Evaluating the effectiveness of storage control in reducing peak demand on low voltage feeders

Conference or Workshop Item

Published Version

Creative Commons: Attribution 3.0 (CC-BY)

Open Access


It is advisable to refer to the publisher’s version if you intend to cite from the work. See Guidance on citing.

Published version at: http://doi.org/10.1049/oap-cired.2017.0626

All outputs in CentAUR are protected by Intellectual Property Rights law, including copyright law. Copyright and IPR is retained by the creators or other copyright holders. Terms and conditions for use of this material are defined in the End User Agreement.

www.reading.ac.uk/centaur
CentAUR
Central Archive at the University of Reading
Reading’s research outputs online
1 Introduction

In the transition towards the low carbon economy, increased electricity demand is expected through the uptake of low-carbon technologies (LCTs). Operation of heat pumps and uncontrolled charging of electric vehicles will impose additional stress on the distribution networks [1]. In the UK, the additional demand from LCTs typically coincides with the usual evening peak demand and, therefore, potentially violates the thermal operational constraints on the networks. Traditionally when the thermal capacity of the network has reached the limit, distribution networks are reinforced by replacing the existing assets (e.g. transformers and feeder cables) with higher rating or installing additional assets to split the load. However, as well as being expensive, such reinforcements are inefficient since the thermal constraints are occurring over relatively short periods of time and the remaining time these assets remain under utilised.

With the decreasing costs of electro-chemical energy storage, deployment of battery energy storage systems (BESS) becomes an effective alternative solution for the deferral of traditional reinforcement of the distribution networks [2–5]. The control strategy applied to BESS, and its size, depends on the location and the purpose of its operation, i.e. peak demand reduction, peak generation reduction and voltage support [6]. One of the most popular and versatile control methods is model predictive control (MPC) which uses a forecast as prior knowledge to plan an optimal BESS charging and discharging schedule whilst adjusting the schedule based on observed demand [7–9].

Due to individuality of customer behaviour and the number of customers on low-voltage (LV) feeders, predicting the demand is much more difficult than on higher voltage levels of the distribution network.

This paper presents an analysis of a scheduling MPC algorithm with a fixed error correction method versus a fixed schedule, applied to a simulated BESS, to reduce peak demand on LV feeders based on five forecasting methods. The forecasts, the MPC algorithm and the fixed schedule are assessed on two weeks of half-hourly demand data from 100 LV feeders monitored as part of the New Thames Valley Vision [10] – Low Carbon Network Fund (LCNF) project, funded by office of gas and electricity markets (OFGEM) and led by Scottish and Southern Electricity Networks. The feature of this paper is application of the fixed schedule and MPC algorithm for a BESS on demand data from 100 real LV feeders using four advanced forecasting techniques.

2 Method

The performance of the control algorithm applied to the BESS is an important factor. Forecast error and poor algorithm performance could result in scheduling BESS to charge at the same time as the actual peak. Higher peak would then lead to further violation of the operational constraints and potentially, equipment failure.

To investigate the relationship between the achieved peak demand reduction and the forecast method, two control algorithms are considered: fixed optimal schedule and MPC with fixed error demand model update. The algorithms are applied to a simulated BESS on a LV distribution feeder in a suburban network. The BESS is sized to deal with 20% reduction of the forecasted demand model update. The algorithms are applied to a simulated BESS on a LV feeder in a suburban network. The BESS is sized to deal with 20% reduction of the forecasted demand aggregated across the three phases.

2.1 Schedule optimisation

The aim of the schedule optimisation is to find a BESS schedule, $p$, for the forecasted demand, $d_i$, over a period of $N$ half-hours (in this case 48), such that the cost function in (1) is minimised:

$$F(p, d_i) = \xi_p(p, d_i) + \alpha \xi_d(p) + \beta \xi_c(c) + \gamma \xi_w(c), \quad (1)$$
Subject to constraints:

\[
C_{\min} \leq c(t) \leq C_{\max}, \quad (2)
\]
\[
P_{\min} \leq p(t) \leq P_{\max}, \quad (3)
\]
\[
c(t + 1) = c(t) + p(t)\mu\tau, \quad (4)
\]
\[
\mu = \begin{cases} 
\frac{1}{\tau} & \text{if } p(t) \geq 0 \\
\frac{\mu}{\tau} & \text{if } p(t) < 0 
\end{cases} \quad (5)
\]
\[
\alpha, \beta, \gamma \in [0, 1] \quad (6)
\]

where \( \xi_p(p, d_i) \) is the peak-to-average cost component for peak reduction, self-normalised to the initial conditions, defined as

\[
\xi_p(p, d_i) = \left( \frac{\sum_{t=1}^{N} (d(t)+p(t))/N}{\xi_f(p, d_i)} \right)^2 \quad (7)
\]

Cost component, \( \xi_{cd} \), represents the cost of charge dynamics, aimed at smoothing the charging of BESS and defined as

\[
\xi_{cd} = \frac{\max\left(\frac{t}{\max(\delta t, \mu \tau)}\right)}{P_{\max}} \quad (8)
\]

The storage cycling cost component, \( \xi_{sc} \), aims to allow at most only one full charge and discharge cycle per day and defined as

\[
\xi_{sc} = \frac{\sum_{i=1}^{N} \left| \frac{[0, \max(\delta t, \mu \tau)]\{t\}}{\delta t} \right| + \sum_{i=1}^{N} \left| \frac{[-\max(\delta t, \mu \tau)]\{t\}}{\delta t} \right|}{2} \quad (9)
\]

At the end of the schedule, the BESS should reach 50\% state-of-charge (SoC), which is achieved with the target SoC cost component, \( \xi_{ts} \), defined as

\[
\xi_{ts}(c) = \frac{(c(N) - 0.5C_{\max})^2}{\xi_{ts}(c)} \quad (10)
\]

Scaling factor, \( w \), ensures that sum of cost components \( \xi_{cd}, \xi_{sc} \) and \( \xi_{ts} \) is at the same scale as \( \xi_p \)

\[
w = \alpha + \beta + \gamma \quad (11)
\]

Constraints in (2) and (3), represent limits on the energy storage capacity, \( c(t) \), and BESS power rating constraints, respectively. A model for the energy storage is given in (4) where \( \tau \) is the duration of the time period in hours and \( \mu \) is the BESS efficiency defined in (5).

2.1.1 Model predictive control for BESS: MPC, also known as receding horizon control, computes an optimal schedule for the duration of the horizon by updating the demand model with recent observations and deploying only the first control value from the current horizon. Once the control for the first time step is deployed and observation for the current time step is received, the controller moves to the next horizon to compute a new optimal schedule on the updated demand model.

In this case study, MPC does not have access to the demand model used in generating the forecasts and so is not able to produce rolling forecasts. Instead, the demand is modelled by updating the forecast with the projection of the forecast error from the previous time step, as depicted in Fig. 1 and it is assumed that all forecast errors are strongly positively correlated. This clearly will not be the case in general.

The length of the horizon is chosen to be 10 half-hourly time steps [9]. The controller is optimising the same cost function as for the fixed schedule in (1), reduced to the length of the control horizon.

The input demand profile, \( d_i \), is replaced for the duration of the horizon \( H_k \) with the forecast, \( d_i^{*} \), shifted by error, \( c(k + 1) \). The error is based on the observed demand at the previous time step (excluding the energy exchanged with BESS) and the original forecast at the previous times step (Fig. 2).

2.1.2 Peak reduction metrics: The case study consists of three scenarios:

- 'best possible' – fixed schedule based on the assuming 100% accurate forecast,
- ‘fixed’ – fixed schedule based on forecast,
- ‘MPC’ – receding horizon control with fixed error.

For each scenario, the peak reduction metric is given as

\[
PR(d^*) = \left( 1 - \frac{\max(d^*)}{\max(d_m)} \right) \times 100%,
\]

where \( d^* \) denotes the resultant demand on the feeder by applying the corresponding schedule and \( d_m \) is the observed demand profile. This metric considers only the overall peak reduction on demand over the entire day, not just the reduction of the observed peak.

2.1.3 Demand data: The demand data used in this case study is based on the monitoring of the LV substations in Bracknell, Berkshire, UK as part of the New Thames Valley Vision project [10]. The data set is based on energy consumption recorded on 100 LV feeders between 31 March 2014 and 14 November 2015. The first 83 weeks were used for training the forecast methods and the last two weeks were used for testing.

2.1.4 Forecasting methods: We consider five basic load forecast to apply in our control method, summarised below:

- 7Sav is our benchmark method and forecasts each time period, e.g. 10:00 a.m. on Thursday is simply the average of the previous 5:10 a.m.’s on Thursday,
- ST is a simple seasonal model for each hour. It is the same as that as presented in [11] but there is now a dummy variable for each day type (Monday, Tuesday etc.),
- SnT is as ST but no annual linear trend is modelled.
(iv) **GAM**, which stands for generalised additive model, is a simple generalised model based on that in [12, 13] which estimates the electricity load using a piecewise smooth function determined from the predictor variable(s). Here we consider only one predictor variable to forecast the electricity load, that is, the electricity load from the half hour two days prior. Note that we do not include weather variables.

(v) **ARWD** is a simple autoregressive method, which is typically used for electricity price forecasting [14]. It is based on a two-step approach. In the first one, the weekly load profile \( \mu_t \) is estimated for every hour of the week. A residual time series \( r_t \) is then created by subtracting the time series from the historical load \( \mu_t = L_t - \mu_r \), where \( L_t \) is the load at time \( t \). In the second step an AR \((p)\) process (autoregressive process of order \( p \)) which satisfies

\[
\begin{align*}
\alpha &= \phi_0 + \sum_{j=1}^{p-1} \phi_j r_{t-j} + \epsilon_t, \text{ with parameters } \phi_0 \text{ and error term } \epsilon_t \text{ is estimated by solving the Yule–Walker equations. The } p \text{ is chosen so that the Akaike information criterion is minimised with a maximal possible value of } \rho_{\text{max}} = 48 \times 15.
\end{align*}
\]

### 3 Results

#### 3.1 Forecast

On average over all 100 feeders the best performing methods were the **ARWD** method and the simple average **7SAV** with mean absolute percentage error (MAPEs) of 17.72 and 18.60, respectively, the seasonal methods **Snt** and **ST** also performed well with average MAPEs of 18.76 for the **ST** method and 19.05 for the **Snt** method. The worst performing method was the **GAM** with a MAPE of 27.54. We note that the **ST** and **Snt** methods have very similar performances. It was also found that certain methods performed better than others for different feeders. For instance, the best scoring method for 48 of the feeders was the **ARWD** method, followed by **Snt** and **ST** with 14 and 31, respectively. Finally, the **7SAV** method was best for the remaining seven feeders. This indicates that different forecasts methods should perhaps be used for different feeders. Identification of why this is the case will be future work.

The relationship between mean daily demand (for the last year) and each feeder for two of the forecast methods achieved some peak reduction. The least increase on the peaks was achieved by **ARWD**. Yet, on average **Snt** provided best peak reduction for both fixed and **MPC**, closely followed by **ARWD**.

Comparison of the daily peak reduction for each forecasting method and each scenario: **PR(\(d^m\))**, **PR(\(d^r\))** and **PR(\(d^m\))**

Fig. 4 shows the boxplot for peak reduction for each control method, each forecast method and the best possible peak reduction, **PR(\(d^r\))**. Overall, on average all forecast methods and control techniques

Fig. 3 Relationship between MAPE and mean daily energy demand for each feeder for two of the forecast methods

Fig. 4 Comparison of the daily peak reduction for each forecasting method and each scenario: **PR(\(d^m\))**, **PR(\(d^r\))** and **PR(\(d^m\))**

4 Discussion

Comparison of MAPE for a range of feeder sizes shows that some forecast perform better for certain types of feeders. Hence, there

Fig. 5 Observed, forecasted demand and profiles resulting from best possible, fixed and **MPC** schedules based on **Snt** forecasting method
was no one forecast that suited all feeders. We tested a number of forecast methods against a competitive benchmark. An advantage of all methods is their simplicity and computational speed in being implemented.

Forecast accuracy is a strong driver for potential peak reduction but accuracy was driven strongly by mean daily demand on the feeder. Hence, the effectiveness of storage is linked to the number of customers on a feeder and the size of these customers. As the result, better peak reduction was achieved with fixed schedule and MPC with simple error correction for the feeders with greater mean daily demand. For small feeders, BESS with fixed schedule actually increases the peak demands. Hence, there should be a minimum size threshold when deciding if a feeder is suitable for BESS with scheduling algorithms. However, MPC with the fixed error demand update method, performed better than fixed schedule, particularly on smaller feeders. Further investigation is required on the correlation of forecast errors and demand characteristics on smaller feeders. More sophisticated error modelling techniques (e.g. rolling forecast) are expected to improve the performance of MPC, especially on larger feeders.

In case of operational implementation of BESS on a LV distribution feeder, the control system is typically based on multiple stages: planning and real-time operation. The real-time operation control is happening at a much higher resolution than the half-hourly planning stage. The half-hourly demand represents an average power within the half-hour meaning that the actual peaks measured at the higher-resolution (e.g. 5 s or one minute) would be significantly greater that the half-hourly average.

Furthermore, this paper only considered aggregated demand across three phases at half-hourly resolution. Due to the number of customers on each phase and their individual behaviour, the demand is likely to be unbalanced. Although balancing the demand on the phases would not decrease the aggregated half-hourly demand, peaks on each phase measured at higher resolution are likely to be significantly reduced, assisting with managing the thermal constraints on the feeder.

5 Summary

The paper has presented a comparison of five forecasting techniques for prediction of LV feeders and their role in the reduction of peak demand using two energy storage control techniques: fixed schedule and model predictive control. The forecasting techniques and control algorithms have been assessed on demand data for 14 days from 100 LV feeders.

Results show that certain type of forecasts perform better for certain sizes of feeders and consequently lead to better performance of the peak reduction algorithms. Both fixed schedule and MPC with simple error achieved better peak reduction for larger feeders. However, MPC with simple error correction have performed better on smaller feeders compared to the fixed schedule.

In future work, integration of advanced demand models and rolling forecast for the model predictive control will be considered.

6 Acknowledgments

This research work was carried out as part of New Thames Valley Vision (SSET203), a LCNF project, funded by OFGEM and led by Scottish and Southern Electricity Networks.

7 References

8 Mégel, O., Mathieu, J. L., Andersson, G.: ‘Scheduling distributed energy storage units to provide multiple services under forecast error’, Int. J. Electr. Power Energy Syst., 2015, 72, pp. 48–57