt, water) is preserved across the vertical native and vertical regridded grids.

\(^5\)There is one exception for the vertical; namely, the overturning mass transport is of scientific interest on both depth/pressure surfaces and potential density surfaces (with 2000 dbar referencing). We detail this diagnostic in Appendix I6.
A5 Data precision for diagnostics

Besides ensuring proper practices for temporal and spatial sampling, it is important to understand the needs for data precision of the archived diagnostics. This issue is important to ensure that analysts are able to maintain accuracy when calculating derived diagnostics, and to minimize storage footprint, particularly as model resolution and diagnostic requests increase.

All model data submitted to CMIP6 should follow the netCDF4 protocol. Precision of the data should be sufficient to ensure robust statistical analyses. For most applications, single precision (seven significant digits) is sufficient.

A5.1 Features of netCDF4

The CMIP5 archives adhered to the netCDF3 protocol, meaning that CMIP5 data was written using single precision (32-bit float) format. In contrast, key features of netCDF4 that motivate its use for CMIP6 include lossless compression (deflation) and file access/read performance tools of chunking and shuffling. Furthermore, most standard analysis packages now support netCDF4 formatted data (see Sect. A5.2), thus placing no burden on the analyst.

In Table A1, we provide information about precision features of different data formatting within the netCDF4 protocol. For most analysis purposes, single precision (seven significant digits) is sufficient. However, length and area factors from grids may usefully be saved in double precision, given that area factors are the basis for statistical analyses and regridding. Notably, it is rare to find observational-based oceanographic data with significance greater than half precision (three significant digits).

A5.2 Software packages supporting netCDF4

NetCDF4 is now a standard library for many software packages, including those listed in Table A2. Consequently, using netCDF4 deflation (and reducing file sizes by roughly 50% in a lossless format) should pose no hindrance for CMIP6 analysis. Note that the 50% compression assumes that the supplied netCDF4 libraries are built with HDF5 and zlib support, which are needed to garner the compression functionality.

A6 Prioritizing the diagnostics

We make use of three priorities for OMIP diagnostics.6

– Priority 1 diagnostics serve as a baseline for the CMIP physical ocean diagnostics. These diagnostics are of

6CMIP5 level = 0 diagnostics detailed in Griffies et al. (2009a) are now termed CMIP6 Priority = 1 diagnostics, and so on for the other priorities. This change in prioritization nomenclature brings the OMIP diagnostic suite into alignment with other CMIP6 MIPs.

---

Table A1. Listing of available data types using the netCDF4 data model, and example data precision for ocean salinity using these data types. Plausible observed salinity ranges (PSS-78; Lewis and Perkin, 1981) are between 2 and 42 (open ocean salinities normally range from 32 to 38), which is the range over which the Practical Salinity Scale (1978) provides coverage. This scale was used to define the valid_min and valid_max from which the representative salinity precision (last column) is calculated. For further details on the precision, see http://en.wikipedia.org/wiki/IEEE_floating-point#Basic_formats and https://www.unidata.ucar.edu/software/netcdf/docs/netcdfc/NetCDF_002d4AtomicTypes.html.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>NetCDF4 type</th>
<th>Precision</th>
<th>Minimum</th>
<th>Maximum</th>
<th>Decimals</th>
<th>Example (35.1234567891)</th>
</tr>
</thead>
<tbody>
<tr>
<td>lat/lon/lon</td>
<td>8-bit signed integer</td>
<td>NC_byte</td>
<td>8-bit</td>
<td>-128</td>
<td>127</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>lon/lat/lat</td>
<td>8-bit unsigned integer</td>
<td>NC_ubyte</td>
<td>8-bit</td>
<td>0</td>
<td>255</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>lon/lat/lat</td>
<td>16-bit signed integer</td>
<td>NC_short</td>
<td>16-bit</td>
<td>-32768</td>
<td>32767</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>lat/lon/lon</td>
<td>16-bit unsigned integer</td>
<td>NC_ushort</td>
<td>16-bit</td>
<td>0</td>
<td>65535</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>lat/lon/lon</td>
<td>32-bit signed integer</td>
<td>NC_int</td>
<td>32-bit</td>
<td>-2147483648</td>
<td>2147483647</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>lat/lon/lon</td>
<td>32-bit unsigned integer</td>
<td>NC_uint</td>
<td>32-bit</td>
<td>0</td>
<td>4294967295</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>lat/lon/lon</td>
<td>64-bit signed integer</td>
<td>NC_int64</td>
<td>64-bit</td>
<td>-9223372036854775808</td>
<td>9223372036854775807</td>
<td>15.95</td>
<td>–</td>
</tr>
<tr>
<td>lat/lon/lon</td>
<td>64-bit unsigned integer</td>
<td>NC_uint64</td>
<td>64-bit</td>
<td>0</td>
<td>18446744073709551615</td>
<td>15.95</td>
<td>–</td>
</tr>
<tr>
<td>temperature</td>
<td>half</td>
<td>f16/binary16</td>
<td>half</td>
<td>–∞</td>
<td>∞</td>
<td>3.31</td>
<td>–</td>
</tr>
<tr>
<td>pressure</td>
<td>single</td>
<td>f32/binary32</td>
<td>single</td>
<td>–∞</td>
<td>∞</td>
<td>7.22</td>
<td>–</td>
</tr>
<tr>
<td>pressure</td>
<td>double</td>
<td>f64/binary64</td>
<td>double</td>
<td>–∞</td>
<td>∞</td>
<td>15.95</td>
<td>–</td>
</tr>
</tbody>
</table>

www.geosci-model-dev.net/9/3231/2016/
Table A2. Table of software products that support netCDF4. Listed are the software packages and the earliest version of that software that supports netCDF4.

<table>
<thead>
<tr>
<th>Software supporting netCDF4</th>
<th>earliest version</th>
</tr>
</thead>
<tbody>
<tr>
<td>CDO</td>
<td>1.5</td>
</tr>
<tr>
<td>CDAT</td>
<td>5.2</td>
</tr>
<tr>
<td>Ferret</td>
<td>6.6</td>
</tr>
<tr>
<td>IDL</td>
<td>7</td>
</tr>
<tr>
<td>Matlab</td>
<td>R2010b</td>
</tr>
<tr>
<td>NCO</td>
<td>3.1</td>
</tr>
<tr>
<td>NCL</td>
<td>6.1.1</td>
</tr>
<tr>
<td>Python</td>
<td>2.6</td>
</tr>
<tr>
<td>CF-Python</td>
<td>1.0</td>
</tr>
</tbody>
</table>

highest priority as they support a broad baseline of CMIP ocean-related studies. Specifically, they facilitate

- characterizing the model configuration;
- evaluating the simulated climate state;
- evaluating the simulated climate change.

- Priority = 2 diagnostics support more in-depth understanding of the simulations. Specifically, they facilitate

  - measuring mass and tracer transports over the globe, within semi-enclosed basins, and across sections;
  - quantifying mass, heat, and salt budget terms on global and/or regional scales;
  - documenting auxiliary fields that render a more complete quantitative characterization of the simulation, such as ventilation;

- Priority = 3 diagnostics serve process-based analyses of CMIP ocean simulations. Specifically, they facilitate

  - quantifying three-dimensional heat and salt budgets;
  - studying sub-monthly transients and/or variability;
  - documenting of parameterized eddy coefficients to characterize subgrid-scale schemes;
  - quantifying impacts on energetics from parameterizations.

A7 Tabulation of ocean diagnostics

In Appendices G, H, I, J, K, L, M, and N, we tabulate the ocean model diagnostics recommended for the CMIP6 archive. These tables contain the following information:

- diagnostic name according to the CMOR short name and the CF standard name;
- community sponsoring the diagnostic (Sect. 3.2);
- relation to CMIP5 as detailed in Griffies et al. (2009a) (same, new, or modification);
- physical units;
- time sampling for output (time mean over day, month, or year, or minimum/maximum over a month);
- spatial shape (i.e. one-dimensional, two-dimensional, or three-dimensional);
- recommended grid (native, spherical, depth/pressure);
- prioritization guidance (Appendix A6);
- experiment for which the diagnostic should be saved. Unless otherwise specified, results should be submitted for the full length of each experiment.

All fields are reported as “missing” over grid cells that are entirely land. The spatial shape of a field that has no horizontal dimension(s) is indicated by a 0 (i.e. a time series); one-dimensional meridional spatial fields are denoted by Y (e.g. meridional mass or heat transport); horizontal two-dimensional fields are denoted XY; vertical two-dimensional fields are denoted YZ or Yρ; three-dimensional fields are denoted XYZ.  

A8 Names and units for the diagnostics

The CMOR names and units for diagnostics are listed in the tables. Model diagnostics submitted to the CMIP6 archive must follow this name and unit convention. Notably, the CMOR names are becoming a community standard given the widespread development of CMIP analysis software.

There is an additional name that is supported by the CF metadata conventions. We list these CF “standard names” in the following sections, and relate these names to the CMOR names. The CF standard names are self-explanatory and interdisciplinary, which can result in rather long names. We thus include them as sub-tables within the diagnostic tables.

Appendix B: Grid cell volume and horizontal area

In order to calculate ocean area integrals and volume integrals, information is needed to weight the grid cells in a manner consistent with conservation properties of the model. All CMIP6 ocean models have a fixed horizontal grid and hence constant horizontal cell areas. Cell areas (areacello) should be stored in each data file (Table G1) in order to keep this important information within each diagnostic file. In contrast, the cell thicknesses (thkcello), and hence cell volumes and masses (masscello), may be time-dependent for many ocean
models. We discuss in this section how to specify ocean grid cell volumes and masses for CMIP6.

**B1 Volume-conserving Boussinesq ocean models**

Boussinesq ocean models are based on volume-conserving kinematics, with these models having been used since the early days of ocean modelling (Bryan, 1969). For budget purposes, Boussinesq models use a constant reference density for seawater, $\rho_0$. Hence, the grid cell mass, $dM$, is equal to the grid cell volume, $dV$, multiplied by the constant reference density (Sect. H3)

$$dM = \rho_0 dV \quad \text{Boussinesq models (kg).} \quad (B1)$$

A netCDF scalar variable containing the constant

$$\rho_0 = rhozero \quad \text{(kg m}^{-3}\text{)} \quad (B2)$$

should be archived in the same file (Table G1).

**B1.1 Boussinesq models with static grid cell volumes**

Certain Boussinesq ocean models assume that grid cells have time-independent volumes, meaning they have static grid cell thicknesses. This property holds for geopotential Boussinesq ocean models based on barotropic dynamics using either the rigid-lid approximation (Bryan, 1969; Pinardi et al., 1995) or a linearized free surface (Dukowicz and Smith, 1994; Roulet and Madec, 2000). By construction, these models do not allow for changes in the volume associated with boundary water fluxes. Consequently, they must make use of virtual tracer flux boundary conditions discussed in Sect. K1.7 as well as Huang and Schmitt (1993) and Griffies et al. (2001).$^8$

If the Boussinesq model has time-independent grid cell volumes, then the grid cell masses (Eq. B1) are also constant in time. For these models, the CMIP6 masscello field for cell mass (sea_water_mass_per_unit_area) is to be saved as a static XYZ variable measuring the mass per area of the tracer grid cell (Table G1). Furthermore, for cells that occupy the entire vertical extent of the grid cell layer (i.e. except for partial cells at the top or bottom of the ocean), the cell thickness can be calculated as the difference of the depth-bounds for the layer. This thickness should equal the cell mass per unit area divided by the Boussinesq reference density. Only for these models, the cell_thickness variable thkcello is not required.

**B1.2 Boussinesq models with time-dependent grid cell volumes**

Many Boussinesq models have time-dependent cell volumes, with examples including isopycnal models, terrain-following sigma models, and stretched depth-coordinate $z^*$ models (Sect. C2). For these models, the cell thickness, thkcello (Table H1), is time-dependent. A separate masscello file is required for each distinct set of time coordinates at which other monthly XYZ scalar fields are provided (Tables H1, L1, M1, and N1). Doing so provides a one-to-one correspondence between the variable to be weighted (e.g. thetao) and the variable providing the weights (masscello). For Boussinesq models, the reference density rhozero should also be saved in each masscello file. The cell thickness, thkcello, is not required, since it can be easily diagnosed through

$$\text{thkcello} = \frac{\text{masscello}}{\text{areacello} \times \text{rhozero}} \quad (m) \quad (B3)$$

In contrast, for typical non-Boussinesq models (see Sect. B2), both masscello and thkcello are required on the same time frequency as the primary fields (e.g. monthly).

**B2 Mass-conserving non-Boussinesq ocean models**

Non-Boussinesq models are based on mass-conserving kinematics (Griffies and Greartbatch, 2012). When hydrostatic, such models are naturally formulated using pressure, or a function of pressure, as the vertical coordinate (Huang et al., 2001; DeSzoëke and Samelson, 2002; Marshall et al., 2004). If based on pressure, then the mass of a grid cell remains constant in time, with the equations isomorphic to the depth-coordinate Boussinesq ocean equations.

In general, the cell thickness, thkcello, and cell mass, masscello (Table 2.2), are time-dependent. A separate masscello file is required for each distinct set of time coordinates at which other XYZ scalar fields are provided (Tables H1, L1, M1, and N1). Doing so provides a one-to-one correspondence between the variable to be weighted (e.g. thetao) and the variable providing the weights (masscello).

**B3 Details of the grid information**

The link between a scalar data variable and the corresponding areacello and masscello variables is made using the cell_measures and associated_files attributes available in a netCDF file. For a field on an XY longitude–latitude horizontal grid, the file should contain variables written as

```text
float pr(time,latitude,longitude);
p:standard_name="rainfall_flux";
p:units="kg m-2 s-1";
float areacello(latitude,longitude);
areacello:standard_name="cell_area";
areacello:units="m2";
```

The areacello variable is not required to have the variable name areacello. In cell_measures, “area: VARNAME” identifies the variable by name.

For a field on an XYZ grid, the file should contain variables written as

```text
```
Appendix C: Details for spatial sampling

In this Appendix, we offer further details regarding horizontal and vertical sampling. Further issues related to gridding are discussed in the WGCM Infrastructure Panel (WIP) contribution to this CMIP6 special issue (Balaji et al., 2016).

C1 Integration over spatial regions

We start with an easy question: how to sample fields to be integrated over a spatial region, such as a basin or section? The answer is to compute the integral using all model grid points within the relevant domain and time average using all model time steps. There is no sub-sampling in space or time.

C2 Vertical gridding

In models with time-dependent grid cell volumes/masses (e.g. isopycnal models, sigma coordinate models, vertical ALE models), it is critical that vertical regridding occur online for each model time step to include correlations between the fluctuating grid cell geometry and the scalar field. Re-gridding subsampled fields in such cases generally leads to erroneous results; it must be avoided.

- For models based on \( z \) (geopotential coordinate), stretched depth \( z^* \), pressure, or stretched pressure \( p^* \), there is no need to perform a depth regridding, unless aiming to regrid to a standard vertical grid such as the 33 levels used by the World Ocean Atlas (Levitus, 1982; Locarnini et al., 2013).

- For models with a time-dependent grid cell thickness that do not use \( z, z^*, p, \) or \( p^* \) vertical coordinates (e.g. isopycnal, terrain following, ALE), the vertical regridding step should be computed each model time step to ensure exact conservation. See Sects. C2.2 and C2.3 for more details of these coordinates.

- Vertical regridding should occur onto a vertical coordinate based on depth (for Boussinesq models) or pressure (for non-Boussinesq models).

- Pressure-based vertical grids should be measured in dbar, in order to facilitate easy comparison to depth-based models using metres.

- Depth and pressure increase downward from the ocean surface, whereas the vertical geopotential \( z \) increases upward starting from the resting ocean surface at \( z = 0 \).

- For those choosing to coarsen the vertical resolution of their archived diagnostics, modellers are encouraged to map onto the 33 levels used for the World Ocean Atlas (Levitus, 1982; Locarnini et al., 2013). However, care should be given to models that do not share the same 5500 m depth as the World Ocean Atlas.

C2.1 To regrid or not?

There are two questions to answer regarding the vertical coordinate.

- Should model output be regridded in the vertical to a common vertical coordinate?

- If regridded, then what is a scientifically relevant vertical coordinate?

There is no ambiguity regarding the vertical grid when working with Boussinesq rigid-lid geopotential-coordinate ocean models, as each grid has a fixed vertical position. It was thus sensible for CMIP3 (WGCM, 2007) to recommend that output in the vertical be on a geopotential grid, preferably regridded to the 33 depth levels used by Levitus (1982) and Locarnini et al. (2013). The more recent trend towards free surface geopotential models raises only trivial issues with the surface grid cell, and these issues can be ignored without much loss of accuracy.\(^9\) However, the move towards pressure, isopycnal, terrain-following, and general/hybrid models increases the complexity of vertical coordinate questions.

We make the following observations and clarifications regarding the recommendations for vertical regridding.

- For isopycnal, terrain following, and general/hybrid models, we recommend regridding to \( z^* \) for Boussinesq models and \( p^* \) for non-Boussinesq (\( z^* \) and \( p^* \) are defined below). This recommendation is based on the predominant needs of analysis. The one exception concerns the overturning streamfunction, which is archived on both geopotential/pressure and density surfaces (Appendices I6 and I7).

\(^9\) We know of no group that considers the question of regridding model fields in the top model cell of a free surface geopotential model to a pre-defined geopotential level. Indeed, there is little reason to do so, as the top cell, whether it has a centre at \( z = -1 \) m or \( z = 1 \) m, for example, still provides the model version of sea surface properties. 

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– Conservative vertical regridding with straightforward linear interpolation is reasonably accurate so long as the regridding is done every model time step. Regridding subsampled fields can lead to erroneous analysis, especially with isopycnal models, and so must be avoided.

– Contrary to the situation in the horizontal, separate vector components can be treated as scalars for the purpose of regridding in the vertical.

C2.2 Rescaled geopotential for Boussinesq models

For Boussinesq models, it is natural to consider regridding to the rescaled geopotential coordinate (Stacey et al., 1995; Adcroft and Campin, 2004)

\[ z^* = H \left( \frac{z - \eta}{H + \eta} \right) \tag{C1} \]

In this equation, \( z \) is the geopotential, \( z = -H(x, y) \) is the ocean bottom, and \( z = \eta(x, y, t) \) is the deviation of the free surface from a resting ocean at \( z = 0 \). To better understand the ratio, note that \( z - \eta \) is the thickness of seawater above a particular geopotential, and \( H + \eta \) is the total thickness of seawater in the fluid column. Surfaces of constant \( z^* \) correspond to geopotentials when \( \eta = 0 \). For most practical applications of global ocean modelling, \( z^* \) surfaces only slightly deviate from constant geopotential surfaces even with nonzero \( \eta \) fluctuations. The advantage of \( z^* \) over geopotential is that it has a time-independent range \( -H \leq z^* \leq 0 \), thus allowing for a more straightforward mapping from a free surface isopycnal or terrain-following model.

C2.3 Rescaled pressure for non-Boussinesq models

The rescaled pressure coordinate is defined as

\[ p^* = p_b^0 \left( \frac{p - p_a}{p_b - p_a} \right) \tag{C2} \]

where \( p \) is the pressure at a grid point; \( p_a(x, y, t) \) is the pressure applied at the ocean surface due to overlying atmosphere, sea ice, and/or ice shelves; \( p_b(x, y, t) \) is the pressure at the ocean bottom; and \( p_b^0(x, y) \) is a static reference bottom pressure, such as the initial bottom pressure. To better understand the ratio, note that in a hydrostatic ocean, \( g^{-1}(p - p_a) \) is the mass per horizontal area of seawater situated above a pressure level \( p \), and \( g^{-1}(p_b - p_a) \) is the total mass per horizontal area of seawater in the fluid column. For most practical applications of global modelling, constant \( p^* \) surfaces only slightly deviate from constant pressure surfaces, even with nonzero fluctuations of \( p_b \). The advantage of \( p^* \) over pressure is that \( p^* \) has a time-independent range \( 0 \leq p^* \leq p_b^0 \), thus allowing for a more straightforward mapping from a non-Boussinesq model making use of alternative vertical coordinates.

C2.4 Visualization and analysis purposes

For visualization purposes, the distinction between geopotential (or rescaled geopotential) and pressure (or rescaled pressure) can be ignored to within great accuracy, so long as geopotential is measured in metres and pressure is measured in decibars.

For analysis purposes, the distinction between geopotential (or rescaled geopotential) and pressure (or rescaled pressure) can be ignored when working with model native scalars and fluxes. The differences cannot be ignored when performing off-line integration of velocity components to approximate fluxes. This is a reason that we request online computed mass fluxes in addition to velocity components (Appendix I).

C3 Vector fields

It is mathematically straightforward to transform (e.g. rotate) a continuum vector field from one coordinate system to another using methods of tensor analysis (e.g. chap. 20 in Griffies, 2004). Unfortunately, these continuum mathematical methods are ambiguous for discrete vector fields. For example, the commonly used C-grid has horizontal velocity components sitting on a C-grid, these components should be mapped onto an A-grid or B-grid, depending on what is more convenient based on the native model grid. Interpolating vector components to a single point greatly facilitates routine interpretation.

If any regridding is performed to the vector fields, we recommend it be done using a high-order (higher than linear) interpolation scheme, thus ensuring smoothness and accuracy. But further manipulation of the regrided vector fields is discouraged, since the regrided vector fields can have spurious divergence and curl. Conservation is generally not needed for vector components. Furthermore, for native vector components sitting on a C-grid, these components should be mapped onto an A-grid or B-grid, depending on what is more convenient based on the native model grid. Interpolating vector components to a single point greatly facilitates routine interpretation.

C4 Zig-zag method for estimating poleward transports

We recommend that each group using non-spherical grids develop a native-grid algorithm that computes the closest native grid approximation to the basin integrated poleward transports. That is, transports across a section (e.g. meridional overturning at a given latitude, transport through a passage, or vertically integrated poleward heat transport) should be computed consistent with the native grid by finding a nearly equivalent path to the section that has been “snapped” to the native grid (often resulting in a “zig-zag” path) (e.g.
see Fig. J1 and Fig. C2 of Forget et al., 2015). This approach retains the native grid variables, and so allows for conservation of transports. It also avoids ambiguities associated with defining a regridded land/sea mask. The resulting transports should be made available as a function of latitude (even though the integrations are not exactly along latitude circles). The latitude spacing should be comparable to that of the model grid spacing.

Appendix D: Seawater thermodynamics

We offer specifications for treating seawater thermodynamics, in particular for temperature, salinity, and associated heat and salt transports. These specifications are made in light of the endorsement by the international oceanography community of the Thermodynamic Equation of State 2010 (TEOS-10) (IOC et al., 2010). TEOS-10 is based on a consistent theory of seawater thermodynamics, as well as empirical measurements updated since the UNESCO-80 equation of state. TEOS-10 represents a major move forward in the fundamental science and practice of seawater thermodynamics.

D1 Balancing the needs

We aim to provide a rational and practical framework for meaningful comparisons across climate models and observation-based measurements. Meeting this aim supports the primary means whereby analysis of CMIP simulations contributes to climate science. In offering recommendations for seawater thermodynamics, we must balance the desire to remain true to IOC et al. (2010) while acknowledging the practical needs for a successful model intercomparison. The document http://www.teos-10.org/pubs/Getting_Started.pdf provides a starting point for incorporating TEOS-10 into ocean models and analysis, and Roquet et al. (2015) offer further steps for ocean models.

Although it has been some years since IOC et al. (2010), many modelling groups are just now incorporating the updated TEOS-10 seawater thermodynamics into their CMIP6 models. Indeed, some groups are unable to realize this transition in time for CMIP6. Hence, CMIP6 will contain models based on TEOS-10 and others based on pre-TEOS-10. Furthermore, there remain unanswered research questions raised by IOC et al. (2010), in particular regarding the treatment of salinity. For CMIP6, we cannot impose strict standards defining what it means to be “TEOS-10 compliant” when research remains incomplete. As of this writing, there are zero peer-reviewed publications using ocean climate simulations based on the suite of recommendations from TEOS-10. In short, the community is in a transition stage from pre-TEOS-10 to TEOS-10. For CMIP6, we thus offer a cosmopolitan approach rather than one based on a well-defined territory.

D2 Specification for temperature

Regardless of the model thermodynamics, modellers should archive potential temperature, \( \theta \). For models using pre-TEOS-10 ocean thermodynamics, no change is required relative to previous CMIPs. For models using TEOS-10 thermodynamics, in which Conservative Temperature, \( \Theta \), is the model prognostic field, we still recommend archiving potential temperature to allow for meaningful comparisons. Doing so requires an online diagnostic calculation to convert at each time step from Conservative Temperature to potential temperature. Additionally, we request TEOS-10-based models to archive Conservative Temperature, anticipating that future CMIPs will naturally see more models based on Conservative Temperature rather than potential temperature.

D3 Specification for heat content

The air–sea flux of heat is exactly the air–sea flux of potential enthalpy (since the reference gauge pressure of potential enthalpy is 0 dbar). Apart from warming caused by the dissipation of turbulent kinetic energy (as well as another smaller term), potential enthalpy is a conservative variable in the ocean (McDouggall, 2003; Graham and McDougall, 2013), meaning that it satisfies a scalar conservation equation analogous to a source-free material tracer. Because of these properties of potential enthalpy, we are justified in calling it the heat content of seawater. That is, the heat content (in Joule) of a seawater parcel or an ocean model grid cell is seawater heat content \( = h_o \rho dV \),

\[ (D1) \]

with

\[ h_o = c_p^o \Theta \]

\[ (D2) \]

the potential enthalpy per mass, \( \Theta \) the Conservative Temperature, \( dV \) the parcel or grid cell volume, and \( \rho \) the in situ seawater density. The seawater heat capacity, as defined by TEOS-10, is the constant

\[ c_p^o = 3991.86795711963 \text{J kg}^{-1} \text{K}^{-1} \].

\[ (D3) \]

The 15 significant digits in \( c_p^o \) is based on a numerical fit. The observation-based data used in this fit are measured to a precision no greater than three or four significant digits. Hence, there is no physics in \( c_p^o \) beyond roughly four significant digits.

Ocean climate models measure heat content (in Joules) of a grid cell according to

model heat content in a grid cell \( = c_p^o \times \text{prognostic temperature} \times \rho dV \).

\[ (D4) \]

We now comment on this model practice and relate it to TEOS-10 and CMIP6.
D3.1 Boussinesq reference density

For a Boussinesq fluid, mass, tracer, and momentum budgets replace the in situ density, $\rho$, with a constant reference density, $\rho_o$ (except for the buoyancy force, where $\rho g$ retains the in situ density). Not all groups use the same $\rho_o$ (see Roquet et al., 2015 for a discussion of various choices). Modellers should therefore archive in CMIP this constant according to the request in Table G1.

D3.2 Heat capacity

The ocean model heat capacity, $c_p^o$, is constant. However, the ocean model heat capacity is not always equal to the TEOS-10 recommended value given by Eq. (D3). We thus ask to archive the model heat capacity in Table G1. We note that the TEOS-10 heat capacity $c_p^o$ (Eq. D3) was chosen so that the surface area average (and ocean mass average) of $c_p^o \theta$ closely matches the corresponding surface area (and ocean mass) averages of potential enthalpy. We thus highly recommend models choose a heat capacity $c_p^o$ for both pre-TEOS-10 and TEOS-10 usage.

D3.3 Heat content

Expression (D4) is the heat content for the respective TEOS-10 and pre-TEOS-10 ocean models. This expression is relevant for CMIP6 since the model prognostic temperature field evolves according to grid cell budgets. Hence, pre-TEOS-10 models should not archive heat content by diagnosing the Conservative Temperature. Rather, they should measure heat content as always done for previous CMIPs, using the model prognostic potential temperature. Likewise, TEOS-10 models should measure heat content using the TEOS-10 recommendation (Eq. D2), using the model prognostic Conservative Temperature field.

D3.4 Boundary heat fluxes

As noted by McDougall (2003), boundary heat fluxes affect the ocean potential temperature, with a tendency proportional to the reciprocal of the specific isobaric heat capacity of seawater. Importantly, this heat capacity varies by 5% over the ocean. However, no ocean climate model makes use of a non-constant specific isobaric heat capacity, even though the temperature field of ocean models is often interpreted as potential temperature. This inconsistency is motivated by the desire to have the model ocean heat content related directly to the model prognostic temperature field, with that temperature field time stepped according to conserved budget equations. Turning this inconsistency into an opportunity, McDougall (2003) noted that ocean models using a constant heat capacity, $c_p^o$, may in fact be interpreted as using Conservative Temperature rather than potential temperature. There are errors associated with this interpretation arising from the calculation of in situ density and boundary heat fluxes. Nonetheless, these errors may in fact be smaller than those associated with ignoring the non-constant heat capacity. Research is needed to further pursue this interpretation.

D3.5 Heat transport

Heat transport and its convergence are determined by various transport processes (e.g. advection, diffusion) impacting on the grid cell heat content (Eq. D4). We ask for the archival of such transports and convergences in Tables I1 and L1.

D4 Specification for salinity

Ocean models based on pre-TEOS-10 thermodynamics carry a salinity variable that approximates the observed quantity of Practical Salinity ($S_p$) – the observed variable from which most ocean model initial states are obtained (often from a version of the World Ocean Atlas such as Zweng et al., 2013). The model version of Practical Salinity is influenced by transport in the ocean interior, and through atmospheric and terrestrial boundary freshwater fluxes that alter the salt mass concentration. However, these similarities between model and observations are more subtle when we consider the new salinity definitions provided with TEOS-10 (IOC et al., 2010).

TEOS-10 aims to better quantify a poorly constrained aspect of the observed quantity of ocean salinity. The new salinity definitions are preferred over Practical Salinity because the thermodynamic properties of observed seawater are directly influenced by the mass of dissolved constituents whereas Practical Salinity depends only on conductivity (and coincident temperature). For example, exchange a small mass of pure water with the same mass of silicate in an otherwise isolated seawater sample maintained at constant temperature and pressure. Since silicate is predominantly non-ionic, the conductivity (and therefore Practical Salinity) is unchanged to measurement precision. In contrast, the Absolute Salinity ($S_A$) and density is increased. Similarly, if a small mass of sodium chloride (NaCl) is added and the same mass of silicate is removed, the salinity mass fraction will not have changed (and so the density will also remain near constant) but the Practical Salinity (measured by conductivity) will have increased. The TEOS-10 Reference Composition of sea salt comprises 15 chemical species, of which Cl− and Na+ comprise 55 and 31 % respectively, with $SO_4^{2−}$ and $Mg^{2+}$ the next most abundant species at 7.7 and 3.6 % (Pawlowicz et al., 2016).

While the new TEOS-10 salinities are more representative of the real-world seawater constituents, the observing platforms and techniques currently used to obtain seawater salinity measurements have not changed. 10 This situation has led to TEOS-10 advocating a continuation of the current practice of Practical Salinity (measured through well-defined conduc-
tivity relationships) being the stored quantity in observed oceanographic databases. However, when observed analyses are being undertaken, TEOS-10 recommends that Absolute Salinity, rather than Practical Salinity, be used.

The enhanced treatment of ocean salinity defined by TEOS-10 leads, unfortunately, to a divergence between observed and modelled salinity quantities. Most models that are contributing to CMIP6 are based on pre-TEOS-10 thermodynamics and carry only salinity that approximates the observed quantity of Practical Salinity. Therefore, to facilitate comparisons across models and with observations, salinity comparisons in CMIP6 will be made against Practical Salinity regardless of the model thermodynamics. This practice represents exact correspondence to earlier CMIPs, and reflects the same role of modelled salinity when considering modelled seawater thermodynamics.

**D5 Specification for salt content**

The salt content in a grid cell is not given by the grid cell mass times Practical Salinity. Instead, it is given by the grid cell mass times Absolute Salinity. However, for CMIP6 models the use pre-TEOS-10 thermodynamics, and so consider Practical Salinity as their conserved prognostic salinity, reflecting the same role of modelled salinity when considering modelled seawater thermodynamics.

**Appendix E: Temperature scales and ocean heat content**

Ocean heat content is arbitrary up to specification of the ocean temperature scale. However, the evolution of ocean heat content is invariant when shifting ocean temperature scales, such as when changing from Kelvin to Celsius. To show this property, consider the heat content of the global ocean as written in Appendix A.4 of Griffies et al. (2014):

\[
\mathbf{H} = c_p M \langle \Theta \rangle^\rho. \quad (E1)
\]

In this expression, \(M\) is the total mass of seawater,

\[
\langle \phi \rangle = V^{-1} \int \phi dV \quad (E2)
\]

is the volume mean operator with \(V\) the total ocean volume,

\[
\langle \Theta \rangle^\rho = \langle \rho \Theta \rangle / \langle \rho \rangle \quad (E3)
\]

is the density weighted mean Conservative Temperature, and \(\langle \rho \rangle = M/V\) is the mean ocean density. As discussed in Sect. K1.6, time changes in ocean heat content are affected by non-advective and advective heat fluxes crossing the ocean boundary

\[
\frac{d \mathbf{H}}{dt} = A (\mathbf{Q}_{\text{non-advect}} + \mathbf{Q}_{\text{advect}}). \quad (E4)
\]

In this equation, \(A\) is the surface area of the liquid ocean, \(\mathbf{Q}_{\text{non-advect}}\) comprise the area mean radiative and turbulent heat fluxes, and \(\mathbf{Q}_{\text{advect}}\) is the area mean advective heat flux. The non-advective heat fluxes are determined by the thermodynamic temperature, i.e. Kelvin. Additionally, a portion, \(\mathbf{Q}_{\text{advect}}^{\text{other}}\) of the advective heat flux is generally determined outside of the ocean, for example when the atmosphere or river model transfers the heat content of precipitation or river runoff to the ocean. Another portion of the advective heat flux is determined by the ocean. We write the advective heat flux in the form

\[
\mathbf{Q}_{\text{advect}} = \mathbf{Q}_{\text{advect}}^{\text{other}} + c_p Q^m \Theta^m, \quad (E5)
\]

where \(Q^m\) is that portion of the boundary mass flux whose heat content is determined by the ocean, and \(\Theta^m\) is the Conservative Temperature of the boundary mass flux. In practice, we often approximate \(\Theta^m\) by the surface ocean temperature, but that is not necessary for the present arguments. Bringing these results together leads to the time changes in the heat content

\[
\frac{d \mathbf{H}}{dt} = A (\mathbf{Q}_{\text{non-advect}} + \mathbf{Q}_{\text{advect}}^{\text{other}} + c_p Q^m \Theta^m). \quad (E6)
\]

When Conservative Temperature is measured in Kelvin, the ocean heat content is related to the Celsius heat content by the offset (see the definition of the heat content in Eq. E1)

\[
\Theta^{(K)} = \Theta^{(C)} + c_p A \Theta^{(C2K)}, \quad (E7)
\]

where \(\Theta^{(C2K)} = -273.15\) is the constant offset in the scales. Hence, their time derivatives are related by

\[
\frac{d \mathbf{H}^{(K)}}{dt} = \frac{d \mathbf{H}^{(C)}}{dt} + A c_p Q^m \Theta^{(C2K)}, \quad (E8)
\]

where

\[
\frac{d M}{dt} = A Q^m \quad (E9)
\]

is the time change of the global ocean mass. When the ocean mass is constant, evolution of ocean heat content does not care what temperature scale is used. To show that this result holds in general, without loss of generality assume that the ocean heat budget Eq. (E6) holds when measuring ocean Conservative Temperature in Kelvin, \(\Theta^{(K)}\), so that

\[
\frac{d \mathbf{H}^{(K)}}{dt} = A (\mathbf{Q}_{\text{non-advect}} + \mathbf{Q}_{\text{advect}}^{\text{other}} + c_p Q^m \Theta^m). \quad (E10)
\]

Now shift to the Celsius temperature scale, \(\Theta^{(C)}\), bringing the right-hand side to the form

\[
\frac{d \mathbf{H}^{(K)}}{dt} = A (\mathbf{Q}_{\text{non-advect}} + \mathbf{Q}_{\text{advect}}^{\text{other}} + c_p Q^m \Theta^{(C)} + c_p Q^m \Theta^{(C2K)}). \quad (E11)
\]
Equating the budgets as written by Eqs. (E8) and (E11) then yields the heat content budget using the Celsius scale

\[
\frac{dH(C)}{dt} = A(Q_{\text{non-adveqt}} + Q_{\text{adveqt}}^o + c_p \rho L G(C)). \tag{E12}
\]

As anticipated, the ocean heat budget using the Celsius scale takes the same form as Eq. (E10), which is the budget for ocean heat using the Kelvin temperature scale. We may thus use either temperature scale when analysing ocean heat budgets. For OMIP, it is more convenient to use the Celsius scale, as that is the scale used for prognostic temperature in ocean models.

**Appendix F: Finite volume scalar equations**

In this appendix, we outline a finite volume framework that underlies our requests for heat and salt budget terms in Appendix L. This framework is based on the discretization of budget equations for extensive fluid properties. Extensive properties include scalars such as seawater mass and tracer mass, as well as vectors such as linear momentum. The scalar concentration, \(C\), is an intensive property that measures the mass of a scalar field (e.g. salt) in a region per mass of seawater in that region:

\[
C = \left( \frac{\text{mass of trace matter}}{\text{mass of seawater}} \right). \tag{F1}
\]

Enthalpy (heat) also follows this formalism (McDougall, 2003), where the “heat concentration” is the Conservative Temperature. Note that for a Boussinesq fluid, mass can be replaced by volume through division by the constant Boussinesq temperature. Note that for a Boussinesq fluid, mass can be replaced by volume through division by the constant Boussinesq temperature. It is useful since it provides a means to conserve fluid properties. Extensive properties include scalars such as seawater mass and tracer mass, as well as vectors such as linear momentum. The scalar concentration, \(C\), is an intensive property that measures the mass of a scalar field (e.g. salt) in a region per mass of seawater in that region:

\[
C = \left( \frac{\text{mass of trace matter}}{\text{mass of seawater}} \right). \tag{F1}
\]

In this equation, \(\rho C \delta n \cdot \hat{n}\) is the advective tracer flux penetrating the boundary with outward normal \(\hat{n}\), and \(\delta n\) is the velocity of a parcel relative to the velocity of the boundary. \(\rho F\) is the subgrid-scale tracer flux and \(dA(\hat{n})\) is the area element on the boundary. We ignored tracer sources for brevity, though they can be trivially introduced as needed for biogeochemical tracers. The volume integral is taken over the region, and the area integral is over the region boundary. That component of the flux \(\rho (C \delta n + F)\) that penetrates the bounding surface alters the scalar content within the region.

Now introduce the discrete finite volume fields with discrete label \(J\)

\[
V_J \equiv \iint_{R_J} dV \tag{F3a}
\]

\[
\rho J V_J \equiv \iint_{R_J} \rho dV \tag{F3b}
\]

\[
\rho J C_J V_J \equiv \iint_{R_J} \rho C dV. \tag{F3c}
\]

For our purposes, an ocean model grid cell forms the canonical example of a finite volume. The discrete field \(C_J\) is the mass weighted mean of the continuous tracer concentration, \(C\), over the finite domain; it is not the value of the continuous tracer evaluated at a point. Making use of definitions (F3a)–(F3c) transforms the continuous conservation Eq. (F2) into a discrete form

\[
\frac{\partial (\rho J C_J V_J)}{\partial t} = - \sum_{\partial R_J} (\rho C \delta n + \rho F) \cdot \hat{n} A(\hat{n}). \tag{F4}
\]

Consequently, the continuous flux form scalar equation (F2) is readily transformed to a finite volume spatially dis-
crete scalar equation (F4). Likewise, the discrete mass equation is realized by setting the tracer concentration to unity and dropping the subgrid-scale term
\[
\frac{\partial (\rho_j V_J)}{\partial t} = - \sum_{\delta R_j} \rho \delta n \cdot \hat{n} A(\hat{\delta}). \tag{F5}
\]
The spatially discrete tracer (Eq. F4) and mass (Eq. F5) equations provide the basis for finite volume scalar equations.

F2 Thickness weighting in ocean models

Ocean circulation models generally assume the horizontal area of a grid cell is constant in time. It is only the cell thickness that fluctuates. A time-dependent cell thickness applies to models using generalized level or layer coordinates, such as \( z^* \), \( p^* \), terrain-following, isopycnal, and arbitrary Lagrangian–Eulerian (ALE).\textsuperscript{11} The finite volume method is quite useful for such models, in which we specialize the finite volume expressions (F3a)–(F3c) to thickness-weighted fields

\[
A_J \Delta z_J \equiv \int \int \int_{R_J} dA \int dz, \tag{F6a}
\]
\[
\rho_J A_J \Delta z_J \equiv \int \int \int_{R_J} dA \int \rho dz, \tag{F6b}
\]
\[
\rho_J C_J A_J \Delta z_J \equiv \int \int \int_{R_J} dA \int \rho C dz, \tag{F6c}
\]

where \( A_J \equiv \int \int_{R_J} dA \) is the time-independent horizontal area of the grid cell, and \( \Delta z_J \) is the time-dependent cell thickness. Since the horizontal grid cell area is constant in time, the discrete finite volume tracer budget (Eq. F4) becomes a budget for the mass of tracer per horizontal area in a grid cell
\[
\frac{\partial (\rho J C_J \Delta z_J)}{\partial t} = - \frac{1}{A_J} \sum_{\delta R_j} \left( C \rho \delta n + \rho F \right) \cdot \hat{n} A(\hat{\delta}). \tag{F7}
\]

Likewise, the discrete mass budget for a grid cell, (Eq. F5), becomes an equation for the mass per horizontal area,
\[
\frac{\partial (\rho_J \Delta z_J)}{\partial t} = - \frac{1}{A_J} \sum_{\delta R_j} \rho \delta n \cdot \hat{n} A(\hat{\delta}). \tag{F8}
\]

Again, for a Boussinesq fluid, the in situ density in the scalar equations is replaced by the constant reference density, \( \rho_o \), so that Eq. (F8) becomes the cell thickness equation.

\textsuperscript{11}Boussinesq geopotential rigid-lid models and linear free-surface Boussinesq geopotential models both assume grid cell area and thickness to be time-independent. Finite difference methods are sufficient to formulate the discrete equations for these models.

Vertical cell faces, oriented normal to the horizontal directions \( \hat{x} \) and \( \hat{y} \), have fixed horizontal positions. Hence, the relative velocity \( \delta n \) is just the horizontal velocity so that
\[
\delta n \cdot \hat{x} dA(\hat{\delta}) = u \ dy \ dz \tag{F9a}
\]
\[
\delta n \cdot \hat{y} dA(\hat{\delta}) = v \ dx \ dz. \tag{F9b}
\]

Likewise, for the vertical faces, defined by surfaces of constant vertical coordinate,
\[
\delta n \cdot \hat{n} dA(\hat{\delta}) = w(s) \ dx \ dy, \tag{F10}
\]

where \( w(s) \) is the dia-surface velocity component. If the vertical coordinate is geopotential, then \( w(s) \) is the usual vertical velocity component. If the vertical coordinate is isopycnal, then \( w(s) \) is the diapycnal velocity component. More details are provided in Sect. 6.7 of Griffies (2004) and Sect. 2.2 of Griffies and Adcroft (2008).

F3 Implications for ocean model diagnostics

To conserve mass, ocean models time step the tracer mass per area, \( \rho_J C_J \Delta z_J \), as per Eq. (F7). Furthermore, the time-dependent mass per horizontal area, \( \rho_J \Delta z_J \), is time-stepped through the mass Eq. (F8). With an updated tracer mass per horizontal area, and an updated seawater mass per horizontal area, we can update the tracer concentration via division

\[
C_J = \frac{C_J \rho_J \Delta z_J}{\rho_J \Delta z_J}. \tag{F11}
\]

This update is performed each model time step so as to have access to the tracer concentration at each time step. Tracer concentration is needed, for example, to evaluate the equation of state and freezing point using the salinity (salt concentration), temperature (heat concentration), and pressure. Temperature is also need for computing air–sea fluxes. For OMIP, we therefore request archives for the tracer concentration \( C_J \), with time-averaging performed online each model time step.

To produce regional maps of an extensive quantity such as salt content or heat content, it is necessary to diagnose the mass weighted tracer concentration online to account for temporal correlations between tracer concentration and cell mass. Absent this online calculation, errors are generally unacceptable when working with isopycnal models, where layer thicknesses can vanish. However, experience at GFDL with Boussinesq \( z^* \) models suggests that errors are minor when working offline using time averaged thickness and time averaged tracer concentration. Nonetheless, to help reduce errors for general purposes, in Table L1 we request the mass integrated temperature and salinity fields
\[
\text{opotentmpint} = \sum_k \Theta_k \rho_k \Delta z_k \tag{F12a}
\]
\[
\text{ocontempmint} = \sum_k \Theta_k \rho_k \Delta z_k \tag{F12b}
\]
where $k$ is the vertical cell index and the sum extends over the full ocean depth. Since the grid cell mass per horizontal area is generally time-dependent, the depth integral must be computed online each time step. From this diagnostic, we can compute globally and regionally integrated heat content and salt content. Furthermore, OMIP requests the online calculation of the mass-averaged temperature and salinity (see Table H1 and Sects. H12 and H17):

\[
\text{somint} = \sum_k S_k \rho_k \Delta z_k, \quad \text{(F12c)}
\]

Many ocean climate models employ the Boussinesq approximation, in which there appears a constant reference density $\rho_o$ within budgets for tracer and momentum, and volume is conserved rather than mass. It is useful to have an archive of this constant for CMIP6.

As noted on page 47 of Gill (1982), with the exception of only a small percentage of the ocean, in situ density in the World Ocean varies by no more than 2% from 1035 kg m\(^{-3}\). Hence, $\rho_o = 1035$ kg m\(^{-3}\) is a sensible choice for the reference density used in a Boussinesq ocean climate model. However, some models use a different value. For example, early versions of the GFDL ocean model (Cox, 1984) set $\rho_o = 1000$ kg m\(^{-3}\). Others choose the average density corresponding to the thermocline region. Roquet et al. (2015) present a summary of various choices.

### G4 Seawater heat capacity

\[ c_{p}ocean \]

As detailed in McDougall (2003) and IOC et al. (2010), the heat capacity of seawater is a constant when measuring the heat content of a parcel in terms of Conservative Temperature. As discussed in Appendix D, not all models choose to use Conservative Temperature as their prognostic heat variable. However, all ocean models use a constant heat capacity, $c_{p}ocean$, to convert between prognostic model temperature and heat content, though not all models use the TEOS-10 value for heat capacity (see Eq. D3 in Sect. D3). Hence, to enable accurate comparisons between ocean model heat contents, we ask that all models archive their choice for the constant seawater heat capacity.

A useful method for archiving this constant is to include it as part of the metadata for the potential temperature or Conservative Temperature diagnostic (Appendices H10 and H11), as well as for all heat-related diagnostics (e.g. boundary heat fluxes in Table K3 and heat budget terms in Table L1). Doing so will facilitate computation of ocean heat content, consistent with how the model converts boundary enthalpy fluxes into temperature tendencies.

### G5 Bathymetry

\[ \text{deptho} \]

For global primitive equation ocean models, the geoid is assumed to correspond to the geopotential surface $z = 0$. The distance from $z = 0$ to the ocean bottom defines the ocean depth field, $H(x, y)$, or the ocean bathymetry, and the vertical position of the bottom is

\[ z = -H(x, y). \quad \text{(G1)} \]

This solid earth boundary used by the model should be archived. Precisely, the bathymetry representing the ocean bottom from the perspective of the model tracer fields defines the field deptho.
Table G1. Static fields and functions to be saved for the ocean model component in CMIP6, as well as how the CMOR name for a diagnostic is related to its CF standard name. These fields provide basic information about the model configuration, and need only be archived once for all the model experiments in the CMIP6 repository (hence the “once” entry for the experiment column). Blank entries signal a characteristic that is not applicable for this particular diagnostic. Furthermore, the bottom topography, grid length and areas, and basin regions should be made available on both the model native grid and on the spherical latitude–longitude grid onto which scalars are regridded. The entry for masscello applies only to Boussinesq models with static grid cell volumes (Appendix B). For other kinds of models, masscello is generally time-dependent and the entry in Table H1 applies instead.

<table>
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<th>Item</th>
<th>CMOR name</th>
<th>Sponsor</th>
<th>CMIP5/CMIP6</th>
<th>Units</th>
<th>Time</th>
<th>Shape</th>
<th>Grid</th>
<th>Priority</th>
<th>expt</th>
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<tbody>
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<td>1</td>
<td>Equation of state</td>
<td>OMIP</td>
<td>same</td>
<td>$\rho(S, \Theta, p)$ or $\rho(S, \Theta, z)$</td>
<td>static</td>
<td>0</td>
<td>0</td>
<td>native/sphere</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>Freezing point</td>
<td>OMIP</td>
<td>same</td>
<td>function of $(S, p)$ or $(S, z)$</td>
<td>static</td>
<td>0</td>
<td>0</td>
<td>native/sphere</td>
<td>1</td>
</tr>
<tr>
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<td>XYZ</td>
<td>native/sphere, z/p</td>
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If the lateral area for exchange of fluid between columns (e.g. mass transport) is anything other than a simple function of the tracer column depths, then the modulated areas affecting the exchange are useful to archive (Adcroft, 2013). For example, this additional information is necessary for models that allow a strait to be more narrow than the nominal width of the cell. However, at this time there is no OMIP specification for this area.

G6 Tracer region masks

- basin

Analysis of budgets and properties over ocean basins is commonly performed for the purpose of assessing the integrity of simulations. This analysis generally involves the use of a mask that partitions the model grid into ocean basins (some enclosed seas may be missing from the model). We recommend the following ocean regions, with the names corresponding to standard CF basin names found at http://cfconventions.org/

1. southern_ocean
2. atlantic_ocean
3. pacific_ocean
4. arctic_ocean
5. indian_ocean
6. mediterranean_sea
7. black_sea
8. hudson_bay
9. baltic_sea
10. red_sea

These region masks are set according to the following flag_values and flag_meanings, which should be recorded as attributes of the variable:

- flag_values = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10
- flag_meanings="southern_ocean, atlantic_ocean, pacific_ocean, arctic_ocean, indian_ocean, mediterranean_sea, black_sea, hudson_bay, baltic_sea, red_sea"

For some grid staggering, the tracer mask differs from the velocity mask, in which case a mask for the velocity cells should be provided to the CMIP6 archive as a distinct output variable, with the same standard name of region. The two variables are distinguished in netCDF by their coordinates, one being on the tracer grid and the other on the velocity grid.
G7 Horizontal area of a tracer cell

- areacello

The static field areacello provides a measure (in m$^2$) of the horizontal area for a tracer cell. This field should be zero or missing over land. More details for areacello are provided in Appendix B.

G8 Mass of a grid cell for Boussinesq models with static cell volumes

- masscello

The three-dimensional masscello field measures the mass per horizontal area of a grid cell. As discussed in Sect. B1, some volume-conserving Boussinesq models maintain static cell volumes, in which case masscello should be reported as part of the Table G1 request. Otherwise, the mass of a grid cell is time-dependent and so should be reported as in Sect. H3.

G9 Extra grid information to facilitate regridding

As per the area discussion in Sect. A3.2, the paper from Balaji et al. (2016) provides guidance for area factors facilitating the regridding of fields from the native grids to the sphere.

Appendix H: Diagnostics involving scalar fields

In this appendix, we present specifications for the scalar fields to be archived as part of CMIP6, with a summary in Table H1.

H1 Pressure at ocean bottom

- pbo

The bottom pressure in a hydrostatic ocean is given by the gravitational acceleration acting on the mass per area of a fluid column, plus any pressure applied at the ocean surface from the overlying atmosphere or ice.$^{12}$ In a discrete model, pbo is given by the vertical sum over the levels/layers in the column

$$p_b = p_a + g \sum \rho \, dz \quad \text{(H1)}$$

where $p_a$ is the pressure applied at the ocean surface (pso discussed in Sect. H2), and we assumed a constant gravitational acceleration.$^{13}$ Hence, $g^{-1}(p_b - p_a)$ is the mass per horizontal area of a fluid column. The bottom pressure is a prognostic field in non-Boussinesq hydrostatic models, whereas it is diagnosed in Boussinesq hydrostatic models. Anomalies of bottom pressure with respect to a suitable reference value, such as $\rho_o g H$, provide a means for measuring mass adjustments throughout the water column.

If the model is Boussinesq (very common), then an adjustment must be made to account for spurious mass sources in the Boussinesq fluid. In particular, if interested in the mass distribution of seawater, as needed for angular momentum (Bryan, 1997), bottom pressure (Ponte, 1999), or geoid perturbations (Kopp et al., 2010), one must account for this spurious mass change that arises due to the oceanic Boussinesq approximation. Details for how to compute these adjustments are provided in Sect. D.3.3 of Griffies and Greatbatch (2012). Please make a note in the meta-data whether an adjustment has been made to correct for the Boussinesq error.

H2 Pressure applied to the ocean surface

- pso

The pressure applied to the ocean surface from the overlying atmosphere is often neglected in climate simulations, in which case it should not be included in the diagnostic pso. However, models that incorporate this effect offer the means to simulate the inverse barometer response of the sea surface and deviations thereof (for a review of the basics, see Wunsch and Stammer, 1998, as well as Appendix C in Griffies and Greatbatch, 2012). Changes in atmospheric pressure present a rapid barotropic forcing to the ocean (Arbic, 2005; Ponte, 2006). Additionally, changes in the distribution of mass in the atmosphere can lead to noticeable changes in regional sea level (e.g. Goddard et al., 2015).

In addition to atmospheric mass impacting on the ocean, there is mass from overlying sea ice, ice shelves, and icebergs. If the ocean model feels this mass through undulations of its free surface, then the mass per area should be included in pso.

Note that solid runoff is defined as all frozen water that enters the ocean from land, such as from snow and land ice, lake ice, and river ice. For example, snow can enter in its frozen state when a land model has a buffer layer of a certain thickness, with all snow exceeding this buffer conveyed to the ocean. Land ice can enter the ocean as icebergs resulting from an ice sheet/shelf model or formed from snow excess (e.g. Jongma et al., 2009; Martin and Adcroft, 2010; Marsh et al., 2015). There is no increase in liquid ocean water until the solid runoff melts. However, the presence of solid ice affects the pressure felt within the liquid ocean column, and affects the heat budget of the ocean through the latent heat of fusion.$^{13}$

$^{12}$If the model is non-hydrostatic, the bottom pressure is affected by the mass per area of the ocean fluid, plus non-hydrostatic fluctuations in the pressure field. Non-hydrostatic dynamics become important for the ocean at spatial scales finer than roughly 100 m (e.g. Marshall et al., 1997). These grid scales are finer than any ocean model used for CMIP6, and hence all CMIP6 ocean models are hydrostatic.

$^{13}$All CMIP6 simulations assume a constant gravitational acceleration, $g$, with a value at or near 9.8 m s$^{-2}$. 

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Table H1. Scalar fields to be saved from the ocean component in CMIP6 ocean model simulations. Entries with grids denoted “native/sphere” denote diagnostics where native and spherical output are recommended to facilitate analysis (see discussion in Sect. A3). The column indicating the experiment for saving the diagnostics generally says “all”, in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCP, Scenario-oMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations. The Priority = 1 diagnostics should be saved as decadal time means at decadal intervals for the piControl spin-up. Blank entries signal a characteristic that is not applicable for this particular diagnostic. Squared diagnostics are computed online by accumulating each time step, so that they can be useful for computing variance fields. The entry for masscello applies for models with time-dependent cell masses (Appendix B). For Boussinesq models with static grid cell volumes, the entry in Table G1 applies instead. The variables bigthetao and bigthetaoga are requested only for models enacting the TEOS-10 Conservative Temperature field as a prognostic model variable (see Sect. H12 and Appendix D). The lower sub-table lists the CMOR names and their corresponding CF standard names.

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In rigid-lid ocean models, the term "surface pressure" refers to the hydrostatic pressure at \( z = 0 \) associated with the layer of liquid water between \( z = 0 \) and \( z = \eta \) (Pinardi et al., 1995). This pressure is also sometimes referred to as the "lid pressure." It can be positive or negative, depending on whether the free surface, \( \eta \), is positive or negative. This "surface pressure" field is distinctly not what we refer to here by \( \text{ps} \). Instead, \( \text{ps} \) records the non-negative pressure applied at \( z = \eta \) due to media above the ocean surface interface. Such pressure may be set to zero in some approximate model formulations, such as the rigid lid, in which case the ocean pressure is not influenced by movement of mass outside the liquid ocean.

**H3 Mass per area of grid cell**

- masscello: cell mass per unit horizontal area

To estimate tracer budgets offline, we require the mass per horizontal area of seawater in the grid cell

\[
\text{masscello} = \rho d_z, \tag{H2}
\]

with units of kg m\(^{-2}\). For a hydrostatic model, the mass per area is proportional to the pressure increment \( dp \) according to \( dp = -g \rho d_z \), so that

\[
\text{masscello} = -g^{-1} dp \quad \text{hydrostatic}. \tag{H3}
\]

For a Boussinesq model, the in situ density factor, \( \rho \), in Eq. (H2) is set to the constant reference density, \( \rho_o \), so that

\[
\text{masscello} = \rho_o d_z \quad \text{hydrostatic / Boussinesq}. \tag{H4}
\]

in which case the mass per area is equivalent to \( \rho_o \) times the grid cell thickness (Sect. H4).

**H4 Thickness (i.e. volume per area) of grid cells**

- thkcello: cell volume per unit horizontal area

The tracer cell thickness

\[
\text{thkcello} = d_z \tag{H5}
\]

measures the distance (in metres) between surfaces of constant vertical coordinates. This information is useful, for example, when measuring changes in thickness between pressure surfaces in a non-Boussinesq pressure-based model exposed to increasing anthropogenic warming (i.e. steric effect).

**H5 Total mass of liquid seawater**

- masso

This diagnostic is the global sum of the grid cell area (area-cello in Sect. G7) multiplied by the cell mass per area (mass-cello in Sect. H3). For the purpose of global budgets in non-Boussinesq models, it is essential to have the total mass of liquid seawater in the ocean domain. This scalar field includes all seawater contained in the liquid ocean, including any enclosed seas that are part of the ocean model integration. As a discrete sum of the three-dimensional grid cells, masso is given by

\[
\text{masso} = M = \sum_{i,j,k} \rho dA dz \quad \text{non-Boussinesq}, \tag{H6}
\]

with \( \rho \) the in situ density,

\[
dA = dx \, dy \tag{H7}
\]

the horizontal area of a grid cell, and \( dz \) the vertical thickness. For a hydrostatic fluid, \( dp = -g \rho d_z \) so that the total seawater mass in a non-Boussinesq model is given by

\[
\text{masso} = -g^{-1} \sum_{i,j,k} dA \, dp \quad \text{hydrostatic non-Boussinesq}. \tag{H8}
\]

For a Boussinesq model, the density factor in Eq. (H6) becomes a constant, \( \rho_o \), so that the net mass is given by

\[
\text{masso} = \sum_{i,j,k} \rho_o dA dz \quad \text{Boussinesq}, \tag{H9}
\]

in which case the mass is equal to \( \rho_o \) times the total volume of liquid in the ocean (Sect. H6).

**H5.1 Summary of the diagnostic**

**H5.2 Theoretical considerations**

In a non-Boussinesq ocean, the total mass of liquid seawater evolves according to the budget

\[
\frac{dM}{dt} = \sum_{i,j} Q^m dA, \tag{H10}
\]

where \( Q^m \) (kg m\(^{-2}\) s\(^{-1}\)) is the net mass per time transported across the liquid ocean boundaries, per horizontal cross-sectional area. The transport arises from evaporation, precipitation, runoff, and material tracers such as salt. Maintenance of this mass budget is a fundamental feature of a conservative non-Boussinesq ocean model.

**H6 Total volume of liquid seawater**

- volo

\(^{14}\)CMIP6 ocean models do not generally add or remove mass associated with the transfer of material tracers across the ocean surface.
This diagnostic measures the sum of the three-dimensional tracer grid cell volumes
\[ \text{volo} = V = \sum_{i,j,k} dA_z. \] (H11)

It is computed as the global sum of the product of the grid cell horizontal area (\( \text{areacello} \) in Sect. G7) and the grid cell thickness (\( \text{thkcello} \) in Sect. H4).

In a Boussinesq fluid, volo evolves according to the budget
\[ \frac{dV_{\text{Bouss}}}{dt} = \frac{1}{\rho_o} \sum_{i,j} Q^m dA. \] (H12)

Maintenance of this volume budget is a fundamental feature of a conservative Boussinesq ocean model. In particular, if there are no net boundary fluxes of volume, then a conservative Boussinesq model will retain a constant total volume to within computational roundoff.

In contrast, a non-Boussinesq model will generally alter its volume in cases even with zero boundary mass fluxes, since non-Boussinesq models conserve mass rather than volume. Hence, the non-Boussinesq model’s total volume changes through changes in the ocean mass (barystatic effects) (Gregory et al., 2013), and changes in global mean ocean density (steric effects) (Griffies and Greatbatch, 2012).

H7 Dynamic sea level

- zos

By definition, this diagnostic field has a zero global area mean, so that it measures sea level pattern fluctuations around the ocean geoid defined via a resting ocean state at \( z = 0 \). That is, zos is the dynamic sea level as defined in Griffies and Greatbatch (2012) or Griffies et al. (2014). The dynamic sea level reflects fluctuations due to ocean dynamics. Consequently, this diagnostic is not used to map the global mean sea level changes due to thermal expansion or changes in ocean mass. Rather, global mean changes due to thermosteric effects are removed from zos, and are instead archived in zostoga (Sect. H9). In the following, we identify various technical points regarding the dynamic sea level diagnostic.

H7.1 Non-Boussinesq vs. Boussinesq

Non-Boussinesq models incorporate global steric effects contributing to sea level changes, such as those related to thermal expansion. In contrast, the prognostic sea surface height in Boussinesq models does not incorporate global steric effects (Greatbatch, 1994). When removing the global mean, sea level patterns from Boussinesq and non-Boussinesq models are directly comparable (Losch et al., 2004; Griffies and Greatbatch, 2012).

H7.2 Algorithm for computing sea surface height

It should be noted in the “comment” attribute whether zos is obtained directly, as in a free-surface model, or diagonstically derived. Diagnostic methods can follow from assuming velocities are geostrophic at some level, or from geostrophy relative to an assumed level of quiescence. Gregory et al. (2001) summarizes various methods of estimating sea level in rigid-lid models. Notably, these methods are largely obsolete, since CMIP6 ocean models generally do not make the rigid-lid approximation.

H7.3 Inverse barometer from sea-ice loading

In some coupled climate models, sea ice (and snow on top of the ice) depresses the liquid seawater through mass loading (appearing as an applied surface pressure on the ocean model as discussed in Sect. H2). This depression occurs independently of the subgrid-scale distribution of sea ice, as it is a result of the mass of sea ice (and snow) in a grid cell acting on the liquid ocean. There is, however, no dynamical effect associated with these depressions in the liquid ocean sea level, so there are no associated ocean currents. See Appendix C in Griffies and Greatbatch (2012) for a discussion of this inverse barometer effect from sea ice.

- For OMIP, do not record inverse barometer responses from sea-ice (and snow) loading in zos. Rather, zos is the effective sea level as if sea ice (and snow) at a grid cell were converted to liquid seawater (Campin et al., 2008).

- A means to measure the effective dynamic sea level is to remove the inverse barometer response to applied pressure loading on the ocean from sea ice and snow (e.g. see Eq. 206 of Griffies and Greatbatch, 2012):

\[
\eta_{\text{effective}} = \eta_{\text{model}} + \frac{p_{\text{ice/snow loading}}}{g \rho_{\text{surf}}}. \] (H13)

In this equation, \( \eta_{\text{model}} \) is the sea level computed by the ocean model, \( p_{\text{ice/snow loading}}/g \) is the mass per unit area of the applied surface loading on the ocean, and \( \rho_{\text{surf}} \) is the surface ocean density.\(^{15}\) For OMIP purposes, the surface ocean density can be approximated by a constant \( \rho_o \).

- The term \( p_{\text{ice/snow loading}}/(g \rho_{\text{surf}}) \) in Eq. (H13) acts to remove the sea-ice and snow loading inverse barometer response contained in \( \eta_{\text{model}} \). Thereafter, we normalize to zero (global area integral vanishes) to render the dynamic sea level archived for OMIP:

\[
\eta_{\text{omip}} = \eta_{\text{effective}} \left( \frac{\sum_{i,j} \eta_{\text{effective}} dA}{\sum_{i,j} dA} \right). \] (H14)

\(^{15}\) Note that \( p_{\text{ice loading}} = 0 \) for models that do not depress the sea surface under the weight of sea ice.
It is the dynamic sea level, $\eta_{\text{omip}}$, that should be reported in $zos$.

**H7.4 Inverse barometer from atmospheric loading**

The inverse barometer response of sea level arising from atmospheric loading has, for many applications on long timescales, minimal dynamical impact (Wunsch and Stammer, 1997). Indeed, most, if not all, ocean components of CMIP models ignore the atmospheric loading on the ocean (see Arbic, 2005, for an exception).

- For those models that do apply atmospheric loading, and thus have an inverse barometer response in $\eta_{\text{model}}$, we request that such loading remain part of the dynamic sea level archived in CMIP. That is, the dynamic sea level will be depressed or raised according to the weight of the atmosphere. We thus do not remove the inverse barometer from atmospheric loading. This treatment for the atmosphere loading contrasts with the recommendation for sea-ice loading detailed in Sect. H7.3.

- If the ocean model feels the effects from the applied atmospheric forcing, then include this fact in the “comments” section for $zos$.

- The key point is that the global area integral of dynamic sea level, $zos$, should be zero, even if the ocean model feels the weight of the atmosphere.

**H8 Squared dynamic sea level**

- $zossq$

The field $zossq$ is the square of the dynamic sea level and accumulated each model time step. This quadratic quantity helps to measure the variability simulated in the dynamic sea level by computing the variance. For that purpose, we can make use of the following identity

$$\text{Var}(zos) = \frac{1}{T} \int_{-T/2}^{T/2} (zos - \overline{zos})^2 \, dt$$

\[(H15a)\]

$$= zossq - (\overline{zos})^2,$$

\[(H15b)\]

where $T$ is the time interval for the time average, and $\overline{zos}$ is the time mean dynamic sea level.

**H9 Global thermosteric sea level changes**

- $zostoga$

The potential for increased sea level due to anthropogenic climate change presents some of the most pressing issues for adaptation to a warmer world (Church et al., 2011, 2013a; Gregory et al., 2013). Sea level changes also provide a baseline assessment of the changing ocean climate in the simulations (Yin et al., 2010a; Yin, 2012; Kuhlbrodt and Gregory, 2012). It is thus of primary importance to consider the effects from sea level rise as simulated in the CMIP models. Results from model simulations should be carefully documented in order to properly interpret the CMIP archive.

There are three main reasons for global mean sea level to increase. First, thermal expansion arises due to the warming ocean (thermosteric change). Second, changes in the mass of seawater in the ocean affect an increase in ocean volume (barystatic change). Third, global halosteric effects alter global mean sea level, though they are far smaller than either thermosteric or barystatic changes (see Fig. 36 in Griffies et al., 2014, and the discussion in Durack et al., 2014a). We now explain how CMIP aims to diagnose these effects in climate models.

**H9.1 Changes in ocean mass**

The mass effect on sea level arises most importantly from increasing melt of glaciers and ice caps. These changes are registered by changes in the bottom pressure (pbo in Sect. H1) and ocean mass (masscello in Sect. H3). However, we conjecture that most CMIP6-based global climate models will have unreliable values for these contributions. The reason is that CMIP6 climate models generally do not include interactive and evolving land glacier and ice sheet models. More reliable estimates for mass effects come from specialized process-based models using CMIP scenarios as input (for example, see Church et al., 2013c). Hence, changes to global sea level due to changes in ocean mass (barystatic sea level change) are not requested from standard CMIP6 climate and earth system models. The Ice Sheet Model Intercomparison Project (ISMIP6) contribution to CMIP6 (Nowicki et al., 2016) aims to advance our ability to model such effects for climate, thus enhancing our confidence in estimates of barystatic sea level change.

**H9.2 Global halosteric changes**

There is no significant global mean sea level rise from changes in salinity. The reason is that the global halosteric effect is tiny in comparison to the global thermosteric effect (see Griffies and Greatbatch (2012) for discussion and Fig. 36 of Griffies et al., 2014).\(^{16}\) Furthermore, global mean sea level changes from the global halosteric effect in a CMIP simulation are associated with inaccurate estimates of ocean mass changes in these models (see Sect. H9.1). In general, the global halosteric effect is a small fraction of the volume change that results from adding freshwater to the ocean (Munk, 2003; Lowe and Gregory, 2006; Wunsch et al., 2007).

\(^{16}\)Regionally, halosteric effects can be sizable, as recently discussed for models by Griffies et al. (2014) and for observations by Durack et al. (2014b).

www.geosci-model-dev.net/9/3231/2016/
H9.3 Global thermosteric changes

Thermal expansion of seawater accounts for roughly one-third to one-half of the observed global mean sea level rise in the 20th and early 21st centuries (Church et al., 2011, 2013a; Gregory et al., 2013; Hanna et al., 2013). Measuring the thermal expansion from CMIP simulations is thus of primary importance.

H9.4 As compared to the CMIP5 request

For the reasons noted above, CMIP6 does not ask for the following CMIP5 diagnostics:
- global_average_sea_level_change = zosga
- global_average_steric_sea_level_change = zoss ga

Rather, only the diagnostic zostoga, measuring global thermal expansion, is requested for CMIP6.

H9.5 Theoretical considerations

To understand the basics of how the global mean sea level changes, we summarize some salient points from Sect. 4.5 of Griffies and Greatbatch (2012). Here, we consider the relation between the total mass of liquid seawater, total volume of seawater, and global mean seawater density,

\[ \mathcal{M} = V(\rho), \quad \langle \rho \rangle = \frac{\sum \rho \, dA \, dz}{\sum dA \, dz} = \frac{\mathcal{M}}{V}. \]  

\[ \langle \rho \rangle = \frac{\sum \rho \, dA \, dz}{\sum dA \, dz} = \frac{\mathcal{M}}{V}. \]  

Temporally changes in total ocean mass are affected by a nonzero net mass flux through the ocean boundaries (Eq. H10)

\[ \frac{dM}{dt} = AQ^m \]  

where \( Q^m \) is the mass crossing the ocean surface (the diagnostic wfo in Sect. K2),

\[ \bar{Q}^m = A^{-1} \sum Q^m \, dA \]  

is the global mean mass per horizontal area per time of water crossing the ocean boundaries, with

\[ \mathcal{A} = \sum dA \]  

For an ocean with a constant horizontal area (i.e. no wetting and drying, as is the case for typical CMIP models), then temporal changes in the ocean volume are associated with sea level changes via

\[ \frac{dV}{dr} = \mathcal{A} \frac{d\eta}{dr}, \]  

where

\[ \eta = A^{-1} \sum \eta \, dA \]  

is the global mean sea level.\(^{17} \) Bringing these results together leads to the evolution equation for the global mean sea level

\[ \frac{d\eta}{dr} = \frac{\bar{Q}^m}{\langle \rho \rangle} \left( \frac{V}{A} \right) \frac{\Delta \langle \rho \rangle}{\langle \rho \rangle}. \]  

The first term in Eq. (H23) alters sea level by adding or subtracting mass from the ocean (barystatic effects; Gregory et al., 2013). The second term arises from temporal changes in the global mean density (steric effects; Griffies and Greatbatch, 2012).

We can approximate each of the terms in Eq. (H23) over a finite time \( \Delta t \) via

\[ \Delta \eta \approx \frac{\bar{Q}^m \Delta t}{\langle \rho \rangle} \left( \frac{V}{A} \right) \frac{\Delta \langle \rho \rangle}{\langle \rho \rangle}. \]  

where the \( \Delta \) operator is a finite difference over the time step of interest. The global steric term is defined by

\[ S = -\left( \frac{V}{A} \right) \frac{\Delta \langle \rho \rangle}{\langle \rho \rangle}. \]  

It is straightforward to diagnose from a model simulation, given temporal changes in the global mean density. Note that this diagnostic is relevant for both Boussinesq and non-Boussinesq ocean simulations, as it depends only on changes in the in situ density.

For CMIP, we are interested in the change in sea level in a global warming scenario experiment, with respect to a reference state defined by the initial conditions of the experiment. In this case, the steric term at a time \( n \) is given by

\[ S = -\left( \frac{V^0}{A} \right) \left( \frac{\rho^n - \rho^0}{\rho^0} \right) = \left( \frac{V^0}{A} \right) \left( 1 - \frac{\rho^n}{\rho^0} \right), \]  

where \( \rho^0 = \rho(\theta^0, S^0, p^0) \) is the in situ density for a grid cell as determined by the grid cell’s reference temperature, reference salinity, and reference pressure; \( \rho^n = \rho(\theta^n, S^n, p^n) \)

\(^{17} \)Contrary to the dynamic sea level \( \eta_{omip} \) considered in Sect. H7, we are interested here in evolution of the global mean of the sea level \( \eta \) with this global mean distinctly nonzero due to global steric effects.
is the in situ density at time step $n$; and $\gamma^0$ is the reference global volume of seawater.

As stated earlier, we are most interested in the global steric changes from CMIP models associated with changes in liquid ocean temperature. These thermosteric effects are recorded in zostoga, which represents that part of the global mean sea level change due to changes in ocean density arising just from changes in temperature. We can estimate this thermosteric effect via

$$S_{\text{thermo}} = \left(\frac{\gamma^0}{A}\right) \left(1 - \frac{\langle \rho(n, S^0, p^0) \rangle}{\langle \rho^0 \rangle}\right). \tag{H27}$$

That is, the ocean density in the numerator is computed as a function of the time evolving potential temperature (or Conservative Temperature), with salinity and pressure held constant at their reference value.

We emphasize that Eq. (H27) only involves properties of the liquid ocean due to ocean density changes associated with temperature changes. These temperature changes arise from any number of processes, including the melting of ice as discussed by Jenkins and Holland (2007).

### H9.6 Specifying the global thermosteric changes

To compute the global mean thermosteric sea level changes, we need to specify a reference state, as per Eq. (H27).

- For OMIP simulations (global ocean/sea-ice models), we recommend the reference state be the first year of the fifth forcing cycle. As a comparison, note that Figure 3 of Griffies et al. (2014) shows the global steric rise over five cycles of forcing. The thermosteric rise will be quite close to the steric rise for this simulation.

- For coupled model historical or double CO$_2$ simulations, we recommend the reference state be the first year of the simulation, which is generally taken at the end of a spin-up phase.

### H10 Potential temperature of liquid seawater

#### thetao

The three-dimensional monthly mean potential temperature should be archived, where the reference pressure is at the ocean surface.

Recommendations from IOC et al. (2010) promote the alternative Conservative Temperature to measure ocean heat. Conservative Temperature is the potential enthalpy divided by a reference heat capacity (Appendix D). Conservative Temperature is far more conservative than potential temperature, and so provides a solid foundation for prognosing heat movement in the ocean. However, as discussed in Appendix D, for comparison to other models and to observational data, as well as to previous CMIPs, we recommend that ocean components in CMIP6 archive potential temperature thetao, regardless whether the models consider this field as prognostic, or as diagnostic (when Conservative Temperature is prognostic).

#### H11 Conservative Temperature of liquid seawater

- bighetetao

For models that make use of the TEOS-10 Conservative Temperature as their prognostic field (Appendix D), they should archive the Conservative Temperature. Doing so will allow for meaningful comparison across CMIP6 with future CMIPs, which will predominantly use Conservative Temperature.

### H12 Global mean ocean temperature

#### thetaoga

- bighetetaoga

In addition to the three-dimensional field of potential temperature, we ask CMIP6 models to archive the global mean potential temperature. Models enacting TEOS-10 (Appendix D) should archive both thetaoga and bighetetaoga. These global mean time series provide a measure of the model drift and reflect on the net heating at the ocean boundaries (see below).

### H12.1 Summary of the diagnostic

For potential temperature, its global mean has the same standard name as the three-dimensional potential temperature, but is distinguished by the cell methods attribute (area and depth mean). For Conservative Temperature, its global mean is requested just for those models enabling the TEOS-10 thermodynamics.

The calculation of global mean prognostic temperature differs depending on the use of Boussinesq or non-Boussinesq ocean equations. In a non-Boussinesq model, the mean is given by the mass weighted mean

$$\langle T \rangle_{\text{non-Bouss}} = \frac{\sum_{i,j,k} T \, dA \, dz}{\sum_{i,j,k} \rho \, dA \, dz}, \tag{H28}$$

where $T$ is the model potential temperature, $\theta$, or Conservative Temperature, $\Theta$. In a Boussinesq model, the mean is computed as the volume weighted mean

$$\langle T \rangle_{\text{Bouss}} = \frac{\sum_{i,j,k} T \, dA \, dz}{\sum_{i,j,k} dA \, dz}. \tag{H29}$$

The distinction between non-Boussinesq and Boussinesq models arises from the differences in the underlying conserved fields in the two model formulations. For both cases, it is necessary to accumulate each model time step when producing the time mean, since the mean is built from the product of time-dependent terms (e.g. density and grid cell thicknesses are generally time-dependent).
The time series of the global mean prognostic temperature provides a measure of simulation drift, as well as low-frequency variability. Furthermore, as discussed next, when combined with the boundary fluxes and total mass/volume, one can diagnose the degree to which the ocean model conserves heat.

H12.2 Theoretical considerations

According to the results of Griffies et al. (2009b) and Griffies et al. (2014), one should not assume that all ocean models are written with numerical methods that ensure the conservation of scalar fields such as mass, heat, and salt. One means to check for heat conservation is to compute the change in total heat over a specified time (say over a year) and compare that change to the total boundary heat input to the ocean system. The change in heat should agree with the heat input through the boundaries, with agreement to within computational roundoff expected from a conservative model. See Appendix F for discussion of this point in the context of finite volume scalar budgets.

If there is a difference greater than computational roundoff, then how significant is the difference? To answer this question, consider an order of magnitude calculation to determine the temperature trend that one may expect, given a nonzero net heat flux through the ocean boundaries. For simplicity, assume a Boussinesq fluid with constant volume (i.e. no net volume fluxes), and assume the model prognostic field is potential temperature. The global mean liquid ocean potential temperature evolves according to

\[
\frac{\langle V \rho_o c_p^o \theta \rangle}{\Delta t} = A \bar{Q}^H, \tag{H30}
\]

where \( \bar{Q}^H = A^{-1} \sum_i Q^H dA \) is the global average boundary heat flux. Typical values for the World Ocean yield \( V \rho_o c_p^o \approx 5.4 \times 10^{24} J \degree C^{-1} \) and \( A = 3.6 \times 10^{14} m^2 \), leading to the decadal-scale potential temperature trend

\[
\frac{\Delta \langle \theta \rangle}{\text{decade}} \approx 0.02 \bar{Q}^H. \tag{H31}
\]

For example, with a 1 W m\(^{-2}\) ocean area average heating of the ocean over the course of a decade,\(^{18}\) we expect a global mean temperature trend of roughly 0.02 \degree C per decade, or 0.2 \degree C per century. If there is an error in the balance (H30), we may define a global mean heat flux:

\[
Q^{\text{error}} = \bar{Q}^H - \left( \frac{\langle V \rho_o c_p^o \theta \rangle}{A} \right) \frac{d\langle \theta \rangle}{dt}. \tag{H32}
\]

To translate the error in the net heating into an error in the temperature trend, use relation (H31) to define

\[
\frac{\Delta \langle \theta \rangle^{\text{error}}}{\text{decade}} \approx 0.02 Q^{\text{error}}. \tag{H33}
\]

H13 Monthly mean SST of liquid water

- \( \text{tos} \)
- \( \text{tosga} \)

In the CMIP archive, it is quite valuable to have the full three-dimensional fields, such as potential temperature and salinity. However, for many purposes, just the top model fields are sufficient. The SST (sea surface temperature) field is archived as \( \text{tos} \), and its global area average is \( \text{tosga} \)

\[
\text{tosga} = \frac{\sum_i \theta_{i,j,k=1} dA}{\sum_i dA}. \tag{H34}
\]

We offer the following points to clarify the SST archived from OMIP simulations.

- SST (\( \text{tos} \)) is the interface temperature at the upper boundary of the ocean. In regions of open ocean, SST recorded for CMIP is the temperature used by the model to calculate the sensible heat transfer between the ocean surface and air above, and to compute upwelling longwave radiation at the surface. If the ocean is covered with sea ice, \( \text{tos} \) is the temperature just below the sea ice (used to calculate heat conduction between the two media). In regions of open ocean the “surface_temperature” will be the same as “sea_surface_temperature”. However, in the presence of sea ice the two will generally differ. In nearly all ocean climate models, the surface temperature is given by the prognostic temperature in the upper-most ocean grid cell.

- Surface tracer fields produced from a climate model generally do not correspond to skin properties. Rather, they are bulk properties averaged over the top grid cell, which is generally no less than a metre thick (Large and Caron, 2015).

- Since the potential temperature is referenced to 0 gauge pressure, the surface potential temperature is the same as surface in situ temperature.

- SST is the surface model value for potential temperature, which is distinct from the surface value of Conservative Temperature (IOC et al., 2010).
H14 Daily mean SST of liquid water

- tos

We recommend that daily mean SST be saved for the purpose of computing space-time diagrams to diagnose propagating signals, such as Tropical Instability Waves. The daily mean SST is also useful for understanding the potential for enhanced coral bleaching in a warming world. Remotely sensed estimates of coral bleaching have converged on a measure based on degree-heating weeks (Strong et al., 2004). Quantifying this measure in models requires an archive of daily mean sea surface temperatures.

H15 Daily and monthly mean squared SST of liquid water

The quadratic field

- tossq

is accumulated each model time step. It is requested to help measure the variability simulated in the sea surface temperature, so that one may compute the variance (see Sect. H8 for sea level variance).

H16 Bottom potential temperature

- tob

For studies of impacts on ecosystem from climate change, it is useful to measure changes in bottom salinity (Sect. H21) and temperature (Cheung et al., 2013; Gehlen et al., 2014; Saba et al., 2015). As with the request to save SST and SSS, we request for CMIP6 the bottom temperature and bottom salinity in order to facilitate easier analysis using these fields.

H17 Salinity of liquid water

- so

- soga

We request the three-dimensional monthly mean ocean salinity field. In addition, as for potential temperature, we recommend saving the global mean salinity of liquid seawater. This mean is computed in a non-Boussinesq model by the mass weighted mean

$$\langle S \rangle_{\text{non-Bouss}} = \frac{\sum_{i,j,k} \rho S \, dA \, dz}{\sum_{i,j,k} \rho \, dA \, dz},$$

(H35)

whereas for a Boussinesq model it is the volume-weighted mean

$$\langle S \rangle_{\text{Bouss}} = \frac{\sum_{i,j,k} S \, dA \, dz}{\sum_{i,j,k} dA \, dz}. \quad (H36)$$

19We discuss salinity and TEOS-10 in Appendix D.

H18 Sea surface salinity (SSS)

- sos

- sosga

The sea surface salinity (SSS) provides a useful means for detecting changes in the high-latitude thermohaline forcing, which can present the analyst with a quick diagnosis of whether a simulation is more or less prone to modification of the overturning circulation. For example, freshwater capping can be seen by diagnosis of the SSS. In this case, signals in SSS may motivate more detailed analysis of the three-dimensional fields. In addition, to further reduce the size of the diagnostic, we request the global area average of the SSS, sampled as monthly means:

$$sosga = \frac{\sum_{i,j} dA \, S_{i,j,k=1}}{\sum_{i,j} dA}. \quad (H37)$$

H19 Daily mean sea surface salinity (SSS)

- sos

Recent remote measures of surface salinity are available from SMOS (Berger et al., 2002), Aquarius (Lagerloef et al., 2008) and SMAP (Piepmeier et al., 2015) satellites. These measures allow for higher temporal features from models to be compared to observations, thus motivating the archival of daily mean SSS from models.

H20 Daily and monthly mean squared SSS

The quadratic field

- sos sq

is accumulated each model time step. It is requested to help measure the variability simulated in the sea surface salinity, so that one may compute the variance (see Sect. H8 for sea level variance).

H21 Bottom salinity

- sob

To study impacts on ecosystems from climate change, it is useful to measure changes in bottom temperature (Sect. H16) and salinity (Cheung et al., 2013; Gehlen et al., 2014; Saba et al., 2015).
H22  Squared ocean buoyancy frequency

\[ \text{obfsq} \]

This diagnostic is the squared buoyancy frequency in units of s^{-2}. We recommend use of locally referenced potential density for computing this measure of vertical gravitational stability.

Previous CMIPs requested the potential density referenced to the ocean surface \( \sigma_0 \). However, the buoyancy frequency is a more useful diagnostic for measuring vertical stability, which motivated us to replace potential density with squared buoyancy frequency. Additionally, buoyancy frequency is commonly used as part of various ocean parameterizations, such as gravity wave mixing (Simmons et al., 2004; Melet et al., 2013), and mesoscale eddy closures (Gent et al., 1995; Griffies et al., 1998).

H23  Ideal age tracer

\[ \text{agesc} \]

The ideal age tracer (Thiele and Sarmiento, 1990; England, 1995) provides a useful measure of ocean ventilation (Bryan et al., 2006; Gnanadesikan et al., 2007). This tracer is set to zero in the model surface level/layer at each time step. Beneath the surface level, the ideal age tracer grows older according to the model time. Ideal age is particularly useful for revealing surface-to-deep connections in regions such as the Southern Ocean. It can also be used to estimate uptake of anthropogenic tracers such as carbon dioxide (Russell et al., 2006; Gnanadesikan et al., 2007). This tracer is set according to the model time. Ideal age is particularly useful for revealing surface-to-deep connections in regions such as the Southern Ocean. It can also be used to estimate uptake of anthropogenic tracers such as carbon dioxide (Russell et al., 2006).

Ideal age satisfies the following advection–diffusion source equation:

\[
\frac{\partial A}{\partial t} + \nabla \cdot (n A) = 1 - \nabla \cdot F + \gamma (A^* - A) \delta_{\text{surf}}. \quad (H38)
\]

In this equation, \( A \) is the ideal age with dimensions of time; a unit source (the “1” on the right-hand side) adds time to the age tracer over each time step; \( F \) is the subgrid-scale (SGS) flux; and a damping is applied in a surface region back to \( A^* = 0 \). The surface damping is often applied just to the top grid cell. Alternatively, it can be applied over a region of specified thickness. If the damping time \( \gamma^{-1} \) is zero (infinitely strong damping), then \( A = A^* = 0 \) is specified for the surface region, i.e. the top cell value of the age tracer is set to \( A = 0 \). Some groups take \( \gamma^{-1} = 0 \), whereas others use a finite value. So long as the restoring strength is sufficiently strong, there should be only minor distinctions between the two approaches, although there is no documented study testing this conjecture.

To facilitate direct comparison of ideal age in the different model simulations, we recommend initializing age globally to zero at 1 January 1850 in the historical experiments, or at the start of any of the various scenario experiments. Measuring age in years, rather than seconds, is the traditional approach in ocean modelling, and is recommended for ideal age in CMIP6.

H24  Mixed layer depth

\[ \text{mlotst} \]

\[ \text{mlotstmax} \]

\[ \text{mlotstmin} \]

H24.1  Summary of the diagnostic

An assessment of model mixed layer depth (MLD) is useful for understanding how water-mass formation is regulated by upper ocean stratification and surface water overturn. For this purpose, we ask for the monthly mean MLD. Additionally, to help measure the minimum and the maximum ventilation depths, we ask for the maximum and minimum MLD over each month. Note that when computing the maximum and minimum, adjacent points in space need not have extrema registered at the same time step.

There is no universally agreed upon criterion for defining the mixed layer depth. For the purpose of fostering a consistent comparison of simulated mixed layers from ocean model components in CMIP6, the “sigma-t” criterion introduced by Levitus (1982) should be followed.

H24.2  Theoretical and practical considerations

The planetary boundary layer is that region of the upper ocean that experiences strong three-dimensional turbulent motion due to mechanical and buoyancy forcing from air–sea and ice–sea interactions. Turbulent mixing in this region is parameterized in hydrostatic ocean models by schemes such as Mellor and Yamada (1982), Gaspar et al. (1990), Large et al. (1994), or Hallberg (2003). Notably, the boundary layer depth is not what is asked for with the OMIP mixed layer depth diagnostic. Nor is the bulk mixed layer (commonly used in isopycnal models; Hallberg, 2003) what is asked for here.

Rather, the mixed layer depth is based on measuring ocean gravitational stability under a vertical displacement from the surface. To determine whether vertical transfer is favoured requires a thought experiment, in which a surface ocean fluid parcel is displaced downward without changing its temperature or salinity, but feeling the local \textit{in situ} pressure. If the density of the displaced parcel is sufficiently far from the local \textit{in situ} density, then the displacement is not favoured, and we are thus beneath the mixed layer and into the stratified interior. What determines “sufficiently far” is subjective, with convention determining the precise value.

The mixed layer has near-zero vertical gradients of temperature, salinity, and density, as well as tracers such as CFCs. So most techniques to estimate the MLD rely on either a threshold gradient or a threshold change in one of...
these quantities, normally in potential temperature $\theta$ or density (see for example Lorbacher et al., 2006; de Boyer Montégut et al., 2004; Monterey and Levitus, 1997). Relying solely on $\theta$ has the advantage of good observational data coverage, but this approach neglects salinity stratification associated with barrier layers (see e.g. Sprintall and Tomczak, 1992) and high latitudes where salinity greatly impacts on density. In contrast, relying solely on density overlooks density-compensating changes in $\theta - S$, thus overestimating the thickness of the mixed layer.

The method we recommend for OMIP comes from Levitus (1982). Here, the MLD is defined based on meeting a “$\sigma$-crit” criterion. This method is readily employed in offline mode, thus supporting the use of monthly mean model fields. However, we recommend computing mlotst online in order to avoid aliasing. Also, we ask for the squared mixed layer depth mlotstsq (see Sect. H25) to allow for computation of the variance. The variance calculation is served best by online mixed layer depth calculations.

We here provide some details for the diagnostic. Mathematically, we compute the difference between the following two densities,

$$
\rho_{\text{displaced from surface}} = \rho[S(k = 1), \Theta(k = 1), p(k)]
$$

$$
\rho_{\text{local}} = \rho[S(k), \Theta(k), p(k)],
$$

and convert that density difference to a buoyancy difference

$$
\delta B = -\left(\frac{g}{\rho_{\text{local}}} \frac{\rho_{\text{displaced from surface}} - \rho_{\text{local}}}{\rho_{\text{local}}} \right).
$$

This buoyancy difference is computed from the surface down to the first depth at which $\delta B > \Delta B_{\text{crit}}$, where the OMIP recommended value is

$$
\Delta B_{\text{crit}} = 0.0003 \text{ m s}^{-2},
$$

with this value also used in Levitus (1982). Other values may be more suitable for regional studies, such as for the Southern Ocean. The mixed layer depth, $H^{\text{mld}}(x, y, t)$, is then approximated by interpolating between the depth where $\delta B > \Delta B_{\text{crit}}$ and the shallower depth.$^{20}$ With $g = 9.8 \text{ m s}^{-2}$ and $\rho_{\text{local}} \approx 1035 \text{ kg m}^{-3}$, then $\Delta B_{\text{crit}} = 0.0003 \text{ m s}^{-2}$ corresponds to a critical density difference of

$$
\Delta \rho_{\text{crit}} = 0.03 \text{ kg m}^{-3},
$$

as used by de Boyer Montégut et al. (2004). Note that some studies employ the larger critical value, $\Delta \rho_{\text{crit}} = 0.125 \text{ kg m}^{-3}$, which will generally result in a deeper mixed layer depth due to the need to penetrate deeper into the stratified water. The choice is subjective, but should be compatible across models and observations to ensure suitable comparisons.

20Linear interpolation is common, though other methods may be used depending on modeller preference.

H25 Squared mixed layer depth

- mlotstsq

This diagnostic is the square of mlotst (Sect. H24). Diagnosing both mlotst and mlotstsq online during each model time step allows one to compute variance of the mixed layer depth (see Sect. H8 for the analogous calculation of dynamic sea level variance).

H26 Barotropic or quasi-barotropic streamfunction

- mstfbarot

H26.1 Summary of the diagnostic

The barotropic streamfunction is a useful field for mapping the vertically integrated fluid transport. However, many ocean models have jettisoned the rigid-lid assumption of Bryan (1969) for both computational and physical reasons. Absent a rigid-lid assumption, the vertically integrated mass transport$^{21}$

$$
U^p = \int_{-H}^{\eta} \rho \ u \ dz
$$

generally has a non-zero divergence, thus precluding it from being fully specified by a single scalar field. Instead, both a streamfunction and velocity potential are needed to specify the transport. For those models that do not compute a barotropic streamfunction, we introduce the notion of a quasi-barotropic streamfunction $\psi^U$ in the following theoretical considerations, with this field serving as a useful approximate alternative to the barotropic streamfunction.

In summary, we request either of the following scalar fields be archived for purposes of mapping the vertically integrated mass transport:

- Barotropic streamfunction for those models that compute this function using an elliptic solver;
- The quasi-barotropic streamfunction $\psi^U$ for more general cases.

We recommend that the dimensions of the streamfunction be mass transport (kg s$^{-1}$), rather than volume transport (m$^3$ s$^{-1}$) (see start of Sect. I).

H26.2 Theoretical considerations

For a mass-conserving non-Boussinesq fluid, the vertically integrated mass transport $U^p = \int_{-H}^{\eta} \rho \ u \ dz$ has a divergence given by

$$
\nabla \cdot \overline{U}^p = -\frac{\partial (D \langle \rho \rangle)}{\partial t} + Q^m,
$$

21The density factor $\rho$ in a non-Boussinesq fluid becomes the constant $\rho_o$ for Boussinesq fluids.
where \( D = H + \eta \) is the thickness of a fluid column. Similarly, for a Boussinesq fluid the depth-integrated velocity \( \mathbf{U} = \int_{-H}^0 u \, dz \) has a divergence

\[
\rho_o \nabla \cdot \mathbf{U} = -\rho_o \left( \frac{\partial \eta}{\partial t} \right) + Q^m. \tag{H45}
\]

Given that neither \( \mathbf{U}^0 \) nor \( \mathbf{U} \) are non-divergent, a barotropic streamfunction is insufficient to fully describe the vertically integrated flow. In general, it is necessary to solve an elliptic boundary value problem to diagonalize the barotropic streamfunction. However, for CMIP purposes, it is sufficient to compute an approximate streamfunction, with details now given.

Consider the function

\[
\psi_U(x, y) = -\int_{y_o}^y U^0(x, y') \, dy', \tag{H46}
\]

where the southern limit \( y_o \) is at Antarctica. Note that all intermediate ranges of latitude bands are included, so there are no shadow regions that may otherwise be isolated due to land/sea arrangements. By definition, the \( y \) derivative \( \psi_U(x, y) \) yields minus the transport in the \( \hat{x} \) (eastward) direction

\[
\frac{\partial \psi_U}{\partial y} = -U^0, \tag{H47}
\]

yet the \( x \) derivative does not yield the \( \hat{y} \)-transport due to the divergent nature of the vertically integrated flow. A complement function

\[
\psi_V(x, y) = \psi_U(x_o, y) + \int_{x_o}^x V^0(x', y) \, dx' \tag{H48}
\]

yields \( \partial_x \psi_V = V^0 \). In the special case of a Boussinesq rigid-lid model absent surface water fluxes, \( \psi_U \) and \( \psi_V \) reduce to the single rigid-lid barotropic streamfunction. In the more general case, comparison of \( \psi_U \) and \( \psi_V \) in climate model simulations at GFDL reveals that after just a few years of spin-up, patterns for the monthly means of \( \psi_U \) and \( \psi_V \) are very similar. This result provides evidence that much of the large-scale vertically integrated circulation is nearly non-divergent. In this case, either function \( \psi_U \) and \( \psi_V \) renders a useful map of the vertically integrated mass transport. Due to its simplicity, we recommend that the quasi-barotropic streamfunction \( \psi_U \) be archived for CMIP6.

**Appendix I: Diagnostics involving vector fields**

We now consider components to vector fields, with a summary of the diagnostics given in Table I1. As for all other fields, the vector fields are mapped to a geopotential, \( \tilde{z}^* \), pressure, or \( p^* \) vertical coordinate surface. For transports, the mapping is conservative.

**I1 Residual mean velocity and transport units**

The residual mean velocity, \( \mathbf{n}^\dagger \), transports seawater mass and tracer in an ocean model, where

\[
\mathbf{n}^\dagger = \mathbf{n} + \mathbf{n}^\ast \tag{I1}
\]

is the sum of the model prognostic velocity \( \mathbf{n} \) (the Eulerian mean) plus a parameterized eddy-induced velocity, \( \mathbf{n}^\ast \). We identify two commonly used eddy-induced velocities.

- mesoscale. The parameterized eddy-induced velocity for mesoscale processes commonly follows that suggested by Gent et al. (1995) or related methods such as Ferrari et al. (2010).

We know of no other processes now commonly parameterized in global climate simulations according to eddy-induced transport, though such may appear in the future. Notably, if there are no parameterizations of eddy-induced transport, \( \mathbf{n}^\ast = 0 \) so that the residual mean is the Eulerian mean, \( \mathbf{n}^\dagger = \mathbf{n} \). We focus our transport diagnostics on the residual mean field, though we still recommend archiving the raw horizontal velocity field, \( \mathbf{u} \) in Sect. I2.

The mass transport

\[
\gamma^\circ \mathbf{n} \cdot \hat{n} \, dA \tag{I2}
\]

measures the mass per time passing through the \( \hat{n} \) face of a grid cell, with \( dA \) the area of the cell face and \( \hat{n} \) the outward normal. This transport is conveniently quantified using the mass Sverdrup

\[
\text{mass Sv} = 10^9 \, \text{kg s}^{-1} \tag{I3}
\]

rather than the volume Sverdrup

\[
\text{volume Sv} = 10^6 \, \text{m}^3 \, \text{s}^{-1}. \tag{I4}
\]

For Boussinesq fluids, the density factor \( \rho \) becomes a constant reference density \( \rho_o \) (see rhozero in Table G1), which trivially allows for use of the mass Sverdrup as the unit of transport in Boussinesq fluids. Therefore, we request archiving mass transport in the units kg s\(^{-1}\) rather than a volume transport (m\(^3\) s\(^{-1}\)).

**I2 Horizontal velocity field from resolved flow**

- \( \mathbf{u}_o \): zonal velocity component \( \left( \hat{x} \cdot \mathbf{n} \right) \)
- \( \mathbf{v}_o \): meridional velocity component \( \left( \hat{y} \cdot \mathbf{n} \right) \)

These diagnostics save the horizontal velocity components, as diagnosed from the velocity field time-stepped as part of the model prognostic equations. This diagnostic does not include any extra velocity that may arise from parameterized subgrid-scale eddy advection.
Table II. Diagnostic table for vector components, including a sub-table relating the CMOR name to its CF standard name. Note that as per the discussion in Sect. A3, we generally recommend native grid sampling of vector field components, with the exception of unstructured mesh models. The column indicating the experiment for saving the diagnostics generally says “all”; in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCPP, ScenarioMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations. The Priority 1 diagnostics should be saved as decadal time means at decadal intervals for the piControl spin-up. Some of the fields in this table should be partitioned into Atlantic–Arctic, Indian–Pacific, and global regions. Spherical regridding (mapping to north–south and east–west vector components) is discussed in Sects. C3 and C4.

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<td>hfx</td>
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</tr>
<tr>
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<td>ldy</td>
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<td>northward_ocean_salt_transport due to gyre</td>
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<td>27</td>
<td>ldybasin</td>
<td>northward_ocean_salt_transport due to overturning</td>
</tr>
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</table>
I3 Horizontal residual mean mass transport

- \( \text{umo} = \rho u^\dagger \, dy \, dz \)
- \( \text{vmo} = \rho v^\dagger \, dx \, dz \)

This diagnostic asks for the horizontal mass transport through faces of a grid cell, where transport arises from the residual mean (sum of model prognostic velocity plus parameterized eddy-induced, as discussed in Sect. II) in each of the basins Atlantic–Arctic, Indian–Pacific, and World Ocean. To separate the Indian and Pacific oceans is not sensible, since there is no meridional boundary separating these basins. Instead, Atlantic–Arctic, Indian–Pacific, and World Ocean are the only three physically relevant partitions available. We ask for the transport as a function of depth/pressure as well as potential density referenced to 2000 db.

The issue of generalized horizontal coordinates adds complexity to the diagnosis of the northward mass transport when using non-spherical grids. As stated in Sect. C4, instead of regridding mass fluxes to a spherical grid, and then computing the basin transports, we recommend computing the transports across native grid lines that approximate latitude circles and reporting these as a function of latitude. Such algorithms can be implemented in a conservative manner for finite volume-based models, even those with complex grids (e.g. see Fig. C2 of Forget et al., 2015). Finite element models, in contrast, require extra care (Sidorenko et al., 2009).

For those models using a non-spherical coordinate horizontal grid, in addition to archiving the meridional overturning streamfunction, we recommend archiving the model native grid \( \hat{y} \)-ward streamfunction, where \((x, \hat{y})\) are directions defined according to the model native grid. We also use the synonyms (iward, jward), using the familiar \((i, j)\) notation for horizontal grid indices. For many purposes and for many of the most commonly used non-spherical structured grids (e.g. the tripolar grids of Murray, 1996 and Madec and Imbard, 1996, and the displaced bipolar grid of Smith et al., 1995), the \( \hat{y} \)-ward native grid streamfunction is sufficient since it closely approximates the spherical meridional streamfunction.

A general expression for the ocean mass transport overturning streamfunction is given by

\[
\Psi(y, s, t) = -\int_{x_u}^{x_b} dx \int_{-H}^{z(s)} \rho v^\dagger \, dz,
\]

where \( v^\dagger \) is the meridional residual mean velocity (see the vmo diagnostic in Sect. I3). \( \Psi \) is in fact a transport streamfunction only for the steady-state rigid-lid Boussinesq case. We nonetheless retain the name “streamfunction” for historical reasons. Note that the zonal integral is computed along surfaces of constant \( s \), where \( s \) is either a geopotential/pressure surface or a potential density surface. That is, we recommend that the following versions of the overturning streamfunction be archived at monthly time averages in the CMIP6 repository, with results for the Atlantic–Arctic, Indian–Pacific, and global oceans:

- meridional-depth overturning streamfunction and \( \hat{y} \)-ward-depth overturning streamfunction: the depth \( z(s) \)
corresponds to either the depth of a geopotential or the depth of a pressure surface, depending on whether the model is Boussinesq or non-Boussinesq, respectively.

- meridional-density overturning streamfunction and $\hat{y}$-ward-density overturning streamfunction: the depth $z(s)$ corresponds to the depth of a predefined set of $\sigma_{2000}$ isopycnals, with the definition of these isopycnals at the modeller’s discretion. This field presents complementary information relative to the $\hat{y}$-ward-depth overturning streamfunction, and is very useful particularly for diagnosing water mass transformation processes.\textsuperscript{22}

- Consistent with the discussion in Sect. A1, it is critical that the time average of the streamfunction be accumulated using each model time step, in order to avoid problems with aliasing and problems ignoring correlations.

17 Meridional and $\hat{y}$-ward overturning streamfunction from SGS processes

- msftmzjmpa: meridional-depth mass streamfunction from parameterized mesoscale
- msftmrhompa: meridional-density mass streamfunction from parameterized mesoscale
- msftyzmpa: $\hat{y}$-depth mass streamfunction from parameterized mesoscale
- msftyrhompa: $\hat{y}$-density mass streamfunction from parameterized mesoscale
- msftmzsmpa: meridional-depth mass streamfunction from parameterized submesoscale
- msftyzsmpa: $\hat{y}$-depth mass streamfunction from parameterized submesoscale

We follow the same philosophy as in Sect. I6 to diagnose here the meridional and $\hat{y}$-ward overturning streamfunction arising from parameterized subgrid-scale (SGS) transport. The following points should be considered for this diagnostic.

- For the Gent et al. (1995) parameterization, the meridional overturning streamfunction for mass transport is

$$\Psi_{gm}(y,s,t) = -\int_{x_a}^{x_b} \int_{-H}^{z(s)} \rho v_{gm}^d dz$$

$$= \int_{x_a}^{x_b} \int_{-H}^{z(s)} \partial_z (\rho \kappa_{gm} S^y) dz$$

$$= \int_{x_a}^{x_b} \rho \kappa_{gm} S^y(z(s)) dx,$$  \( I7c \)

where $\kappa_{gm} > 0$ is the eddy diffusivity, $S^y$ is the $\hat{y}$ neutral slope, and $\kappa_{gm}$ vanishes at the ocean bottom. As for the residual mean streamfunction $\Psi^m$ defined by Eq. (I6), we recommend archiving $\Psi_{gm}$ on both depth/pressure levels and isopycnal ($\sigma_{2000}$) levels.

18 Net heat transport from resolved and parameterized processes

- hfx: depth-integrated $x$-component to net ocean heat transport
- hfy: depth-integrated $y$-component to net ocean heat transport
- hfbasin: depth-integrated northward net ocean heat transport integrated within basins

There are many ocean processes that affect heat transport: resolved advective transport, diffusion, parameterized eddy-induced advection or skew transport, overflow parameterizations, etc. In the analysis of ocean model simulations, it is useful to have a measure of each component of the heat transport, particularly in the horizontal. We request the $\hat{x}$-ward
and \(\hat{y}\)-ward heat transport from all ocean processes. The horizontal components to this depth-integrated heat transport are archived in \(hfx\) and \(hfy\). Note that the heat transports are computed using the Celsius temperature scale (see Appendix E).

Following from the approach taken for the meridional overturning streamfunction, each ocean model using non-spherical coordinate horizontal grids should also compute the northward heat transport in each of the basins (northward_ocean_heat_transport), approximated using the model native grid fields without regridding. For models using a spherical latitude–longitude grid, there will be no difference. The approximated poleward transport in non-spherical grids will generally consist of transports crossing a “zig-zag” path (Sect. C4). The resulting poleward heat transport should be reported as a function of latitude, with latitudinal resolution comparable to the model native grid resolution.

19 Adective heat transport from parameterized mesoscale and submesoscale processes

- \(hfbasinpmadv\): northward heat transport from parameterized mesoscale advection
- \(hfbasinpsmadv\): northward heat transport from parameterized submesoscale advection
- \(hfbasinpsmadv\): northward heat transport from parameterized mesoscale diffusion
- \(hfbasinpadv\): northward heat transport from parameterized advection (meso + submeso)

In support of understanding the importance of various subgrid-scale (SGS) parameterizations, we recommend that depth- and basin-integrated northward heat transports should be archived for the Atlantic–Arctic, Indian–Pacific, and World Ocean basins. Additional notes for this diagnostic follow.

- Parameterized SGS advection from mesoscale closures (such as Gent et al., 1995) and submesoscale closures (such as Fox-Kemper et al., 2008, 2011) are included. They occur with the suffix “advection”, even if the implementation of the schemes appears as a skew transport.
- If the eddy-induced advection from the mesoscale and submesoscale closures are combined operationally in the model, and cannot be separately diagnosed, then their net effect is archived in fields with suffix “due_to_parameterized_eddy_advection”.
- In addition to eddy-induced advection, mesoscale eddies are commonly parameterized through neutral diffusion as in Solomon (1971) and Redi (1982). Contributions to heat transport from neutral diffusion should be placed in the fields with suffix “due_to_parameterized_mesoscale_diffusion”.
- The vertically integrated northward transports can be approximated using the a “zig-zag” path method discussed in Sect. C4. The components should be archived as monthly means for the Atlantic–Arctic, Indian–Pacific, and World oceans. The transports should be reported as a function of latitude, with the latitudinal spacing comparable to the model native grid spacing.

I10 Gyre and overturning decomposition of heat and salt residual mean advective transport

- \(htovgyre\): northward heat transport from gyres
- \(htovovrt\): northward heat transport from overturning
- \(sltovgyre\): northward salt transport from gyres
- \(sltovovrt\): northward salt transport from overturning

110.1 Summary of the diagnostic

The \(\hat{y}\)-ward advective transport of a tracer within a particular ocean basin is given by the integral

\[
\mathcal{H}^{(S)}(y, t) = \int_{x_1}^{x_2} \int_{-H}^{\eta} \rho \, \nabla \cdot \mathbf{v} \, dz; \quad (I18)
\]

where \(C\) is the tracer concentration, \(\mathbf{v}^\dagger\) is the residual mean meridional velocity component (sum of resolved plus parameterized advection), \(z = -H(x, y)\) is the ocean bottom, \(z = \eta(x, y, t)\) is the ocean free surface, and \(x_1\) and \(x_2\) are the boundaries of the basin or global ocean. It is useful for some analysis to decompose the transport (I18) into “gyre” and “overturning” components, with these terms defined in the following. See Sect. 3.1.1 of Farneti and Vallis (2009) for an example of this diagnostic in use.

We recommend that the monthly means for the components to heat and salt transport be archived, partitioned according to Atlantic–Arctic, Indian–Pacific, and World Ocean. The transports should be reported as a function of latitude, with the latitudinal spacing comparable to the model native grid spacing.

110.2 Theoretical considerations

The total mass transport leaving the \(\hat{y}\)-ward face of a grid cell is written

\[
V \, dx = v^\dagger \, \rho \, dz \, dx, \quad (I19)
\]

and so \(C \, V \, dx\) measures the mass per time (kg s\(^{-1}\)) or heat per time (watt) of tracer leaving the \(\hat{y}\)-ward face, including transport from resolved and parameterized advection. We now consider a decomposition of this transport by defining the basin average transport and basin average tracer concentration as follows

\[
[V] = \frac{\sum_i V_i \, dx}{\sum_i dx} \quad (I11a)
\]
\[ C = \frac{\sum_i C \, dx}{\sum_i dx} \]  

(I10b)

along with the deviations from basin average

\[ V = [V] + V^* \quad \text{(I11a)} \]

\[ C = [C] + C^* \quad \text{(I11b)} \]


The discrete \( i \)-sum extends over the basin or global domain of interest, so that \( \sum_i V \, dx \) is the total \( \hat{y} \)-ward transport of seawater at this band at a particular ocean model vertical level. The resulting \( \hat{y} \)-ward tracer transport becomes

\[ \mathcal{H}(y, t) = \sum_{i,k} V C \, dx = \sum_{i,k} \left( [V][C] + V^* C^* \right) \, dx, \quad \text{(I12)} \]

where the \( k \) sum extends over the vertical cells in a column. It is common to identify three components:

\[ y_{\text{flux\_advect}} = \sum_i \sum_k V C \, dx \quad \text{(I13)} \]

\[ y_{\text{flux\_over}} = \sum_i \sum_k [V][C] \, dx \quad \text{(I14)} \]

\[ y_{\text{flux\_gyre}} = \sum_i \sum_k V^* C^* \, dx, \quad \text{(I15)} \]

with

\[ y_{\text{flux\_gyre}} = y_{\text{flux\_advect}} - y_{\text{flux\_over}}. \quad \text{(I16)} \]

This identity follows very simply when the advective flux takes on the form of either first order upwind or second order centered differences. It becomes more complex when considering higher order, or flux limited, advection schemes. In the more general cases, the expression (I16) serves to define the gyre transport component. In this way, the advective flux is built from the advection scheme used in the ocean model.

### Appendix J: Diagnostics of mass transports through pre-defined transects

- mfo

There are a number of climatologically important straits, throughflows, and current systems whose mass transport has been measured observationally. These mass transports provide a useful means of characterizing the rates at which water flows through key regions of the ocean. Offline diagnostics of these transports, using the archived velocity and/or the barotropic streamfunction, can be subject to uncertainty, especially for models with complex horizontal and vertical grids. It is thus more direct and accurate for each participating model group to diagnose transports online.

23 The CLIVAR Ocean Model Development Panel maintains the REOS website http://www.clivar.org/clivar-panels/omdp/reos (Repository for Evaluating Ocean Simulations), on which the transports in Table J1 are listed.

In Table J1, we offer a list of recommended transports for CMIP6, with further details for these sections given in Table J2. A map of the sections is provided in Fig. J1, as realized in a particular model configuration used at GFDL. Each transport section has an associated string valued coordinate given by the name. We present references to observational estimates in Table J2, though note the large uncertainties in many locations.

We make the following recommendations regarding the integrated mass transports.

- In Table J1, we note the approximate geographical longitude and latitude coordinates of the straits and currents. Given considerations of model grid resolution and grid orientation, precise values for the coordinates may differ for any particular model. In general, we recommend computing the simulated transport where the strait is narrowest and shallowest in the model configuration, and where the model grid is closely aligned with the section.

- For many ocean model grids, the requested transports can be diagnosed by aligning the section along a model grid axis. In this case, it is straightforward to assign a positive sign to transports going in a pseudo-north or pseudo-east direction, and negative signs for the opposite direction. We use the term pseudo here as it refers to an orientation according to the model grid lines, which in general may not agree with geographical longitude and latitude lines. The sign convention chosen for the...
Table J1. This table summarizes the sections for archiving the depth-integrated mass transport time series from the ocean component in CMIP6 simulations. Each time series is identified by the CF standard name sea_water_transport_across_line. Additionally, each geographical region has an associated string-valued coordinate given by the name in this table. All time series should be saved as monthly means in units of kg s$^{-1}$. Positive and negative numbers refer to total northward/eastward and southward/westward transports, respectively. The column indicating the experiment for saving the diagnostics generally says “all”, in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCPP, ScenarioMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations.

| Item | CMOR name | Geographical endpoints | Depth | Sponsor | CMIP5/CMIP6 | Units | Time | Priority | exp |
|------|------------|------------------------|-------|---------|-------------|-------|------|----------|-----|-----|
| 1    | mfo (parents_opening) | (16.8°E, 76.5°N)/(19.2°E, 70.2°N) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 2    | mfo (bering_strait)   | (171°W, 66.2°N)/(166°W, 65°N) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 3    | mfo (caribbean_windward_passage) | (75°W, 20.2°N)/(72.6°W, 19.7°N) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 4    | mfo (davis_strait)    | (50°W, 65°N)/(56°W, 65°N)    | full   | OMIP    | new         | kg s$^{-1}$ | month | 2     | all      |     |
| 5    | mfo (denmark_strait)  | (37°W, 66.1°N)/(22.5°W, 66°N) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 6    | mfo (drape_passage)   | (68°W, 54°S)/(60°W, 64.7°S)   | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 7    | mfo (english_channel) | (1.5°E, 51.1°N)/(1.7°E, 51.0°N) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 8    | mfo (faroe_scotland_channel) | (6.9°W, 62°N)/(5°W, 58.7°N) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 9    | mfo (florida_bahamas_strait) | (78.5°W, 26°N)/(80.5°W, 27°N) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 10   | mfo (fram_strait)     | (20°W, 79°N)/(11°E, 79°N)    | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 11   | mfo (gilbaltar_strait) | (35.8°N, 5.6°W)/(36°N, 5.6°W) | full   | OMIP    | new         | kg s$^{-1}$ | month | 2     | all      |     |
| 12   | mfo (iceland_faroe_channel) | (13.6°W, 64.9°N)/(7.4°W, 62.2°N) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 13   | mfo (indonesian_throughflow) | (100°E, 6°S)/(140°E, 6°S) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 14   | mfo (mozambique_channel) | (39°E, 16°S)/(45°E, 18°S) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 15   | mfo (pacific_equatorial_undercurrent) | (155°W, 2°S)/(155°W, 2°N) | 0-350m | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |
| 16   | mfo (taiwan_and_luzon_straits) | (121.8°E, 18.3°N)/(121.8°E, 22.3°N) | full   | OMIP    | same        | kg s$^{-1}$ | month | 2     | all      |     |

recorded transport should be indicated in the metadata information for the transport field.

- Some models may have a strait artificially closed, due to inadequate grid resolution. In this case, a zero or missing transport should be recorded for this strait.

- The full column depth-integrated mass transport vanishes for mesoscale closures based on Gent et al. (1995) and the submesoscale closures based on Fox-Kemper et al. (2008). Hence, when computing a column-integrated mass transport, it only involves the resolved advective transport.

- For the equatorial undercurrent, we ask for the residual mean zonal transport from the surface to 350 m.

Appendix K: Diagnostics of boundary fluxes

The ocean is a forced-dissipative system, with forcing largely at its boundaries. To develop a mechanistic understanding of ocean simulations, it is critical to have a clear sampling of the many forcing fields. Some of the following fields can be found in other parts of the CMIP6 archive as part of the sea-ice or atmosphere components. However, these fields are typically on grids distinct from the ocean model. Fluxes on grids distinct from the ocean make accurate budget analyses difficult to perform. Additionally, these other components are absent in the OMIP ocean/sea-ice simulations. We thus follow the CMIP5 approach, in which we request that CMIP6 models archive the precise boundary fluxes used to force the ocean model.

K1 General comments on boundary fluxes

We offer here some general comments regarding the boundary flux fields. Specifications for the requested fluxes are given in the subsequent subsections.

K1.1 Area normalization

All fluxes (water mass, salt mass, heat, momentum) are normalized according to the horizontal area of the ocean model grid cell. In some cases (e.g. rainfall), the flux computation requires integrating the rainfall over the ice-free sea (to get a mass per time of rainfall) and then dividing by the ocean grid cell area (to get mass per time per area). For these fluxes, according to the CF metadata conventions, the cell_methods attribute for the fields should read

- area: mean where ice_free_sea over all_area_types.

In other cases (e.g. melting sea ice) the flux computation requires integrating the sea-ice melt over the sea-ice-covered portion of the ocean grid cell, and then dividing by the ocean grid cell area. For these fluxes, according to the CF metadata conventions, the cell_methods attribute for the fields should read

- area: mean where sea_ice over all_area_types.
K1.2 Diagnosing transports from fluxes

Multiplication of a boundary flux by the ocean model grid cell area allows for computing the transport of mass, salt, heat, or momentum passed to the ocean. This property must be maintained whether the fluxes are archived on the native model grid, or mapped onto a spherical grid.

K1.3 Sign convention for fluxes

Momentum fluxes have a sign so that a positive flux in a particular direction will increase the momentum of the liquid ocean. Likewise, fluxes of mass, salt, and heat are positive if they increase the ocean content of mass, salt, and heat. This convention for scalars follows that from CMIP5, with one exception. Namely, the evaporation diagnostic in CMIP5 was positive for water leaving the ocean. The CMIP6 convention aims to make all scalar fluxes compatible with one another, so that the net mass flux entering the ocean is the sum of all the component mass fluxes. With this convention, evaporation has a negative sign, whereas condensation is positive.

K1.4 Coupling beneath the surface ocean grid cell

Many climate models place boundary fluxes just at the ocean surface. However, more general couplings are being considered (e.g., penetrative shortwave heating; sea-ice and ice-shelf models that interact with more than the surface ocean cell; river runoff inserted as a side boundary at depth). To allow for such generality, we ask that those fluxes that are three-dimensional be archived with their full three-dimensional structure.
K1.5 Flux adjustments

The term “flux correction” in Tables K1, K2, K3, and K4 refers to the imposition of a prescribed boundary flux that has at most a monthly variability (sometimes only an annual mean is used) (Sausen et al., 1988; Weaver and Hughes, 1996; Gordon et al., 2000). These modifications of the prognostic fluxes have no interannual variability.

We prefer the term “flux adjustments” since the use of modified fluxes, though aiming to reduce flux errors relative to observations, should not be presumed to be “correct”. They are included in some models for the purpose of reducing model drift, with such drift a function of nearly all aspects of the particular model configuration. Flux adjustments are rather uncommon in CMIP6 due to model improvements during the recent 10–20 years, largely due to improved representation of poleward heat transport in both atmosphere and ocean models (see, for example, Sect. 8.4.2 of McAvaney et al., 2001). In such cases, the flux adjustment fields are zero or simply not archived.

Note that for the CMIP6/FAFMIP experiment (Sect. 3.2 and Gregory et al. (2016)), the prescribed perturbation fields should be saved in the appropriate flux correction diagnostics for mass (or virtual salt), heat, and momentum.

K1.6 Heat content of water crossing ocean boundaries

Seawater carries salt, heat, carbon, and other trace matter. Some tracers are transferred across the ocean surface as mass enters or leaves the ocean. This “advective” mass transfer across ocean boundaries must be accounted for in the budget for ocean tracer content (an extensive property). Salt is generally not transferred across the air–sea interface. However, it is transferred across the ice–sea boundary, since sea ice has a non-zero salinity. It can also be advected into the ocean from salty estuaries. The ocean heat budget is affected by the boundary transfer of radiative (shortwave and longwave), turbulent (sensible and latent), and advective heat fluxes. For example, water entering the ocean through rain or river runoff increases the ocean mass, and in so doing it increases the ocean heat content, even if it enters at the local sea surface temperature.

There is an arbitrariness in ocean heat content associated with the arbitrary temperature scale. However, time changes in the heat content are not affected, as we show in Appendix E. We find it convenient to measure the heat content using the Celsius temperature scale, since that is the scale used in ocean models. Consequently, the associated heat content (as a flux and relative to 0 °C) is requested in Table K3. Models that artificially preclude water to cross the ocean boundary (e.g. rigid-lid models, or models with a virtual tracer flux discussed in Sect. K1.7) have zero contributions to these heat fluxes, in which case there is no need to archive the zero fields.

For precipitation and evaporation, the heat flux associated with water transport across the ocean boundaries generally represents a global net heat loss for the ocean. The reason is that evaporation transfers water away from the ocean at a temperature typically higher than precipitation adds water. Delworth et al. (2006) estimate a global mean for this heat flux from a coupled climate model (see their Sect. 3), arriving at the value

\[ Q_{\text{advective}} \approx -0.15 \text{ W m}^{-2}. \]  

Likewise, Griffies et al. (2014) determine a heat flux for forced ocean-ice simulations to be (see their Appendix A.4)

\[ Q_{\text{advective}} \approx -0.30 \text{ W m}^{-2}. \]

Locally, the heat flux can be far larger in magnitude.

In a steady state, where the total ocean mass and heat content are constant, this heat loss due to advective mass transfer is compensated by ocean mass and heat transport. This ocean transport is in turn balanced by atmospheric transport. However, most atmospheric models do not account for heat content of its moisture field, and so the moisture field carries no temperature information. Hence, the atmospheric model represents only the moisture mass transport, but not the moisture heat content transport. The global heat budget is therefore not closed for these coupled climate models due to a basic limitation of the modelled atmospheric thermodynamics.

K1.7 Virtual salt fluxes

Some ocean models do not allow for the passage of water mass across the liquid ocean boundaries. Virtual salt fluxes are instead formulated to parameterize the effects of changes in salinity on the density field (Huang, 1993; Griffies et al., 2001; Yin et al., 2010b). The models that use virtual fluxes do not have a physically correct water cycle, as they have zero exchange of water between the ocean and other components of the climate system. Correspondingly, they do not have a physically correct salt budget, since the real ocean system has a trivial net flux of salt across the air–sea boundary, contrasting with the nontrivial virtual salt fluxes. Additionally, they are missing the Goldsborough–Stommel circulation (Goldsbrough, 1933; Stommel, 1957; Huang and Schmitt, 1993). Since virtual salt flux simulations are still in use, we continue to request that those models archive the relevant salt fluxes as part of CMIP6.

K2 Boundary mass fluxes

The water mass fluxes in Table K1 aim to present the analyst with sufficient information to perform a water mass budget on the liquid ocean, and to map regionally where water enters or leaves the ocean through various physical processes. The following presents some general comments.

- Liquid runoff is defined as liquid water that enters the ocean from land, such as through rainwater in rivers, or
Table K1. This table details the boundary fluxes of water mass to be saved from the ocean model component in CMIP6 simulations. Positive fluxes are into the ocean. Hence, for example, evaporating water represents a negative mass flux (this sign convention is opposite that for CMIP5). The column indicating the experiment for saving the diagnostics generally says “all”, in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCPP, ScenarioMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations. The Priority = 1 diagnostics should be saved as decadal time means at decadal intervals for the piControl spin-up. Entries with grids denoted “native/sphere” denote diagnostics where native and spherical output are recommended to facilitate analysis (see the discussion in Sect. A3). The bottom sub-table lists the relation between the CMOR name for a diagnostic and its CF standard name.

<table>
<thead>
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Snow and ice meltwater in rivers. It may also incorporate meltwater from sea ice, icebergs, and ice shelves.

– Absent an iceberg model, solid land ice is calved next to coasts and melted by the liquid ocean. It is important to record this melt field.

– An iceberg model exports a certain amount of calved land ice away from the coasts. It is thus important to record where the icebergs melt (horizontal position and depth), hence the suggestion to include iceberg melt in Table K1.

– Models that employ a virtual salt flux, and so do not allow for the transfer of water mass across the liquid ocean boundary, will have zero for each of these mass flux fields. In that case, the mass flux diagnostics should not be reported. Instead, see Sect. K3 for virtual salt fluxes diagnostics. Note that virtual salt flux models assume the virtual salt has zero mass.

We now present specifications for the diagnosed fields. As discussed in Sect. K1.1, the fluxes, which may be defined only over a portion of each ocean grid cell, are normalized by the full area of each ocean grid cell. As a result, multiplying the ocean grid cell horizontal area times the flux will render the mass per time of water entering or leaving an ocean grid cell.

– pr: mass flux of liquid precipitation from the atmosphere entering the ice-free portion of an ocean grid cell.

– prsn: mass flux of frozen precipitation (i.e. snow) from the atmosphere entering the ice-free portion of an ocean grid cell.

– evs: rate at which water crosses the air–sea interface due to evaporation and condensation, passing through the ice-free portion of an ocean grid cell. This flux is positive for water entering the liquid ocean through condensation and negative when leaving the ocean through evaporation. This sign convention is opposite to that used for CMIP5.

– friver: mass of liquid water runoff entering the ocean from land boundaries. This runoff is typically inserted.
into the top model grid cell. However, more recent development inserts the runoff as a lateral boundary condition which can generally take place at depth.

- iceberg: solid masses that enter the ocean from land–ocean boundaries will eventually melt in the ocean. This melt may occur just at the ocean–land boundary, be distributed seawards by a spreading scheme, or participate in the transport via icebergs. It may also be distributed with depth.

- fsitherm: contribution to liquid ocean mass due to the melt (positive mass flux) or freezing (negative mass flux) of sea ice.

- wfo: net flux of liquid water entering the liquid ocean.

- wfonocorr: mass flux due to physical processes absent the flux corrections. For models without flux corrections, wfonocorr = wfo.

- wfcorr: mass flux due to flux corrections. It is zero for models with no prescribed flux corrections/adjustments. However, for the CMIP6/FAFMIP experiment (Sect. 3.2), the prescribed perturbation water flux should be saved in the wfcorr diagnostic for FAFMIP models that make use of a real water flux.

The following equalities are satisfied by the requested water flux fields:

\[
\begin{align*}
\text{wfo} &= \text{wfonocorr} + \text{wfcorr}, \\
\text{wfonocorr} &= \text{pr} + \text{prsn} + \text{evs} + \text{friver} + \text{iceberg} + \text{fsitherm}. \\
\end{align*}
\]

(K3a) (K3b)

### K3 Boundary salt fluxes

The salt fluxes in Table K2 aim to present the analyst with sufficient information to perform a salt budget on the liquid ocean, and to map regionally where salt enters or leaves the ocean through various physical processes. The following presents some details about the fields. Note that for models using real water fluxes, the virtual salt flux fields are all zero, so that there is no reason to submit these diagnostics.

- vsfpr: virtual salt flux associated with liquid and solid precipitation.

- vsfevap: virtual salt flux associated with evaporation of water.

- vsfriver: virtual salt flux associated with liquid and solid runoff from land processes.

- vsfsit: virtual salt flux associated with melting or freezing of sea ice.

- vsf: total virtual salt flux entering the ocean. It is the sum of all of the above virtual salt fluxes, including the salt flux correction.

- vsfcorr: virtual salt flux arising from a salt flux correction. It is zero for models with no prescribed virtual salt flux correction/adjustment. For the CMIP6/FAFMIP experiment (Sect. 3.2) and for such models making use of a virtual salt flux, then the virtual salt flux corresponding to the prescribed perturbation water flux should be saved in the vsfcorr diagnostic.

- sfdsi: salt transport from sea ice to the ocean. The field arises since sea ice has a nonzero salinity, so it exchanges salt with the liquid ocean upon melting and freezing. This field is distinct from the virtual salt flux into seawater due to sea-ice thermodynamics.

- sfriver: salt content of rivers. This field is typically zero, though some river models carry a non-zero salt concentration.

### K4 Boundary heat fluxes

The following heat fluxes are summarized in Table K3. They present the analyst with sufficient information to perform a heat budget on the liquid ocean, and to map regionally where heat enters or leaves the ocean through various physical processes. We provide further details in the following.

- hfgeou: upward geothermal heat flux at the sea floor

- hfrainds: heat content of liquid (rain), liquid condensate (precipitating fog), and solid (snow) precipitation (relative to 0 °C)

- hfevapds: heat content of water leaving the ocean (relative to 0 °C) due to evaporation or sea-ice formation

- hfrunoffds: heat content of runoff in a liquid form (rivers) and solid form (calving land ice and icebergs) (relative to 0 °C)

- hfsifrazil: heat flux due to frazil ice formation

- hfsnthermds: latent heat flux due to snow melting

- hfibthermds: latent heat flux due to iceberg melting

- rlntds: surface net downward longwave flux

- hls: surface downward latent heat flux (from evaporating vapour and from melting solids)

- hfss: surface downward sensible heat flux (including both air–sea and ice–sea sensible heating)

- rsntds: net downward shortwave flux at seawater surface

- rsdo: downwelling shortwave flux in seawater

- hfcorr: heat flux correction

- hdfds: net downward heat flux at the sea surface (excluding any flux correction/adjustment)

\[25\text{Note there was a mistake in the CMIP5 Xcel spreadsheet, with rsdo incorrectly listed as rsds. In fact, rsds is an atmospheric field.}\]
Table K2. This table provides a summary of the boundary fluxes of salt mass that should be saved from the ocean model component in CMIP6 simulations. Positive fluxes are into the ocean. The column indicating the experiment for saving the diagnostics generally says “all”, in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCPP, ScenarioMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations. The Priority = 1 diagnostics should be saved as decadal time means at decadal intervals for the piControl spin-up. Entries with grids denoted “native/sphere” denote diagnostics where native and spherical output are recommended to facilitate analysis (see discussion in Sect. A3). The lower sub-table relates the CMOR name to its CF standard name.

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K5 Relations satisfied by the heat fluxes

We summarize here some relations satisfied by the diagnosed heat fluxes.

- net heat flux
  
The net heat flux crossing the bottom and surface boundaries of the liquid ocean is given by
  
  \[
  \text{net heat} = hfgeou + hfds + hfcorr. \tag{K4}
  \]

- surface heat flux without hfcorr
  
The net heat flux crossing the surface boundary of the liquid ocean, without flux adjustments, is given by
  
  \[
  hfds = hfrains + hfevapds + hfrunoffds
  + rhntds + hfls + hfss + rsnds
  + hfsifrazil. \tag{K5}
  \]
  
  This is a critical identity to verify prior to making use of the various surface heat flux components for analysis.

- latent heat flux
  
The net latent heat flux, hfls, contains contributions from the latent heat loss due to evaporating water, melting snow (hfsnthermds), melting icebergs (hfibthermds), and the melt/formation of sea ice.

  - Heat content of precipitation
    
The net heat content of precipitation, hfrains, contains contributions from the mass of liquid precipitation (rain), melting solid precipitation (snow), sea-ice melt, and condensed fog that falls into the ocean.

  - heat content of runoff
    
The net heat content of runoff, hfrunoffds, contains contributions from the mass of liquid runoff and solid runoff. The solid runoff may be exported from the coast via a spreading scheme and/or an iceberg model.

K6 Specifications for the boundary heat fluxes

We here provide further specification for these diagnostics.

K6.1 hfgeou

- hfgeou: geothermal heat flux
  
The geothermal heat flux is typically a static field. Models that use a time dependence should archive the monthly heat flux.
Table K3. This table provides a summary of the boundary fluxes of heat to be saved from the ocean component in CMIP6 simulations. Positive fluxes are into the ocean. The column indicating the experiment for saving the diagnostics generally says “all”, in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCPP, ScenarioMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations. The Priority=1 diagnostics should be saved as decadal time means at decadal intervals for the piControl spin-up. For the geothermal heating, most models use a static geothermal heating, in which case only one time step need be archived. If time-dependent, then monthly fields are requested. Note that many climate models place boundary fluxes at the ocean surface. However, more general couplings are being considered (e.g. a sea ice or ice shelf model that interacts with more than the surface ocean cell). To allow for such generality, we note that many of the fluxes can be three-dimensional. Note that the field “rsdo” was mistakenly included in the CMIP5 diagnostic excel spreadsheet as “rds”. Entries with grids denoted “native/sphere” denote diagnostics where native and spherical output are recommended to facilitate analysis (see discussion in Sect. A3). The lower sub-table relates the CMOR name to its CF standard name.

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K6.2 hfrainds

- hfrainds: heat content of liquid and solid precipitation with respect to 0°C

For many climate models, this diagnostic is estimated using ocean properties

\[ hfrainds(W/m^2) = c_p (Q_{\text{rain}} T_{\text{rain}} + Q_{\text{snow}} T_{\text{snow}}). \]  

(K6)

where \( Q_{\text{rain}} \) and \( Q_{\text{snow}} \) are the rain and snowfall mass fluxes, in kg/(m²s), \( T_{\text{rain}} \) is the temperature of rainfall in degrees Celsius, and \( T_{\text{snow}} \) is the temperature of snowfall in degrees Celsius. Most climate models choose the rainfall and snowfall temperature equal to the ocean sea surface temperature. An assumption is needed since atmospheric models do not generally carry the temperature of their moisture field, and so do not provide heat content for the rain and snow (see discussion in Sect. K1.6 and Appendix E).

The field hfrainds is zero for ocean models employing a virtual tracer flux, in which there is no mass or volume transport of water across the ocean surface.

K6.3 hfevapds

- hfevapds: heat content of water leaving the ocean, with respect to 0°C.
This diagnostic measures the heat content of water carried away from the liquid ocean via evaporation or sea-ice formation. This heat is distinct from latent heat flux, which arises from a phase change. Instead, this heat content can be computed with respect to 0 °C just as the diagnostic hfrainds. Here, if we make use of ocean fields, then

\[ h_{\text{evapds}} = c_{p} \left( Q_{\text{evap}} T_{\text{evap}} + Q_{\text{ice form}} T_{\text{ice form}} \right), \]  

(K7)

where \( Q_{\text{evap}} \) and \( Q_{\text{ice form}} \) are the evaporative and ice formation mass fluxes, in kg/(m\(^2\) s), \( T_{\text{evap}} \) is the temperature of evaporating water in degrees Celsius, and \( T_{\text{ice form}} \) is the temperature of water forming sea ice in degrees Celsius. These temperatures are typically approximated by the sea surface temperature from the ocean model.

The field \( h_{\text{evapds}} \) is zero for models employing a virtual salt flux, in which there is no mass transport of water across the ocean surface.

**K6.4 hfrunoffs**

- **hfrunoffs**: heat content of liquid runoff with respect to 0 °C

This diagnostic measures the heat content of liquid and solid runoff that enters the liquid ocean, with respect to 0 °C. This heat is typically estimated through use of ocean properties via

\[ h_{\text{runoffds}} = c_{p} \left( Q_{\text{runoff}} T_{\text{runoff}} + Q_{\text{icebers}} T_{\text{icebers}} \right), \]  

(K8)

where \( Q_{\text{runoff}} \) and \( Q_{\text{icebers}} \) are the liquid and solid runoff mass fluxes, in kg/(m\(^2\) s), \( T_{\text{runoff}} \) is the temperature of liquid runoff in degrees Celsius, and \( T_{\text{icebers}} \) is the temperature of solid runoff in degrees Celsius.

The field \( h_{\text{runoffds}} \) is zero for models employing a virtual tracer flux, in which there is no mass transport of water across the ocean surface.

**K6.5 hfsifrazil**

- **hfsifrazil**: frazil heat flux

As the temperature of seawater cools to the freezing point, sea ice is formed, initially through the production of frazil. Operationally in an ocean model, liquid water can be supercooled at any particular time step through surface fluxes and transport. An adjustment process heats the liquid water back to the freezing point, with this positive frazil heat flux extracted from the ice model as frazil sea ice is formed. This term is necessary to close the heat budget of the liquid ocean.

**K6.6 hfsntermds**

- **hfsntermds**: latent heat of fusion required to melt snow

Snow entering the liquid ocean melts upon obtaining the latent heat of fusion from the ocean. This latent heat loss by the liquid ocean is what is archived in hfsntermds. Note that hfsntermds is also included as part of the net latent heat flux diagnostic hfls.

**K6.7 hfibthermds**

- **hfibthermds**: latent heat of fusion required to melt calving land ice and/or icebergs

Icebergs transport calved land ice from the land into the ocean. A rudimentary “iceberg” model may simply be the insertion of calving land ice/snow into the ocean, with an associated mass and heat transport (heat content of ice plus heat of fusion required to melt the ice). More realistic iceberg models are now becoming more common (Jongma et al., 2009; Martin and Adcroft, 2010; Marsh et al., 2015; Merino et al., 2016). Melting of the icebergs into the liquid ocean is associated with a transfer of the latent heat of fusion from the liquid ocean, and so represents a cooling of the liquid ocean in regions where the icebergs melt. It is this heat flux that is archived in hfibthermds.\(^{26}\) Note that hfibthermds is also included as part of the net latent heat flux diagnostic hfls.

**K6.8 rlntds**

- **rlntds**: downward flux of longwave radiation

This diagnostic measures the net downward flux of longwave radiation that enters the liquid ocean. Negative values cool the ocean.

**K6.9 hfls**

- **hfls**: latent heat flux

This diagnostic provides the net latent heat flux, including contributions from latent heat loss due to evaporating water, melting snow (hfsntermds), melting icebergs (hfibthermds), and the melt/formation of sea ice. Negative values cool the ocean, as occurs when liquid water evaporates or ice and snow melts.

**K6.10 hfss**

- **hfss**: sensible heat flux

This diagnostic measures the net downward flux of sensible heat acting on the liquid ocean. Positive values warm

---

\(^{26}\)In testing the NEMO-ICB iceberg model, Marsh et al. (2015) considered icebergs with zero heat capacity. However, heat conservation in the coupled climate system requires that the latent heat of fusion used to create the ice on land must be given up by the liquid ocean as the icebergs melt. Consequently, icebergs with zero heat capacity should not be used in a coupled climate simulation for CMIP6. In fact, the nonzero heat capacity of icebergs is now included in the NEMO-ICB for use in CMIP6 (Robert Marsh, personal communication, 2016).
the ocean and negative values cool. The physical processes contributing to this turbulent heat flux include air–sea and ice–sea interactions.

K6.11 rsntds

- rsntds: shortwave radiative flux at top of ocean

This diagnostic measures the net downward flux of shortwave radiation at the top of the ocean surface. Positive values warm the ocean.

K6.12 rsdo and rsdoabsorb

- rsdo: downwelling shortwave flux in seawater
- rsdoabsorb: net rate of absorption of shortwave energy in the ocean layer

Shortwave radiation penetrates into the ocean column and so heats the ocean interior (see Fig. L1). The field rsdo measures the shortwave heat flux at the bottom of a tracer grid cell face. The field rsdoabsorb is the vertical convergence of rsdo, and is requested for the heat budget in Table L1.

Theoretical considerations

The parameterization of oceanic absorption of downward solar radiation is generally written as

\[ \text{rsdo} = I_{\text{penetrate}}(x, y, z) = I_{\text{down}}(x, y) \mathcal{F}(z), \]  

where \( I_{\text{down}} \), in units of W m\(^{-2}\), is the downwelling shortwave radiative heat per unit area incident at the ocean surface, and \( \mathcal{F}(z) \) is a dimensionless attenuation function that depends on seawater optical properties.

Some models equate the downwelling shortwave, \( I_{\text{down}} \), to the net incoming shortwave radiation, \( I_{\text{net}} = \text{rsntds} \). However, some models decompose the net shortwave into downwelling and non-downwelling contributions

\[ \text{I}_{\text{net}} = \text{I}_{\text{down}} + \text{I}_{\text{non-down}}. \]  

Again, \( I_{\text{down}} \) is the downwelling radiation that participates in shortwave penetrative radiation according to Eq. (K9). In contrast, the non-downwelling portion, \( I_{\text{non-down}} \), is deposited directly into the skin layer of the upper ocean (generally assumed to be in the upper ocean model grid cell), so that \( I_{\text{non-down}} \) does not participate in the downwelling penetrative radiation.

Penetrative shortwave fluxes affect the heat budget according to

\[ \text{rsdoabsorb}_k = e^0 \left( \frac{\partial (\Theta \rho dz)}{\partial t} \right)_k \]  

\[ = (I_{\text{penetrate}} - I_{\text{penetrate}}) \]  

\[ = \text{rsdo}_{k-1} - \text{rsdo}_k, \]  

where \( k \) is the discrete vertical index increasing downward, and \( \text{rsdo}_k = I_{\text{penetrate}} \) is the penetrative shortwave heat flux at the bottom of tracer cell \( k \). The penetrative shortwave flux entering the top of a cell, \( I_{\text{penetrate}} \), is larger than the flux leaving the cell bottom, \( I_{\text{penetrate}} \), so that shortwave radiation is deposited within a tracer cell. The net shortwave absorbed by the tracer cell, rsdoabsorb, is asked for in the heat budget Table L1. Assuming a zero penetrative heat flux through the ocean bottom, \( \text{rsdo}_{k_{\text{max}}} = 0 \), we can infer the flux field \( \text{rsdo}_k \) by integrating the convergence field \( \text{rsdoabsorb}_k \) upwards

\[ \text{rsdo}_{k-1} = \text{rsdo}_k + \text{rsdoabsorb}_k. \]  

We note here a peculiarity of penetrative shortwave heating implemented in some models. Namely, the net downwelling radiation at the top of the ocean, \( I_{\text{down}} \), is sometimes included as part of the surface boundary condition portion of the code, rather than as part of the penetrative shortwave code. If this convention is followed, then rsdoabsorb will be negative (i.e. cooling) in the \( k = 1 \) grid cell, since in this case the \( I_{\text{down}} \) contribution is part of rsntds. When performing a heat budget, care should be exercised to not double-count, or conversely to not account for, the contribution of \( I_{\text{down}} \) to the \( k = 1 \) cell. We discuss this point further in Sect. L4.9.

K6.13 hfcorr

- hfcorr: heat flux correction

This diagnostic records the heat flux correction acting at the liquid ocean surface. This field is zero for nearly all CMIP6 models. However, for the CMIP6/FAFMIP experiment (Sect. 3.2 and Gregory et al., 2016), the prescribed FAFMIP perturbation heat should be saved in the hfcorr diagnostic (see Table K3).

K6.14 hfds

- hfds: net surface downward heat flux at sea surface, excluding any flux correction/adjustment

This diagnostic measures the net heat flux passing across the ocean upper surface due to radiative, turbulent, latent, frazil, and heat content fluxes. It is related to the other diagnostic heat fluxes through Eq. (K5). It does not include any heat flux correction/adjustment.

K7 Boundary fluxes of momentum

- tauuo: downward surface x-stress
- tauvo: downward surface y-stress
- taucorr: downward surface x-stress correction/adjustment
- taucorr: downward surface y-stress correction/adjustment

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L.1 Tracer budgets for a grid cell

To help ensure proper archival and use of heat and salt budget terms, we provide here a tutorial for tracer budgets in a discrete ocean model, with this discussion following the finite volume formulation in Appendix F. This formulation leads to the following semi-discrete equations used as the basis for an ocean model tracer budget in surface, interior, and bottom grid cells, respectively:

\[
\frac{\partial (C \rho \, dz)}{\partial t} = -\nabla_s \cdot [\rho \, dz \, (u \, C + \rho \, F)] + \left[ (w \, \rho \, C + \rho \, F^{(s)}) \right]_{s = s_k} - \left[ (w \, \rho \, C + \rho \, F^{(s)}) \right]_{s = s_{k-1}} + Q^{(C)}_{\text{advect}} + Q^{(C)}_{\text{non-advect}} + S^{(C)}, \quad (L1)
\]

\[
\frac{\partial (C \rho \, dz)}{\partial t} = -\nabla_s \cdot [\rho \, dz \, (u \, C + F)] - \left[ \rho \, (w \, C + F^{(s)}) \right]_{s = s_k} + \left[ \rho \, (w \, C + F^{(s)}) \right]_{s = s_{k-1}} + \rho \, F^{(s)} + S^{(C)}, \quad (L2)
\]

\[
\frac{\partial (C \rho \, dz)}{\partial t} = -\nabla_s \cdot [\rho \, dz \, (u \, C + F)] - \left[ \rho \, (w \, C + F^{(s)}) \right]_{s = s_{k-1}} + \rho \, F^{(s)} + S^{(C)} \quad (L3)
\]

These budgets are formulated as finite volume contributions to the tracer mass (or heat) per horizontal area of a grid cell, with the horizontal area of the grid cell assumed constant in time. The left-hand side of these equations represents the net time tendency for the tracer content in a grid cell, per horizontal area of the cell. The right-hand side arises from the convergence of advective and subgrid-scale fluxes crossing the faces of a grid cell, as well as boundary fluxes and sources.

Appendix L: Diagnostics of budget terms for heat and salt

Heat and salt budget terms facilitate mechanistic information about model behaviour. Studies such as Gregory (2000), Piecuch and Ponte (2011), Palter et al. (2014), Buckley et al. (2015), Griffies et al. (2015), Exarchou et al. (2015), Kuhlbrodt et al. (2015), and Morrison et al. (2016) illustrate the value for physical interpretation provided by budget terms. The bulk of the science resulting from these budgets has thus far come from use of the annual mean fields, hence we request annual means, with these fields being Priority = 1 for FAFMIP (Gregory et al., 2016) and Priority = 3 for other experiments. Additionally, FAFMIP requests monthly mean fields at Priority = 2 in order to study seasonal variations of the budget terms.

These fluxes are summarized in Table K4. They quantify the net momentum imparted to the liquid ocean surface, with positive values accelerating the liquid ocean in the noted direction. These stresses arise from the overlying atmosphere, sea ice, icebergs, ice shelf, etc. For models that do not apply a stress flux correction/adjustment, they will not report any diagnostics for either taupor or taupcor. However, for the CMIP6/FAFMIP experiment (Sect. 3.2 and Gregory et al. (2016)), the prescribed perturbation wind stress should be saved in the taupor and taupcor diagnostics.

A schematic of ocean model grid cells over an ocean column is shown in Fig. L1. Grid cells generally have a non-constant thickness and non-constant density (although Boussinesq budgets have a constant density factor \( \rho \rightarrow \rho_o \)). The lateral convergence operator acting on an advective or
Table K4. This table presents the net surface stress applied at the liquid ocean surface due to air–sea plus ice–sea interactions. Positive fluxes accelerate the ocean in the given direction. The column indicating the experiment for saving the diagnostics generally says “all”, in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCPP, ScenarioMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations. The units N m$^{-2}$ are identical to Pascal. The lower sub-table relates the CMOR name to the CF standard name.

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Subgrid-scale flux is formulated numerically so that multiplication by the respective area of a grid cell face leads to a difference operator acting on the lateral flux components crossing the tracer grid cell faces. That is, the numerical discretization satisfies Gauss’s Law (Sect. L9), as doing so allows us to retain the familiar finite volume budgets within the numerical model. We now detail terms in these budgets.

- $C$ is the potential (or Conservative) temperature of a grid cell, or the mass of tracer (e.g. salt or another material tracer) per mass of seawater within the cell (i.e. tracer concentration).

- $\rho \, dz$ is the mass of seawater per horizontal area in a grid cell, with $\rho$ the in situ density and $dz$ the thickness. For Boussinesq models, the $\rho$ factor is replaced by a constant reference density $\rho_0$ (rhozero in Sect. G). Furthermore, for Boussinesq models with fixed grid cell thicknesses (Sect. G8), the thickness factor $dz$ is a temporal constant.

- The product $C \, \rho \, dz$ is the mass per unit horizontal area of a grid cell if $C$ is a material tracer such as salinity. Since the horizontal area of the cell is constant in time, we may multiply by the horizontal area to recover a budget for the tracer mass in the cell.

- The product $C \, \rho \, dz$ is the heat per horizontal area if $C$ is potential or Conservative Temperature multiplied by the heat capacity. Since the horizontal area of the cell is constant in time, we may multiply by the horizontal area to recover a budget for the heat within the grid cell, in SI units of Joule.

- The generalized vertical coordinate is denoted by $s$, and its discrete values $s_k$ determine the vertical grid cell.

- The horizontal velocity component is $u$ (oriented perpendicular to $\hat{z}$). The dia-surface component is $w = (\partial z/\partial s) \, Ds/Dt$, with $D/Dt$ the material time derivative.

- The horizontal subgrid-scale transport is $\rho \, F$ and the dia-surface component is $\rho \, F(s)$.

- Tracer flux associated with the boundary water flux is accounted for by the term $Q^{(C)}_{\text{advect}}$. In particular, this term accounts for the heat content of the mass crossing the ocean surface, with discussion of this term given in Sects. K4, K5, and K6.

- $Q^{(C)}_{\text{bot}}$ is the flux of tracer passed into the liquid ocean through the solid bottom boundary, such as through geothermal heating (Sect. K4).

- $Q^{(C)}_{\text{non-advect}}$ is the non-advective flux of tracer crossing the ocean surface boundary. The sign is defined so that a positive value represents a flux of tracer into the ocean, e.g. positive sign adds heat, salt, carbon, or other tracers to the ocean. For the heat budget, this term arises from such terms as shortwave, longwave, latent, and sensible heat fluxes (Sect. K4).

- $S^{(C)}$ is the tracer source term, which is critical for biogeochemical tracers as per the biogeochemical portion of OMIP (Orr et al., 2016). Sources are zero for heat and salt. Notably, CMIP6 models generally do not include Joule heating from frictional dissipation of kinetic energy.
Table L1. This table summarizes fields that support the study of three-dimensional ocean heat and salt budgets, listing here terms contributing to the time tendency of heat and salt in a model grid cell, mass and thickness of a cell, and depth-integrated heat and salt. Annual means fields are Priority = 1 for the FAFMIP experiment (Gregory et al., 2016), whereas the monthly means are Priority = 2. For all other experiments, the annual means are Priority = 3, as listed here. For models with prognostic temperature given by potential temperature, then these models should fill the potential_temperature fields and leave the conservative_temperature fields blank; conversely for models with Conservative Temperature as the prognostic temperature field. The column indicating the experiment for saving the diagnostics generally says “all”, in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCPP, ScenarioMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations. The lower sub-table lists the CMOR names and the corresponding CF standard names.

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L4.1 Net tendency of heat and salt in a grid cell

We request the mass-weighted depth-integrated prognostic temperature. For models using potential temperature as their prognostic temperature field, the relevant diagnostic is opotentmpmint; for models that use Conservative Temperature as their prognostic temperature field (see Appendix D), the diagnostic is ocontempmint. These diagnostics are computed as a depth-integrated sum

\[
\text{ocontempmint} = \sum_k \Theta \rho \, dz,
\]

\[
\text{opotentmpmint} = \sum_k \theta \rho \, dz,
\]

where the in situ density factor, \(\rho\), is set to the reference density, \(\rho_o\) (rhzero in Table G1), for Boussinesq fluids, and where \(\theta\) is potential temperature and \(\Theta\) is Conservative Temperature, \(\Theta\).

L4 Processes diagnosed for heat and salt budgets

There are numerous physical processes contributing to the evolution of heat and salt in a grid cell. It is not practical to request all such terms for CMIP. Rather, we aim to archive a suite of terms whose physical content is both interesting and generally nontrivial. In addition to the boundary salt fluxes detailed in Sect. K1, and the boundary heat fluxes and penetrative shortwave radiation detailed in Sect. K4, we recommend archiving the following three-dimensional terms associated with advective and parameterized subgrid-scale transport. For the heat budget terms, save the potential temperature terms if that is the model prognostic temperature, otherwise save the Conservative Temperature terms.

L4.1 Net tendency of heat and salt in a grid cell

- \text{opotentmpmint}: net time tendency for heat (via potential temperature) in a grid cell due to all processes.
- \text{ocontempmint}: net time tendency for heat (via Conservative Temperature) in a grid cell due to all processes.
- \text{osalttend}: net time tendency for salt in a grid cell due to all processes.

This term captures the net time tendency for heat and salt within a grid cell arising from all processes. For potential temperature, this term takes the form

\[
opotentmpmint = c_p \left( \frac{\partial (\theta \rho \, dz)}{\partial t} \right),
\]

and likewise for Conservative Temperature and salinity. It is crucial that this term encompass all processes affecting the tracer, as its residual from other diagnosed terms will be used to infer contributions from unsaved processes.

L4.2 Residual mean advection

- \text{opottemppradvect}: convergence of residual mean advectivefluxes of heat (via potential temperature)
- \text{ocontemppradvect}: convergence of residual mean advectivefluxes of heat (via Conservative Temperature)
- \text{osaltpradvect}: convergence of residual mean advectivefluxes of salt

This term measures the time tendency of heat and salt due to the three-dimensional convergence of fluxes from the residual mean velocity, \(n^t = n + n^*,\) where \(n^*\) is the parameterized eddy-induced advection velocity, including both mesoscale and submesoscale processes (see Sect. I1). If there are no eddy-adective parameterizations, then \(n^* = 0\), in which case advection occurs solely from the resolved model prognostic velocity.

L4.3 Net parameterized eddy advection

- \text{opottemppadvec}: convergence of parameterized eddy advective fluxes of heat (via potential temperature)
- \text{ocontemppadvec}: convergence of parameterized eddy advective fluxes of heat (via Conservative Temperature)
- \text{osaltpadvec}: convergence of parameterized eddy advective fluxes of salt

This term measures the time tendency of heat and salt due to the convergence of three-dimensional fluxes from just the parameterized eddy-induced velocity. The eddy-induced velocity can arise from mesoscale, submesoscale, and/or other processes. Notably, the eddy advection parameterizations can be implemented either as a traditional advection process, or as a skew transport, with their convergence the same in the continuum (Griffies, 1998). If there are no eddy advection parameterizations, then \(n^* = 0\), in which case this budget term is absent.

L4.4 Parameterized submesoscale eddy advection

- \text{opottempsmadvec}: convergence of parameterized submesoscale eddy-advective fluxes of heat (via potential temperature)
– ocontemppsmadvect: convergence of parameterized submesoscale eddy-advective fluxes of heat (via Conservative Temperature)
– osaltpsmadvect: convergence of parameterized submesoscale eddy-advective fluxes of salt

This term measures the time tendency of heat and salt due to the convergence of three-dimensional fluxes from just the submesoscale eddy parameterization. The canonical form for this closure is that from Fox-Kemper et al. (2008) and Fox-Kemper et al. (2011). Note that Bachman and Fox-Kemper (2013) propose a diffusive component to the submesoscale parameterization. However, we know of no model making use of this scheme for CMIP6.

Note that if only mesoscale plus submesoscale processes contribute to the eddy-induced advective transport, then knowledge of the net parameterized eddy advective transport, opottemppadvect for example, as well as the submesoscale contribution, ocontemppadvect, allows for the mesoscale contribution to be inferred by subtraction.

L4.5 Parameterized mesoscale diffusion

– opottemppmdiff: convergence of parameterized mesoscale eddy-diffusive fluxes of heat (via potential temperature)
– ocontemppmdiff: convergence of parameterized mesoscale eddy-diffusive fluxes of heat (via Conservative Temperature)
–osaltpmdiff: convergence of parameterized mesoscale eddy-diffusive fluxes of salt

This term measures the time tendency from the convergence of parameterized diffusive fluxes associated with mesoscale closures. Such diffusion is usually oriented according to neutral directions or isopycnal directions (Solomon, 1971; Redi, 1982; Griffies et al., 1998). We note the added complexity associated with the use of an implicit time stepping for the diagonal vertical portion of the rotated diffusion tensor (Cox, 1987; Griffies et al., 1998). Care should be exercised to include this portion of the rotated diffusion as part of this online diagnostic calculation.

L4.6 Parameterized vertical and dia-neutral diffusion

– opottempdiff: convergence of parameterized dia-neutral/vertical diffusive fluxes of heat (via potential temperature)
– ocontempdiff: convergence of parameterized dia-neutral/vertical diffusive fluxes of heat (via Conservative Temperature)
– osaltdiff: convergence of parameterized dia-neutral/vertical eddy-diffusive fluxes of salt

This term measures the time tendency from the convergence of parameterized fluxes associated with dia-neutral (or diapycnal) processes as well as vertical boundary layer processes. These parameterizations are generally implemented as down-gradient diffusion. In addition, this term can include mixing due to vertical convective adjustment. This budget term includes

1. convection via an enhanced vertical diffusivity;
2. convection via a convective adjustment scheme (e.g. Rahmstorf, 1993);
3. boundary layer mixing (e.g. Large et al., 1994);
4. interior shear-driven mixing (e.g. Pacanowski and Philander, 1981; Jackson et al., 2008);
5. gravity wave-induced mixing (e.g. Simmons et al., 2004; Jayne, 2009; Melet et al., 2013);
6. static background diffusion (e.g. Bryan and Lewis, 1979); and
7. other vertical diffusion processes.

L4.7 Remaining processes

Contributions from remaining processes can be inferred as a residual by taking the difference of all diagnosed processes from the net tendency. Residual processes may include non-local KPP mixing (Large et al., 1994), mixing from overflow schemes (e.g. Beckmann and Döscher, 1997; Campin and Goosse, 1999; Danabasoglu et al., 2010; Bates et al., 2012), and mixing across unresolved straits (e.g. see Sect. 3.5 of Griffies et al., 2005).

L4.8 Penetrative shortwave radiation

Heat absorbed in a tracer cell due to penetrative shortwave radiation is saved in the rsdoabsorb diagnostic. This diagnostic is discussed in Sect. K6.12.

L4.9 Summary heat budget

The heat budget (via potential temperature or Conservative Temperature) for a surface grid cell is dependent on how shortwave radiation is treated (see discussion in Sect. K6.12). For models where the shortwave at the top of the ocean, rsntsds, is included only in hfds, not in rsdoabsorb, then the surface grid cell budget takes the form

\[ \text{opottemptend} = \text{hfds} + \text{rsdoabsorb} + \text{opottemppadvect} + \text{opottemppmdiff} + \text{opottempdiff} + \text{other.} \]  

(L5)

A complement treatment assumes that all of the surface shortwave flux, rsntsds, participates in penetrative shortwave
heating (see Sect. K6.12). In this case, rsdoabsorb accounts for the shortwave flux converging into the top cell. Consequently, the surface grid cell balance (L5) reads

\[
opottempdelt = \text{hfds} + (\text{rsdoabsorb} - \text{rsntds})
+ \text{opottempadvect}
+ \text{opottemppmdiff} + \text{opottempdiff}
+ \text{other.} \tag{L6}
\]

The budget for an interior grid cell is realized by removing the net surface heat flux hfds (Sect. K4). The budget for a bottom grid cell is the same, with hfds replaced by the bottom geothermal heat flux, hfgeou. The budget for salt is analogous, yet without the penetrative shortwave heat flux, rsdoabsorb, nor the bottom geothermal heat flux.

**L.5 Conventions for the heat budget terms**

Following from the tracer budget given by Eqs. (L1)–(L3), all heat budget terms take the form

\[
Q_{\text{process}(n)}^{(\Theta)} = c_p \left( \frac{\partial (\rho \ dz \ \Theta)}{\partial t} \right)_{\text{process}(n)}, \tag{L7}
\]

where \( n \) labels the particular physical process. The physical units for the heat budget terms are thus given by

\[
Q_{\text{process}(n)}^{(\Theta)} \equiv \text{W m}^{-2}. \tag{L8}
\]

The area normalization for each budget term corresponds to the horizontal area of the tracer grid cell. Multiplication of any budget term by the tracer grid cell horizontal area thus yields the heat content change for that grid cell in units of watts.

**L.6 Conventions for the salt budget terms**

Following from the tracer budget given by Eqs. (L1)–(L3), all salt budget terms for archiving into CMIP take the general form

\[
Q_{\text{process}(n)}^{(S)} = \frac{1}{1000} \left( \frac{\partial (\rho \ dz \ S)}{\partial t} \right)_{\text{process}(n)} \quad \text{kg m}^{-2} \text{s}^{-1}, \tag{L9}
\]

where \( S \) is the salinity in units of ppt = gram of salt per kilogram of seawater or psu, depending on the model salinity field (see Appendix D), and \( n \) labels the particular physical process. Division by 1000 converts grams to kilograms. Multiplication of any budget term by the tracer grid cell horizontal area thus yields the salt content change for that grid cell in units of kilogram per second.

\^\footnote{We use \( \Theta \) in this section, as appropriate for TEOS-10 models. For pre-TEOS-10 models, they should archive tendencies appearing in the potential temperature, \( \theta \) equation. See Appendix D for discussion of seawater thermodynamics.}

**L.7 Temperature tendency terms**

The heat budget term (Eq. L7) scales according to the thickness of a cell. This is expected, since the budget determines the change in heat content per horizontal area of a cell, and this is the prognostic term in the ocean model.

For diagnostic purposes, it may be useful to consider a temperature tendency corresponding to the heat budget terms, with the temperature tendency in units of \( ^\circ \text{C} \text{s}^{-1} \). Doing so removes dependence on the grid cell thickness. That is, we may choose to consider the tendency for an intensive quantity, temperature, rather than the budget for an extensive quantity, heat. For this purpose, we recommend dividing the heat budget terms in Eq. (L7) by the annual mean mass per horizontal area of a grid cell, according to

\[
\delta \Theta_{\text{process}(n)} = \frac{Q_{\text{process}(n)}^{(\Theta)}}{c_p \rho \ dz} \quad \text{[\( \equiv \) \( ^\circ \text{C} \text{s}^{-1} \).} \tag{L10}
\]

The factor \( \rho \ dz \) is the annual mean mass per unit area of a grid cell (masscello), requested in Sect. H3. In this way, we can map vertical sections of the tendency terms and thus remove dependence on the grid cell thicknesses. Note that for a Boussinesq model with grid cell thicknesses that are time-independent (Sect. G8), temperature tendency terms are trivially related to the heat budget terms.

**L.8 Salinity tendency terms**

Likewise, we may convert the salt budget terms into salinity tendencies in units of ppt s\(^{-1}\). For this purpose, we may divide the salt budget terms in Eq. (L9) according to

\[
\delta S_{\text{process}(n)} = \frac{Q_{\text{process}(n)}^{(S)}}{\rho \ dz} \quad \text{[\( \equiv \) ppt s}^{-1}.} \tag{L11}
\]

The \( \rho \ dz \) array is the annual mean mass per unit area of a grid cell, requested in Sect. H3. Note that for a Boussinesq model with grid cell thicknesses that are time-independent, salinity tendency terms are trivially related to the salt budget terms.

**L.9 Diagnosing a flux vector versus a flux convergence**

In the mechanistic analysis of budgets, one is often interested in assessing budgets over a region, such as an ocean basin or within a subregion of a basin. These regional budgets help to identify dominant processes contributing to changes in heat and salt within the region, which in turn can help characterize physical mechanisms. For many purposes, this sort of analysis may involve characterizing the fluxes of heat and salt crossing the regional boundaries, in which case the three components of a flux vector may be required.

However, it is ultimately the convergence of a flux vector into a region that causes the change in heat or salt in that region. Additionally, fluxes remain arbitrary up to the curl of a vector since the curl has zero convergence. One therefore
must be careful when focusing an analysis on fluxes. Further words of caution are summarized in the appendix of Gregory (2000), who studied global and regional heat budgets, as well as in the study of equatorial Pacific heat budgets by Lee et al. (2004).

We are not advocating outright abandonment of flux components for mechanistic analyses, rather cautioning in their use absent consideration of their convergences into a region. It is largely for this reason that we prefer saving budget terms comprised of the convergence of fluxes associated with various physical processes. Besides saving archive space relative to saving fluxes (by a factor of 3), we are assured that the budget analysis is making use of terms that directly contribute to the changes in heat and salt within a region.

We furthermore note that integration of the divergence over a region leads, through Gauss’s Law, to the sum of the fluxes crossing the boundary of the region

$$\int \int \int \nabla \cdot \mathbf{F} \, dV = \int \int \limits_{\partial \mathcal{R}} \mathbf{\hat{n}} \cdot \mathbf{F} \, dS,$$

where \( \mathcal{R} \) is an arbitrary volume of fluid, \( \partial \mathcal{R} \) is the boundary of \( \mathcal{R} \), and \( \mathbf{\hat{n}} \) is the outward normal on the boundary. Hence, by integrating a flux divergence (negative of the convergence) over a chosen volume (left-hand side), one can garner mechanistic insight into the impacts from various physical processes in that region, without having to make direct use of flux components (right-hand side).

### Appendix M: Diagnostics of vertical/dianeutral subgrid-scale parameterizations

In Table M1, we present fields to help characterize subgrid-scale (SGS) parameterizations and their impact on the simulation, with focus on the vertical/dianeutral.

#### M1 Vertical/dianeutral tracer diffusivities

- difvho: total vertical heat diffusivity
- difvso: total vertical salt diffusivity

Vertical/dianeutral tracer diffusivities used in modern CMIP models typically consist of a static background value and a dynamically determined value. For the background diffusivity, some modellers choose a globally constant value, whereas others impose spatial dependence. There is evidence that the background diffusivity influences such processes as tropical currents (Meehl et al., 2001), and overturning strength (Bryan, 1987) in model simulations.

There are an increasingly large number of physical processes used by CMIP-class models that affect the vertical tracer diffusivity. For example, vigorous mixing processes in the upper ocean are associated with large mixing coefficients; more quiescent processes in the ocean pycnocline lead to much smaller coefficients; and enhanced mixing near the ocean bottom generally increases the mixing coefficients. The background, tidal, and boundary layer diffusivities are the same for temperature, salinity, and other tracers. However, the total diffusivities may differ if including a parameterization of double diffusive processes. We request archival of just the net heat diffusivity in difvho and salt diffusivity in difvso.

#### M2 Rate of work against stratification

- \( \text{tpeno} \): tendency of potential energy due to vertical mixing

##### M2.1 Summary of the diagnostic

A vertical/dianeutral diffusivity impacts the solution predominantly where there are nontrivial vertical tracer gradients. A measure of the impact can be deduced by mapping the rate at which work is done against the stratification by the tracer diffusivity. This work against stratification also impacts the potential energy budget. We recommend mapping this work rate per horizontal area as a depth integrated two-dimensional field.

##### M2.2 Theoretical considerations

The non-negative rate of work done against stratification by vertical/dianeutral diffusion of density is given by

$$\mathcal{P} \equiv \int \kappa_d N^2 \rho \, dV,$$

where \( N^2 \) is the squared buoyancy frequency (see the ob-vfsq diagnostic discussed in Sect. H22), and \( \kappa_d \) is the vertical/dianeutral diffusivity. Equation (M1) assumes the heat and salt diffusivities are the same, which is the case for tidal and background diffusivities. However, the full heat diffusivity, \( \kappa_d^H \), and salt diffusivity, \( \kappa_d^S \), can differ through effects from double diffusion. In this case, we split the integral as

$$\mathcal{P} \equiv -g \int \left( \kappa_d^H \frac{\partial \rho}{\partial \theta} \frac{\partial \theta}{\partial z} + \kappa_d^S \frac{\partial \rho}{\partial S} \frac{\partial S}{\partial z} \right) dV.$$  

(M2)

This term should be archived as a two-dimensional map of depth-integrated mixing work:

$$\text{tpeno} = -g \int_{-H}^{\eta} \left( \kappa_d^H \frac{\partial \rho}{\partial \theta} \frac{\partial \theta}{\partial z} + \kappa_d^S \frac{\partial \rho}{\partial S} \frac{\partial S}{\partial z} \right) dz.$$  

(M3)

Multiplication by the horizontal grid area, then summing over the globe, provides the global amount of work done by vertical mixing.
Table M1. This table summarizes diagnostics that support the study of vertical/dianeutral subgrid-scale (SGS) parameterizations. The column indicating the experiment for saving the diagnostics generally says “all”, in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCPP, ScenarioMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations. We ask only for annual means from these fields, rather than the monthly means requested for most other diagnostics. Additionally, this table has been reduced from the 12 fields requested in CMIP5 to the 3 requested here. Furthermore, the field tnpeo was requested as a three-dimensional field in CMIP5, whereas for CMIP6 it is requested as a depth-integrated two-dimensional field. The lower sub-table lists the CMOR names and the corresponding CF standard names.

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Appendix N: Diagnostics of lateral subgrid-scale parameterizations

We now detail diagnostics helping to characterize lateral subgrid-scale (SGS) parameterizations, with Table N1 summarizing the diagnostics. As for the vertical/dianeutral SGS parameterizations, we propose that dominant scientific use of the fields discussed in this subsection are realized by archiving just the annual mean fields.

N1 Lateral tracer diffusivities

- diftrelo: diffusivity for parameterized epineutral mesoscale eddy-induced Laplacian diffusion

- diftrblo: diffusivity for parameterized mesoscale eddy-induced advection

These diffusivities are used for neutral diffusion (Solomon, 1971; Redi, 1982), and eddy-induced advective transport (Gent et al., 1995).

N2 Eddy kinetic energy source from mesoscale parameterization

- tknebto: tendency of eddy kinetic energy from parameterized eddy advection

An energetic analysis of the extraction of potential energy by the Gent et al. (1995) scheme indicates that it affects an increase in the eddy kinetic energy (Aiki and Richards, 2008; Eden and Greathatch, 2008; Marshall and Adcroft, 2010). The rate of eddy kinetic energy increase, per unit horizontal area over an ocean column, is

\[ \text{tknebto} = \int_{-H}^{\eta} \kappa \left( N S \right)^2 \rho \, dz. \]  

(N1)

In this expression, \( N \) is the buoyancy frequency, \( S \) is the magnitude of the neutral slope, \( \kappa \) is the diffusivity setting the overall strength of the parameterization, and \( \rho \, dz \) is the grid cell mass per horizontal area, with \( dz \) the cell thickness. In a Boussinesq model, the in situ density factor should be set to the constant Boussinesq reference density \( \rho_0 \) used by the model (see rhozero in Table G1). Note that the CMIP5 request asked for the full three-dimensional field, whereas for CMIP6 we only ask for the depth-integrated two-dimensional field to reduce the archive burden.

Horizontal maps of the column-integrated work from the mesoscale parameterization (N1) can be readily compared across the suite of CMIP models. This depth-integrated field also provides a means for directly comparing the work done by vertical diffusion (Sect. M2). Furthermore, multiplication by the horizontal grid area, and then summing over the globe, provides the global amount of work associated with the scheme.

N3 Lateral momentum viscosities

- difmxylo: Laplacian viscosity

- difmxybo: biharmonic viscosity

These viscosities are generally time-dependent. Note that we do not make the distinction between various methods used to compute the lateral momentum viscosities. Hence, we only recommend the total viscosities be archived from ocean models in CMIP6.

N4 Kinetic energy dissipation by lateral viscosity

- dispkexyfo: kinetic energy dissipation from lateral friction
Table N1. This table summarizes diagnostics that support the study of lateral subgrid-scale (SGS) parameterizations. The column indicating the experiment for saving the diagnostics generally says “all”, in which case we recommend the diagnostic be saved for CMIP6 experiments in which there is an ocean model component, including the DECK, historical simulations, FAFMIP, DAMIP, DCPP, ScenarioMIP, and C4MIP, as well as the ocean/sea-ice OMIP simulations. We ask only for annual means from these fields, rather than the monthly means requested for most other diagnostics. Additionally, this table has been reduced from the 10 fields requested in CMIP5 to the 6 requested here. Furthermore, note that the fields takekbo and dispkexyfo were requested as three-dimensional fields for CMIP5, whereas they are now requested as depth-integrated two-dimensional fields. The lower sub-table lists the CMOR names and the corresponding CF standard names.

### Lateral sgs parameterizations

<table>
<thead>
<tr>
<th>Item</th>
<th>CMOR name</th>
<th>Sponsor</th>
<th>CMIP5/CMIP6</th>
<th>units</th>
<th>time</th>
<th>shape</th>
<th>grid</th>
<th>priority</th>
<th>expt</th>
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</thead>
<tbody>
<tr>
<td>1</td>
<td>diftrblo</td>
<td>OMIP/FAFMIP</td>
<td>(month → annual) and (hist → all)</td>
<td>m²/s⁻¹</td>
<td>annual</td>
<td>XYZ</td>
<td>native, z/p</td>
<td>3</td>
<td>all</td>
</tr>
<tr>
<td>1</td>
<td>diftrelo</td>
<td>OMIP/FAFMIP</td>
<td>(month → annual) and (hist → all)</td>
<td>m²/s⁻¹</td>
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<td>XYZ</td>
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<td>3</td>
<td>all</td>
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<tr>
<td>2</td>
<td>takekbo</td>
<td>OMIP/FAFMIP</td>
<td>(month → annual) and (hist → all)</td>
<td>Wm⁻²</td>
<td>annual</td>
<td>XY</td>
<td>native</td>
<td>3</td>
<td>all</td>
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<tr>
<td>4</td>
<td>difmxylo</td>
<td>OMIP/FAFMIP</td>
<td>(month → annual) and (hist → all)</td>
<td>m³/s⁻¹</td>
<td>annual</td>
<td>XYZ</td>
<td>native, z/p</td>
<td>3</td>
<td>all</td>
</tr>
<tr>
<td>5</td>
<td>difmxybo</td>
<td>OMIP/FAFMIP</td>
<td>(month → annual) and (hist → all)</td>
<td>m³/s⁻¹</td>
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<td>XYZ</td>
<td>native, z/p</td>
<td>3</td>
<td>all</td>
</tr>
<tr>
<td>6</td>
<td>dispkexyfo</td>
<td>OMIP/FAFMIP</td>
<td>(month → annual) and (hist → all)</td>
<td>Wm⁻²</td>
<td>annual</td>
<td>XY</td>
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### CMOR name related to CF standard name

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<th>CMOR name</th>
<th>CF standard name</th>
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<td>diftrblo</td>
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</tbody>
</table>

### N4.1 Summary of the diagnostic

As for the vertical/diagonal viscosity, we recommend archiving the maps of energy dissipation from lateral viscous friction integrated over a full ocean column. The diagnostic dispkexyfo accounts for dissipation from the sum of Laplacian plus biharmonic friction active in the model.

### N4.2 Theoretical considerations

The local energy dissipated in a hydrostatic model by a lateral Laplacian friction with isotropic viscosity $A$ and anisotropic viscosity $D$ is given by the non-positive quantity (see Sect. 17.8.2 of Griffies, 2004)

$$ D = -\rho \, dV \left[ A \left( e_T^2 + e_S^2 \right) + 2D \Delta^2 \right], \quad \text{(N2)} $$

where

$$ e_T = (dy) \left( u/dx \right)_x - (dx) \left( v/dy \right)_y \quad \text{(N3a)} $$

$$ e_S = (dx) \left( u/dx \right)_y + (dy) \left( v/dy \right)_x \quad \text{(N3b)} $$

are the deformation rates,

$$ 2 \Delta = e_S \cos \theta - e_T \sin \theta \quad \text{(N4)} $$

is a measure of the anisotropy of the viscous operator with $\theta$ an angle that sets the alignment of the generally anisotropic viscosity (Large et al., 2001; Smith and McWilliams, 2003), and $dx$ and $dy$ are the horizontal grid elements. We recommend archiving depth-integrated dissipation per horizontal area

$$ \text{dispkexyfo}^{\text{Laplacian}} = \frac{\eta}{H} \int_{-H}^{H} (\rho \, dz) \left[ A \left( e_T^2 + e_S^2 \right) + 2D \Delta^2 \right]. \quad \text{(N5)} $$

The local energy dissipated in a hydrostatic model by a lateral biharmonic friction is given by the non-positive quantity (see Sect. 17.9.2 of Griffies, 2004)

$$ D = -\rho \, dV \, \mathbf{F} \cdot \mathbf{F}, \quad \text{(N6)} $$

where $\rho \, dV \, \mathbf{F}$ is the lateral Laplacian friction vector used to build up the biharmonic operator. As for the dissipation from vertical viscosity, we recommend mapping the dissipation per horizontal area for each column of seawater, as given by

$$ \text{dispkexyfo}^{\text{biharmonic}} = -\frac{\eta}{H} \int_{-H}^{H} (\rho \, dz) \, \mathbf{F} \cdot \mathbf{F}. \quad \text{(N7)} $$

Many models make use of both Laplacian and biharmonic friction. To account for the net dissipation of kinetic energy, the diagnostic dispkexyfo is comprised of the sum

$$ \text{dispkexyfo} = \text{dispkexyfo}^{\text{Laplacian}} + \text{dispkexyfo}^{\text{biharmonic}}. \quad \text{(N8)} $$
Acknowledgements. This document benefitted from the direct and indirect input of numerous ocean and climate scientists who contributed to the various CORE-II analysis papers (see Sect. 2.1). We also thank many scientists at various modelling centres who provided candid and essential feedback needed to help optimize the scientific utility of OMIP. Thanks also go to Bill Hurlin and Jasmin John at GFDL for commenting on early drafts of this paper. We also thank Frank Bryan, Tim Graham, Astrid Kerkweg, Cath Senior (for the CMIP6 panel), and Wilbert Weijer for their very useful online reviewer comments on the GMD-Discussion manuscript.

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