

Use of data assimilation methods in coastal sediment models

Conference or Workshop Item

Presentation

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Use of data assimilation methods in coastal sediment models

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Outline

- Motivation: morphodynamics and flooding
- Observational data and morphodynamic model
- Data assimilation
- Parameter estimation
- Conclusions

Case study: Morecambe Bay

- Channels in Morecambe Bay can move by several kilometres in just a few years
- Channel movement
 - impacts on habitats in the bay
 - affects access to ports
 - has implications for flooding during storm events
- For example, Morecambe can be flooded by storm waves propagating up the deepwater channels



The general idea

- Coastal bathymetry is dynamic and evolves with time
 - water action erodes, transports, and deposits sediment, which changes the bathymetry, which alters the water action, and so on
- Accurate knowledge of coastal bathymetry at the time of a storm event would allow improved flood forecasting using coastal flood inundation models
 - but it is impractical to continually monitor large coastal areas in anticipation of a storm
- A solution may be to run an operational coastal area morphodynamic model
 - and keep the model on track using data assimilation
- As observations become available they can be used to nudge model bathymetry back towards true bathymetry
 - these observations may be infrequent and only sample a small part of the model domain
- Data assimilation can also be used for parameter estimation

Sequential data assimilation



Waterline data for Morecambe Bay





An image of the land-sea boundary (satellite SAR image © ESA) Water elevation predicted along the boundary by a hydrodynamic model with surge component



LiDAR data from 15/11/05 to be used for validation.

Morphodynamic model



Spatial resolution ~ 240m

A simple model, relative to state-of-the-art engineering models, but adequate for assessing the benefits of data assimilation

3D Var data assimilation

Field value



$$J(\mathbf{w}_k) = (\mathbf{w}_k - \mathbf{w}_k^b)^{\mathbf{T}} \mathbf{B}_k^{-1} (\mathbf{w}_k - \mathbf{w}_k^b) \quad \begin{array}{c} \text{observation} \\ \swarrow & \mathbf{term} \\ \end{array} \\ \begin{array}{c} \bullet & \bullet \\ \bullet & \bullet$$

B and **R** are the covariance matrices of the background and observation errors

3D Var data assimilation

Field value



$$J(\mathbf{w}_k) = (\mathbf{w}_k - \mathbf{w}_k^b) \stackrel{\mathbf{\Gamma} \mathbf{B}_k^{-1}}{\longrightarrow} \mathbf{w}_k - \mathbf{w}_k^b) \stackrel{\text{observation}}{\swarrow} term$$

background term $+ (\mathbf{y}_k - \tilde{\mathbf{h}}_k(\mathbf{w}_k))^T \mathbf{R}_k^{-1} (\mathbf{y}_k - \tilde{\mathbf{h}}_k(\mathbf{w}_k))$

B and **R** are the covariance matrices of the background and observation errors Choice of matrix is crucial to success of assimilation scheme

Choosing the lengthscale for B

Increment (Analysis-Background) for assimilation of 1 waterline





L = 0.5

L = 3.0

Comparison with lidar validation data



No assimilation

With assimilation Calibrated params

With assimilation Weighted ensemble mean Parameter ensemble

Parameter estimation

- Numerical models suffer from errors in their initial conditions and parameters.
- Initial conditions are often estimated by data assimilation; combining model predictions with observational data to produce an updated model state (the analysis) whilst keeping the model parameters fixed.
- Even with perfect initial data, inaccurate model parameters will lead to the growth of prediction errors.
- Using *state augmentation* in data assimilation we can estimate model parameters concurrently with the state.

Joint state-parameter estimation

Model state & parameter evolution

$$\mathbf{z}_{k+1} = \mathbf{f}(\mathbf{z}_k, \mathbf{p})$$
 $\mathbf{p}_{k+1} = \mathbf{p}_k$

Augmented system model

$$\mathbf{w}_{k+1} = \begin{pmatrix} \mathbf{z}_{k+1} \\ \mathbf{p}_{k+1} \end{pmatrix} = \begin{pmatrix} \mathbf{f}(\mathbf{z}_k, \mathbf{p}_k) \\ \mathbf{p}_k \end{pmatrix} = \tilde{\mathbf{f}}(\mathbf{w}_k)$$

Observations

$$\mathbf{y}_k = ilde{\mathbf{h}}(\mathbf{w}_k) + oldsymbol{\delta}_k = ilde{\mathbf{h}} \left(egin{array}{c} \mathbf{z} \ \mathbf{p} \end{array}
ight) + oldsymbol{\delta}_k = \mathbf{h}(\mathbf{z}_k) + oldsymbol{\delta}_k$$

Background error covariance

$$J(\mathbf{w}_{k}) = (\mathbf{w}_{k} - \mathbf{w}_{k}^{b}) \stackrel{\mathbf{\Gamma} \mathbf{B}_{k}^{-1}}{\longrightarrow} \mathbf{w}_{k} - \mathbf{w}_{k}^{b}) \stackrel{\text{observation}}{\swarrow} term$$

background term $+ (\mathbf{y}_{k} - \tilde{\mathbf{h}}_{k}(\mathbf{w}_{k}))^{T} \mathbf{R}_{k}^{-1} (\mathbf{y}_{k} - \tilde{\mathbf{h}}_{k}(\mathbf{w}_{k}))$



For joint state-parameter estimation, it is important that the a priori cross-covariances between the parameters and the state are well specified.

A hybrid approach

Combines ideas from 3D-Var and the extended Kalman filter (EKF)

- assumes \mathbf{B}_{zz} and \mathbf{B}_{pp} fixed
- uses a flow dependent state-parameter cross covariance $\mathbf{B}_{\mathbf{z}\mathbf{p}_{k}}$

$$\mathbf{B}_{k+1} = \begin{pmatrix} \mathbf{B}_{\mathbf{z}\mathbf{z}} & \mathbf{N}_{k}\mathbf{B}_{\mathbf{p}\mathbf{p}} \\ \mathbf{B}_{\mathbf{p}\mathbf{p}}\mathbf{N}_{k}^{T} & \mathbf{B}_{\mathbf{p}\mathbf{p}} \end{pmatrix}$$
where $\mathbf{N}_{k} = \frac{\partial \mathbf{f}(\mathbf{z},\mathbf{p})}{\partial \mathbf{p}}\Big|_{\mathbf{z}^{a},\mathbf{p}^{a}}$

 $|\mathbf{z}_k^a, \mathbf{p}_k^a|$

A simple sediment transport model

Based on the sediment conservation equation

$$\frac{\partial z}{\partial t} = -\left(\frac{1}{1-\varepsilon}\right)\frac{\partial q}{\partial x} \quad \text{with} \quad q = Au^n$$

where z(x,t) is the bathymetry, t is time, ε is the sediment porosity, q is the sediment transport rate, u(x,t) is the depth averaged current and A and n are constant parameters.

Can we use data assimilation to estimate the parameters A and n?

Experiments

Identical twin:

- reference solution generated using 'true' parameter values A = 0.002 ms⁻¹ and n = 3.4
- model then re-run with incorrect initial bathymetry and parameter values
- Observations assimilated sequentially at regular time intervals
 - taken from reference solution & assumed perfect
 - the 3D-Var cost function is minimized iteratively using a quasi-Newton descent algorithm
- Background error covariances
 - **B**_{zz} fixed
 - $\mathbf{B}_{\mathbf{z}\mathbf{p}_k}$ time varying

without data assimilation ...







with data assimilation

Parameter estimates

Initial estimates (a) $A_0 = 0.02 \text{ ms}^{-1}(b) n_0 = 2.4$



 $(A_{true} = 0.002 \text{ ms}^{-1}, n_{true} = 3.4)$

Summary

- Up-to-date knowledge of near-shore coastal bathymetry is important in flood prediction and risk management
- Assimilated SAR waterline data into a model of Morecambe Bay to keep the model on track
- Best results are obtained using an ensemble of parameters
- Developed a new hybrid data assimilation scheme for joint estimation of model parameters and state.
- Recovers the true parameter values to a good level of accuracy, even when observations are noisy.
- Relatively simple to implement and computationally inexpensive to run
- Method also successfully applied to a range of simple dynamical system models.
- Expect this new technique to be easily transferable to more complex models.