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1 Urban surface temperature observations from ground-based thermography: intra- and 2 inter-facet variability

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7 Abstract

8 Ground based thermal cameras are used to observe urban surface temperatures (T_s) with an
9 unprecedented combination of: temporal and spatial resolution (5 min and ~ 0.5 m \rightarrow 2.5 m), spatial
10 extent (3.9 ha), instrument number (6 static cameras) and surface heterogeneity (mixed high rise and
11 vegetation). Unsupervised classification of images by geometry and material properties (surface
12 orientation, albedo, solar irradiance, and shadow history) is facilitated by a detailed three-dimensional
13 surface model (430 m x 430 m extent) and sensor view modelling. From detailed source area analysis,
14 9.5 % of the area is observed by the cameras. Across all camera pixels, the 5th - 95th percentile T_s
15 differences reach 37.5 K around midday. Roofs have the greatest diurnal T_s range (290.6 K \rightarrow 329.0
16 K). T_s differences across sunlit sloped roofs reach 23.3 K. Walls of different cardinal orientations
17 consistently differ by > 10 K between 10:00 and 15:00. Shadow tracking within images is used to
18 model cooling rates, where recently shaded (< 30 min) ground can be 18.6 K warmer than equivalent
19 unshaded T_s . West walls remain warm past sunset and are 1.2 K warmer than north walls at 23:00 (~ 4
20 hours after sunset). Recently shaded walls cool exponentially to ambient T_s at a similar rate as the
21 ground, but four times slower than roofs. The observed T_s characteristics are anticipated to have a
22 wide range of applications (e.g. evaluation of urban surface energy balance models, ground-truthing
23 of satellite thermal remote sensing).

24 1. Introduction

25 Urban surface temperature (T_s) is an important control in the surface energy balance (Krayenhoff and
26 Voogt, 2007) that has distinct characteristics across cities (Offerle *et al.*, 2006). There is increasing
27 interest in T_s observations with high temporal and spatial resolution at facet (e.g. roof, wall, ground)
28 and sub-facet (e.g. materials, shadowing) scales as the degree of urban modelling complexity required
29 for atmospheric models is unclear (Chen *et al.*, 2011). Numerical weather prediction (NWP)
30 frequently characterises the urban surface energy balance by facet (e.g. TEB, Masson, 2000;
31 MORUSES, Porson *et al.*, 2010; SLUCM, Kusaka and Kimura, 2004; BEP, Krayenhoff *et al.*, 2020).
32 Increasingly complex and realistic sub-facet details within urban areas are resolved by models for:
33 computational fluid dynamics (CFD) (Toparlar *et al.*, 2017), sub-facet surface energy balance (e.g.
34 TUF3D, Krayenhoff and Voogt, 2007; THERMORender, Xu and Asawa, 2020), thermal radiation
35 stress (e.g. SOLWEIG, Lindberg and Grimmond, 2011; RayMan, Fröhlich *et al.*, 2019) and building

36 energy (e.g. EnergyPlus, Crawley *et al.*, 2001). Such models may have T_s as a prognostic variable
37 which requires observational evaluation across the facets resolved by the model processes.

38 High temporal and facet-scale resolution urban T_s observation for model evaluation faces many
39 challenges resulting in a general lack of such studies (Toparlar *et al.*, 2017). Exploiting space-borne
40 data for evaluation (e.g. Alexander *et al.*, 2015 using MODIS; Toparlar *et al.*, 2015 using Landsat) is
41 constrained by: low revisit times, a view bias of horizontal surfaces (Hu and Wendel, 2019), and low
42 spatial resolutions such that one pixel may cover the entire model domain (e.g. MODIS, Meteosat
43 Second Generation). Thermal cameras on airborne platforms (e.g. helicopters Hénon *et al.*, 2012;
44 Antoniou *et al.*, 2019; drones Gaitani *et al.*, 2017; Naughton and McDonald, 2019) can view the
45 convoluted urban surface at facet-scale but also have low revisit times and directional view bias
46 (Lagouarde *et al.*, 2004). These studies typically assume no atmospheric effects (Meier *et al.*, 2011;
47 Morrison *et al.*, 2020) on observations. From ground-based platforms, thermal cameras have potential
48 to supersede point-based *in-situ* sensors (e.g. thermocouples used by e.g. Kanda *et al.*, 2005; Rotach *et al.*,
49 *et al.*, 2005; Pearlmutter *et al.*, 2006) due to higher temporal and spatial resolutions to observe both
50 inter- and intra- facet variations (e.g. Alchapar *et al.*, 2014). A few studies (e.g. low-rise suburb,
51 Adderley *et al.*, 2015; scale model, Morrison *et al.*, 2018) achieve adequate spatial coverage but are
52 limited to simple surface heterogeneity. Ground- or airborne sub-facet thermal imagery across more
53 realistic cities is rare, given the challenges with: logistics to obtain adequate camera views of the
54 convoluted three-dimensional surface and classifying the observations to know what is actually
55 sampled and therefore can/should be compared to model outputs. Sub-facet resolution sampling is
56 done on foot at street level (e.g. Lee *et al.*, 2018) or with vehicle traverses to sample more walls and
57 ground (e.g. Voogt and Oke, 1997; Hilland and Voogt, 2020). Other thermography observations have
58 increased spatial coverage using Asano and Hoyano's (1998) spherical sampling technique (e.g.
59 Acuña Paz y Miño *et al.*, 2020), rotating masts (Adderley *et al.*, 2015), or multiple cameras (e.g.
60 Morrison *et al.*, 2020). Classification methods have used time consuming and subjective techniques
61 such as manual digitisation (Hartz *et al.*, 2006; Lee *et al.*, 2018; Antoniou *et al.*, 2019) or supervised
62 clustering (Voogt and Oke, 1997; Hénon *et al.*, 2012). To expand classification possibilities, Hilland
63 and Voogt (2020) use concurrent visible imagery.

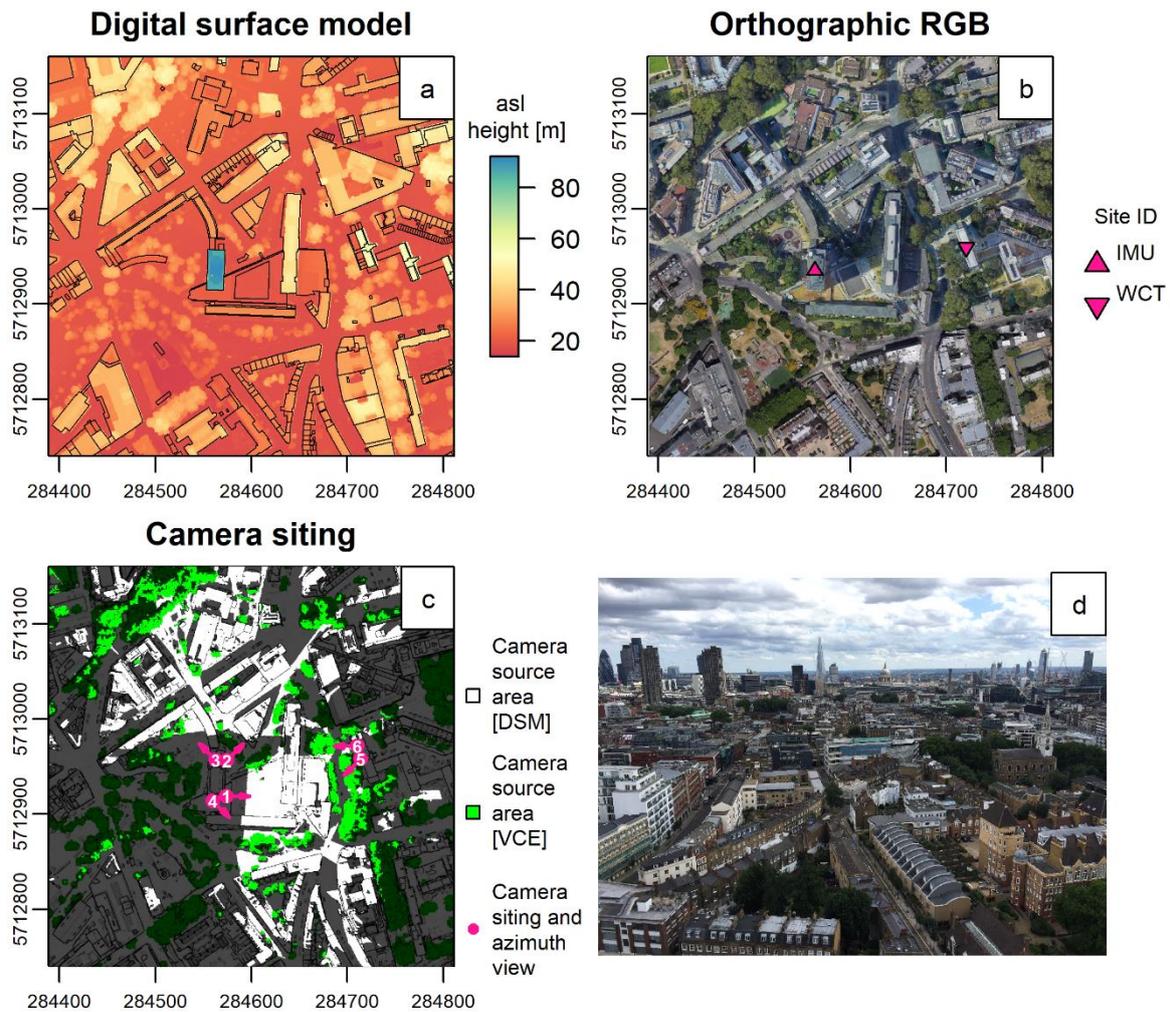
64 The objectives of this paper are to: (i) outline an unsupervised and objective method to analyse
65 surface-based thermal remote sensing images and (ii) investigate the drivers of urban T_s variability at
66 a high level of detail. The Morrison *et al.* (2020) London network of six ground-based infrared
67 cameras is used to obtain unprecedented T_s detail (5 min temporal and ~ 1 m spatial resolution) for a
68 local-scale area, giving unique insight into urban T_s variability. A digital surface model (DSM) is used
69 with perspective projection and radiative transfer modelling to objectively classify observations by
70 transient sun-surface geometry effects that would not be possible by manual or supervised means.

71 **2. Methods**

72 To investigate the drivers of urban T_s variability, ground-based thermal camera observations are
73 processed to determine the surfaces “seen” across a range of scales, from building scale features
74 (facet, orientation and bulk material) through to sun-surface geometry and shadow history at the sub-
75 facet scale.

76 **2.1. Study area and observations**

77 Observation sites in the Borough of Islington, London, UK (51°31'35" N, 0°06'19" W) on two high
78 rise residential tower blocks are identified (ID) as “IMU” and “WCT” (IMU at 74 m agl (above
79 ground level); WCT 36 m agl) (Fig 1a). The study area covers a real world (RW) area with irregular
80 street pattern with streets often lined with deciduous trees. There is a mix of residential and
81 commercial buildings (often four to six storeys tall) arranged in terrace rows or large single units (Fig
82 1d).



83
 84 Fig 1. Plan view of study area with: (a) height of all surfaces above sea level (asl) with building footprints (black lines, from
 85 Evans *et al.*, 2011), (b) orthorectified RGB image from a mosaic of Google Earth (Google, 2019) images with
 86 locations (symbols) of the study sites, (c) a render of the “model world” (MW) digital surface model (DSM) and
 87 vegetation canopy element (VCE) geometry with DSM (white) and VCE (green) seen by the cameras located (pink
 88 dots) around the observation sites with different view directions (pink arrows) and unique camera identification
 89 (white) numbers (Table 1 gives details), (d) Digital camera image looking southeast and next to camera number 4
 90 (C4) on 25th Oct 2017. (a – c) use Coordinate Reference System WGS84 UTM grid zone 31N. (a-c) are modified
 91 from Morrison *et al.* (2020).

92 Optris PI-160 (Optris GmbH, 2018) longwave infrared (LWIR) cameras (Table 1) measure upwelling
 93 longwave radiation from the study area (Fig 1c) for 27th – 28th August 2017 (mainly clear-sky summer
 94 days). The cameras have multiple view angles (Table 2) allowing various facets of the complete
 95 canopy surface to be sampled. Morrison *et al.* (2020) provide details on the study area and the
 96 observations, including: camera siting, measurement procedure, meteorological conditions, and the
 97 atmospheric and emissivity corrections of observations to estimate T_s from the at-sensor brightness
 98 temperatures. Downwelling shortwave (SW) irradiance (E_{sw}^\downarrow , $W m^{-2}$) from a Davis Vantage Pro 2
 99 weather station located 114 m agl, 1.1 km southeast of IMU aids the image classification.

100 Table 1. Measurement and corrections used to determine surface temperature (T_s) from longwave infrared (LWIR) cameras.

| Property | Description |
|-----------------------------|---|
| Platform | Static ground-based |
| Sample rate | 1 min |
| Temporal resolution | 5 min (median of samples at end of interval) |
| Image resolution | 160 x 120 pixels |
| Temperature resolution | 0.1 K |
| Number of cameras | 6 |
| Observation campaign period | 7th July – 10th Nov 2017 (here 27 th – 28 th August) |
| Enclosure | Custom built enclosures (Morrison <i>et al.</i> , 2020) |
| Radiometric calibration | Manufacturer calibrated 2 months prior to study |
| Accuracy | ± 2 K |
| Spectral range | 7 – 14 μm , see Morrison <i>et al.</i> (2020) |
| Image distortion correction | Rectilinear correction; see Morrison <i>et al.</i> (2018) |
| Atmosphere correction | Multi line of sight; see Morrison <i>et al.</i> (2020) |
| Emissivity correction | Corrected for multiple scattering with anisothermal surface emission; see Morrison <i>et al.</i> (2020) |

101 Table 2. Siting properties of the ground based LWIR cameras installed on two high-rise residential towers named “IMU” and
 102 “WCT” within the study area (Fig 1).

| Camera ID | Location Site ID | Field of View ($^\circ$) horizontal x vertical | Cardinal Facing | Viewing Zenith Angle (Θ , $^\circ$) | Median Path Length (m) |
|-----------|------------------|--|-----------------|--|------------------------|
| C1 | IMU | 68.6 x 54.2 | E | 46.5 | 88.8 |
| C2 | IMU | 62.6 x 49.1 | NE | 51.7 | 97.9 |
| C3 | IMU | 62.8 x 49.2 | NWW | 52.9 | 106.6 |
| C4 | IMU | 37.3 x 28.4 | SE | 56.7 | 122.7 |
| C5 | WCT | 38.4 x 29.3 | SW | 66.6 | 79.0 |
| C6 | WCT | 62.4 x 48.9 | W | 61.7 | 67.5 |

103 **2.2. Image classification**

104 To facilitate image classification, the RW study area and instrumentation are represented in a “model
 105 world” (MW). The MW uses a vector-based 3D DSM with a 3D mesh of triangles and a voxelated
 106 representation of vegetation covering the RW study area (Fig 1). The DSM extends 430 m x 430 m
 107 horizontally to cover the camera source areas. The MW also uses sensor view modelling to replicate
 108 the RW camera perspectives (hereafter “MW cameras”), whereby the DSM is projected on to the MW
 109 camera image plane, using a pinhole camera projection (Hartley and Zisserman, 2004).

110 Modelled camera perspectives determine various surface types “seen” by each camera pixel (x, y).
 111 Types of surface are differentiated by class (i) at timestep t for each pixel [$i(x, y, t)$]. Within class i ,
 112 three surface properties are defined (Table 3): orientation and material (Σ), sun-surface geometry
 113 (bidirectional reflectance factor, BRF) and shadow history (time in shade, t_{shd} , min). Thus i principally
 114 describes sun-surface geometry which is a key driver of T_s variability (Krayenhoff and Voogt, 2016;
 115 Morrison *et al.*, 2018).

116 Many features of the MW are created and managed by the Discrete Anisotropic Radiative Transfer
 117 (DART) model (Gastellu-Etchegorry *et al.*, 2012). DART allows 3D radiative transfer (RT) processes
 118 to be simulated in both natural and urban landscapes in the visible to LWIR regions of the

119 electromagnetic spectrum using a ray tracing approach. Here DART is used to simulate the BRF
 120 “seen” by each MW camera pixel, shown by Morrison *et al.* (2018) for simple building geometry to
 121 differentiate sunlit and shaded areas. For a full description of DART see Gastellu-Etchegorry *et al.*
 122 (2015).

123 Orientation and material (Table 3) for each camera pixel [$\Sigma(x, y)$, Fig 2b] is obtained using Blender
 124 rendering software (Blender, 2018), where DSM triangle colours are rendered for each MW camera
 125 image perspective (Morrison *et al.*, 2018 for details). A pixel is $\Sigma_{\text{mixed}}(x, y)$ (dark grey, Fig 2b) if it (a)
 126 has more than one surface and orientation property rendered or (b) views surfaces beyond the MW
 127 extent (e.g. Fig 2b C2, top of image). Pixels manually masked [$\Sigma_{\text{masked}}(x, y)$] from further analysis
 128 include near-field IMU and WCT roofs which are challenging to align, a low emissivity metal roof
 129 (C2, Fig 2b) and the corner of the C1 enclosure (Fig 2b, top left). Compared to prior studies that
 130 manually classify images, our classification is objective and automated but typically has fewer
 131 classes. Christen *et al.*'s (2012) images classified by manual inspection and digitisation (see their Fig
 132 1d) include e.g. brick/painted walls and tile/gravel roofs by manual inspection and digitisation.
 133 Inclusion of such classes here - in Σ and across Fig 2b - would require a similarly classified DSM
 134 which was not available in this study.

135 To determine the sun-surface geometry characteristics (Table 3), all MW surfaces, including
 136 vegetation canopy elements, are defined in DART as opaque Lambertian reflectors. Direct
 137 downwelling spectral irradiance ($E_{\lambda}^{\downarrow, \text{dir}}$, $\text{W m}^{-2} \mu\text{m}^{-1}$) is simulated by DART at $0.5 \mu\text{m}$ wavelength (λ ,
 138 bandwidth $\Delta\lambda = 0.01 \mu\text{m}$). Rays originate from a horizontal layer just above the tallest building (625
 139 rays m^{-2}) and are tracked downward with spectral radiant flux density $E_{\lambda}(\theta, \phi, \Omega, t)$ ($\text{W m}^{-2} \mu\text{m}^{-1}$)
 140 along solid angle Ω (sr) and direction (θ, ϕ) at timestep t . $E_{\lambda}(\theta, \phi, \Omega, t)$ intercepted by the MW surface
 141 is scattered for all possible scattering directions, according to the surface position and orientation.
 142 Scattered rays that intercept the image plane of a MW camera are used by DART to calculate at-
 143 sensor spectral radiance [$L_{\lambda}^{\text{cam}}(x, y, t)$, $\text{W m}^{-2} \text{sr}^{-1} \mu\text{m}^{-1}$].

144 The BRF across the camera images is calculated as:

$$\text{BRF}(x, y, t) = \frac{\pi L_{\lambda}^{\text{cam}}(x, y, t, \Omega)}{E_{\lambda}^{\downarrow, \text{dir}}(t)}. \quad \text{Eqn. 1}$$

145 For a shaded surface BRF is zero. $\text{BRF} = 1$ for sunlit horizontal surfaces (i.e. surfaces plane-parallel
 146 to the ground) regardless of daytime sun angle and camera view angle, as $E_{\lambda}^{\downarrow, \text{dir}}$ is referenced to a
 147 horizontal layer. The BRF of a non-flat surface departs from unity. BRF increases as the sun angle
 148 becomes perpendicular to the surface, and vice versa. For example, in the northern hemisphere, east
 149 facing walls have the highest BRF in the early morning, decreasing through the morning as the sun-
 150 surface angle becomes more oblique.

151 A low density of rays incident on a surface can occur if the direct-beam solar radiation is near-
 152 perpendicular to a surface and/or when the sun angle is low relative to the surface. This can cause
 153 inaccuracies and erroneous patterns in $BRF(x, y)$ and isolated “sunlit” pixels [$BRF(x, y) > 0$] (i.e.
 154 none of the surrounding 8 pixels have $BRF(x, y) > 0$). To resolve this, in this study we reassign these
 155 pixels to $\Sigma_{mixed}(x, y)$. Where $BRF(x, y, t)$ has a continuous scale, the final surface property for analysis
 156 is $\overline{BRF}(x, y, t)$, which is $BRF(x, y, t)$ binned (indicated by overbar) between $0 \rightarrow 2$ using a bin width
 157 of 0.25. The bins are centre labelled. The first bin is 0 and is for values between 0 and 0.125 e.g.
 158 $BRF(x, y, t) = 0.10$ is assigned to $\overline{BRF}(x, y, t) = 0$; the second bin is 0.25 and has values between
 159 0.125 and 0.375 e.g. $BRF(x, y, t) = 0.13$ is assigned $\overline{BRF}(x, y, t) = 0.25$; etc. To differentiate shaded
 160 pixels [$BRF(x, y, t) = 0$] from the lowest \overline{BRF} bin ($\overline{BRF}(x, y, t) = 0$), pixels with $BRF(x, y, t) < 0.05$
 161 on timesteps with no direct solar radiation are assigned to a separate bin, $\overline{BRF}(x, y, t) = -1$ for analysis.
 162 E_{sw}^{\downarrow} observations (Section 2.1) are considered to have no direct solar radiation if they fall below a
 163 threshold of modelled clear-sky direct and diffuse insolation (Bird and Hulstrom, 1981, model
 164 implemented in *solaR* software, Perpiñán, 2012).

165 Shadow history is defined for the time a surface has spent in shade (t_{shd}, min) (Table 3) and is
 166 determined by comparison of $\overline{BRF}(x, y, t)$ to the prior timestep [$\overline{BRF}(x, y, t - 5\text{min})$]. If a surface
 167 becomes shaded at time t , it has spent $t_{shd}(x, y, t) = 5 \text{ min}$ in shade. For the timestep prior to this ($t - 5$
 168 min), the surface has spent zero minutes in shade and has $t_{shd}(x, y, t - 5\text{min}) = 0 \text{ min}$. A surface that
 169 continues to be in shade [i.e. $\overline{BRF}(x, y, t + 5\text{min}) = -1$] has $t_{shd}(x, y, t + 5\text{min}) = 10 \text{ min}$ at the next
 170 timestep, etc. As a pixel can view a surface that is part sunlit and part shaded across multiple
 171 timesteps, these pixels are designated fully sunlit or fully shaded based on the 10-timestep (50 min)
 172 window around each timestep. If a pixel has $\overline{BRF}(x, y, t) > -1$, is sunlit at $t - 25 \text{ min}$ and shaded at $t +$
 173 25 min , then it is considered partially sunlit at t . In these cases, the following threshold is used to
 174 determine if the observed surface is more shaded than sunlit and $t_{shd}(x, y, t)$ is updated accordingly:

$$t_{shd}(x, y, t) = \begin{cases} 0 & \text{if } BRF(x, y, t) < [0.75 \cdot BRF(x, y, t - 25 \text{ min})] \\ 5 & \text{otherwise} \end{cases} \quad \text{Eqn. 2}$$

175 If $t_{shd}(x, y, t) = 0$, pixels are allocated the maximum $\overline{BRF}(x, y)$ that occurred up to 5 timesteps prior
 176 (i.e. $\max\{\overline{BRF}(x, y, t - 25 \text{ min} \rightarrow 0)\}$) to assign partially shaded pixels with a fully sunlit status.

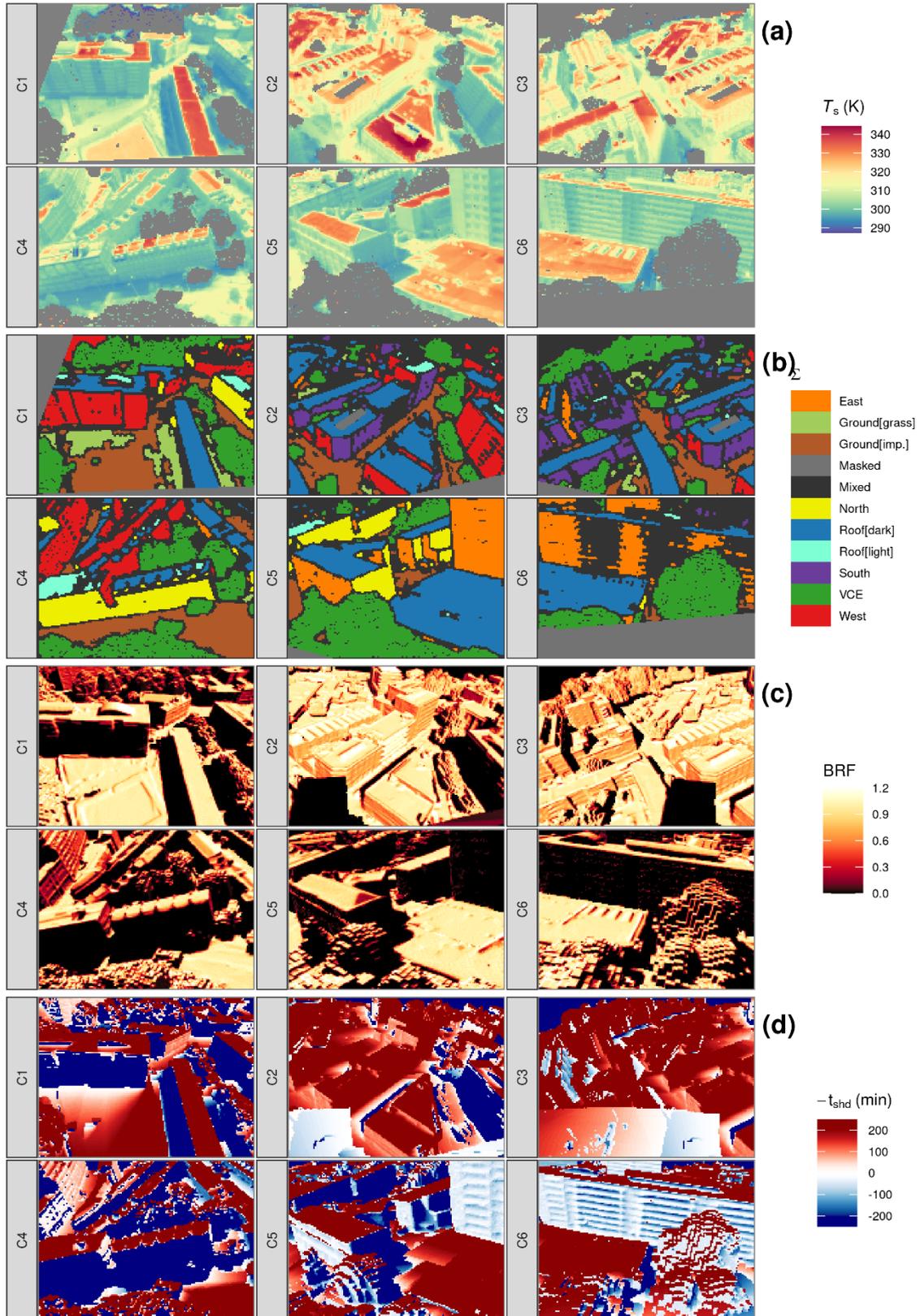


Fig 2. (a) Optris PI longwave infrared (LWIR) camera observations for 27th August 2017 12:00 UTC and (b – d) simulated surface properties projected onto the image plane of “model world” (MW) cameras that simulate the perspective of (a). Surface properties are: (b) orientation and material (Σ), (c) shortwave bidirectional reflectance factor (BRF) to determine sun-surface geometry assuming Lambertian reflecting surfaces, and (d) time surfaces have spent in shade (t_{shd} , white \rightarrow blue) or sun (white \rightarrow red). The cameras (Table 2) are indicated to the left of each image. (a-b) are modified from Morrison *et al.* (2020).

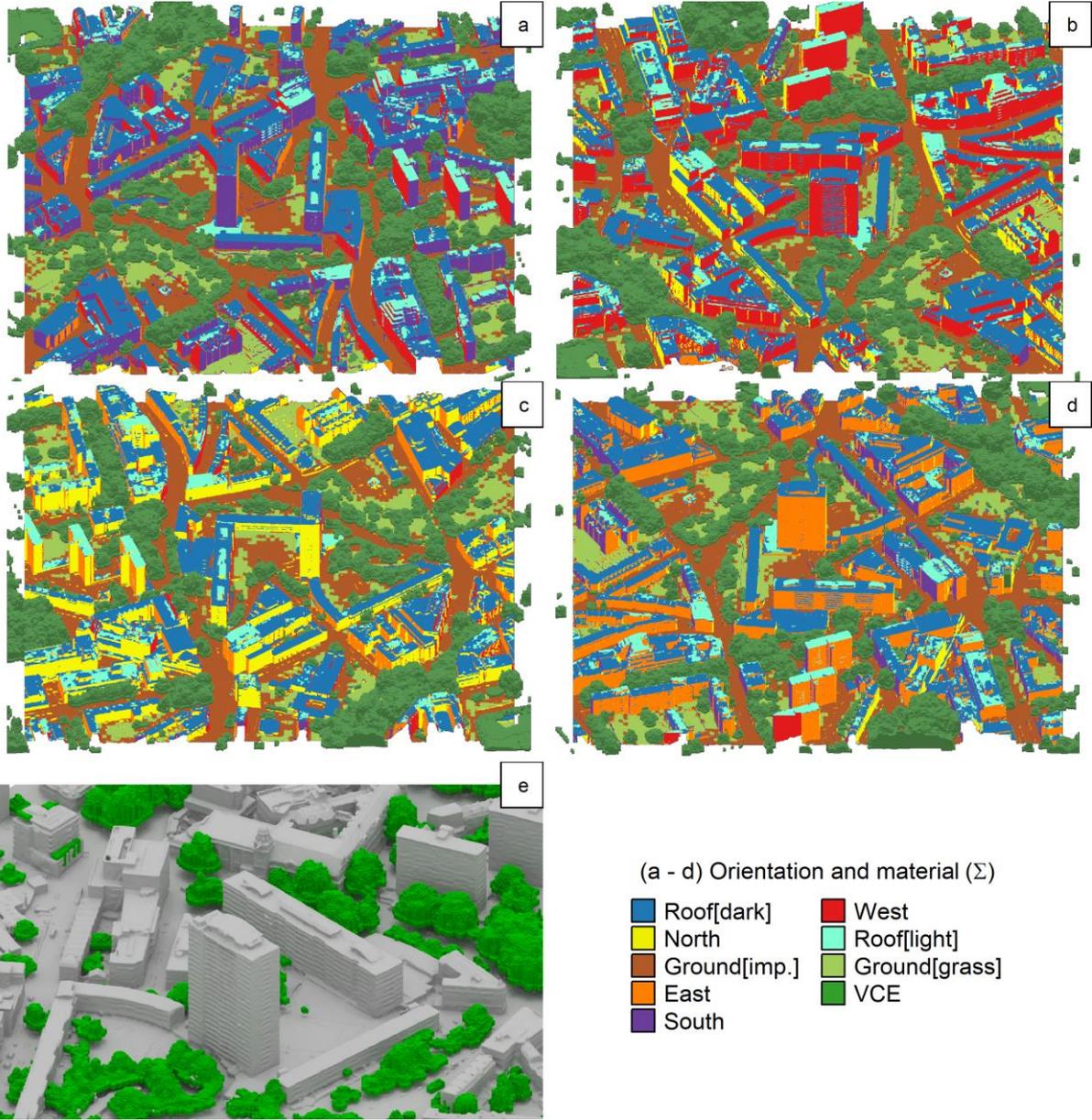
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Table 3. Surface properties of orientation and material (Σ), bidirectional reflectance factor (BRF) and shadow history (t_{shd}) used for per-pixel classification of LWIR camera observations (Fig 2). A surface class (i) has three surface properties: Σ , $\overline{\text{BRF}}$, t_{shd} .

| | Property | Method | Description | Values | Example | |
|-------------------------|--------------------------|--|--|---|---------|--------|
| Σ | Orientation and material | Blender 3D modelling | Cardinal orientation and material | Roof[dark] | South | Fig 2b |
| | | Land cover map | | Roof[light] | West | Fig 3 |
| | | Airborne hyperspectral (Morrison <i>et al.</i> , 2020) | | Ground[imp.] | Down | |
| | | | | Ground[grass] | Mixed | |
| | | | | North | Masked | |
| | | | | East | | |
| $\overline{\text{BRF}}$ | Sun-surface geometry | DART simulation | DART bidirectional reflectance factor (BRF) simulation | BRF binned ($\overline{\text{BRF}}$) as $0 \rightarrow 2$ at $\Delta 0.25$ (unitless). Shaded surfaces ($\text{BRF} < 0.05$) are assigned to bin $\overline{\text{BRF}} = -1$ | | Fig 2c |
| t_{shd} | Shadow history | DART simulation | Time in shade | $0 \rightarrow 2\tau \Delta 5$ (min) | | Fig 2d |



188
 189 Fig 3. Vector digital surface model (DSM) and vegetation canopy elements (VCE) for the study area created from Google
 190 Earth (Google, 2019; Morrison *et al.*, 2020) imagery with (colours) orientation and material surface properties (Σ)
 191 rendered in Blender (Blender, 2018) for off-nadir view directions facing: (a) north, (b) east, (c) south, (d) west and (e)
 192 northeast with focus on the study sites and surface geometry, rendered without Σ . VCE covers a slightly larger area
 193 than the DSM.

194 **2.3. Cooling events**

195 A “cooling event” time window is used to analyse the shadow history (Section 2.2) effect on observed
 196 T_s . This starts when a pixel is sunlit for the last time ($t_{\text{shd}}(x, y) = 0$ min) and ends when it is
 197 substantially cooled ($t_{\text{shd}}(x, y) > n\tau$), with time constant τ (min) and multiplicative factor n . A cooling
 198 event can continue after sunset and across days. To determine a representative time window for
 199 cooling events, τ is calculated using an exponential rate of cooling (Vollmer, 2009) for all pixels that
 200 enter shade as:

$$T_s[a] = T_s[b] + (T_s[c] - T_s[d])e^{-\frac{t}{\tau}} \quad \text{Eqn. 3}$$

201 using T_s observation subsets (Table 4). In Eqn. 3, the T_s difference for recently shaded ($T_s[a]$) and
 202 prolonged shaded ($T_s[b]$, hereafter “ambient” T_s) surfaces throughout the cooling event isolates the
 203 rate of cooling from any ambient variations in surface temperature. The ambient temperature is
 204 included in the cooling event definition as it isolates the direct solar irradiance component of the
 205 surface energy balance from all other energy balance processes. These include variations in sensible
 206 heat exchange (from e.g. wind speed and direction), incoming diffuse radiation (due to e.g. patchy
 207 cloud or day-night transition) and heat storage. After τ minutes, the temperature difference is reduced
 208 to $1/e$ (~ 0.368) of the value at $t_{\text{shd}} = 0$ (Vollmer and Möllmann, 2017).

209 Table 4. Surface temperature sub-classes used to determine exponential cooling (Eqn. 3). See text and Table 3 for
 210 definitions. Cooling event lengths ($n\tau$) have units of minutes

| | Surface temperature (T_s) description | Definition |
|----------|--|--|
| $T_s[a]$ | Pixel T_s with time in shade no longer than $n\tau$ | $T_s(x, y, \Sigma, \overline{\text{BRF}} > -1, t_{\text{shd}} > 0 \ \& \ \leq n\tau, t)$ |
| $T_s[b]$ | Ambient T_s at time t , aggregated (median) from pixels in shade for more than $n\tau$ | $T_s(\Sigma, \overline{\text{BRF}} = -1, t_{\text{shd}} > n\tau, t)$ |
| $T_s[c]$ | Pixel T_s at the timestep prior to shadowing ($t_{\text{shd}} = 0$), i.e. at start of the cooling event ($t = 0$) | $T_s(x, y, \Sigma, \overline{\text{BRF}} > -1, t_{\text{shd}} = 0, t = 0)$ |
| $T_s[d]$ | Ambient T_s at the timestep prior to shadowing ($t = 0$), aggregated (median) from pixels in shade for more than $n\tau$ | $T_s(\Sigma, \overline{\text{BRF}} = -1, t_{\text{shd}} > n\tau, t = 0)$ |

211 Cooling event lengths ($n\tau$) need to be initially estimated. Using all pixels within a day for a given
 212 surface orientation and material, $n\tau$ is set at 15 min and increased incrementally until the majority of
 213 observations are at ambient T_s ; i.e. when $> 68\%$ of pixels with $t_{\text{shd}}(x, y) = n\tau$ have an exponentially
 214 cooled T_s ($T_s[a]$) that is lower than the ambient temperature ($T_s[b]$, median) plus one standard
 215 deviation. Cooling events are only considered if a pixel has a temperature recorded at $t_{\text{shd}}(x, y) = 0$ and
 216 $t_{\text{shd}}(x, y) = n\tau$.

217 To demonstrate cooling events, $T_s(x, y)$ for recently shaded surfaces (Fig 4a, black and grey) and an
 218 aggregated value of all pixels viewing surfaces that have been shaded for an extended ($>n\tau$) period
 219 (“ambient” temperature, Fig 4a, blue) are compared over 1.5 h (Fig 4b is one randomly selected
 220 cooling event). From this, $\tau(x, y, t)$ (Eqn. 3) is estimated using a nonlinear least squares (NLS) model
 221 fit for all per-pixel cooling events (Fig 4b, red). Across all pixels during the study date, the NLS fit of
 222 $\tau(x, y, t)$ is rejected if (1) it contains less than 5 timesteps, (2) the pixel surface property becomes
 223 “mixed” (Section 2.2) at any point during the event, (3) the NLS fit fails to converge, or (4) $\tau(x, y, t) >$
 224 1000 min. A generalised modelled value of τ uses the median value of $\tau(x, y, t, \Sigma)$ determined from all
 225 eligible cooling events across the study date as one representative time constant for three surface
 226 types: roofs, walls, and ground [$\tau(\Sigma)$].

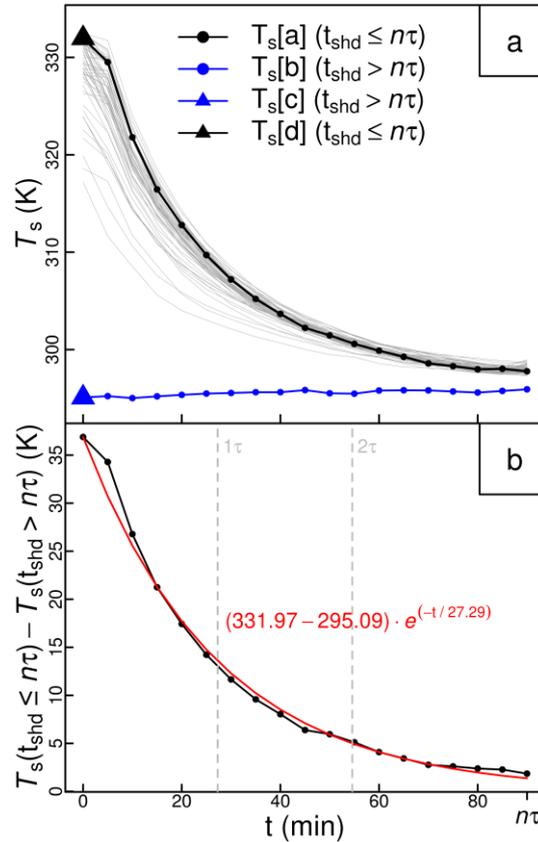


Fig 4. Visual definition and example of “cooling events”. These occur after a surface becomes shaded and are parameterised by an exponential rate of cooling. Shown here for all C3 camera roof-viewing pixels shaded from $t = 0$ and $t = 90$ (min) (10:00 and 11:30 on 27th August 2017) with: (a) all samples (grey lines) and one (random, black) cooling event with the “ambient” surface temperature (blue line) (b) modelled with an exponential fit (red, Eqn. 3) for one (black line from a) cooling event.

3. Observational source area

Of the total model world (MW) surface area ($A_{TOTAL} = 4.1 \times 10^5 \text{ m}^2$, Fig 5), 88.0 % is composed of DSM triangles and the remainder (12.0 %) is from the vegetation canopy elements (VCE) plan area. East and west walls are 23.3 % of A_{TOTAL} compared to 18.3 % for north and south walls. These numbers are not equal as the MW buildings are not cuboids and some are cut off at the MW edges (Fig 3). The ground surfaces (30.3 %) (e.g. streets, parks, courtyards) have greater area than the roofs (15.6 %). Roofs mostly have low albedo (Roof[*dark*], 12.8 %).

The overall camera source area (A_{CAM}) is $38,950 \text{ m}^2$ (9.5 % of A_{TOTAL}), approximated as the summed area of triangles completely within the field of view of any camera. A_{CAM} excludes VCE directly but resolves the occlusion of other surfaces by VCE. Where cameras have overlapping source areas (Fig 1c, Fig 2) the overlapping area is allocated arbitrarily to the camera with lowest ID (Table 2). With A_{CAM} calculated using the DSM triangles (not rendered images), it includes all mixed (“complex” geometry) and masked (near field objects, e.g. roofs directly beneath cameras, Fig 2b) pixels causing a small overestimation of A_{CAM} . A_{CAM} may further underestimate the actual source area of classified pixels, as partially visible triangles (MW camera field of view) are rejected.

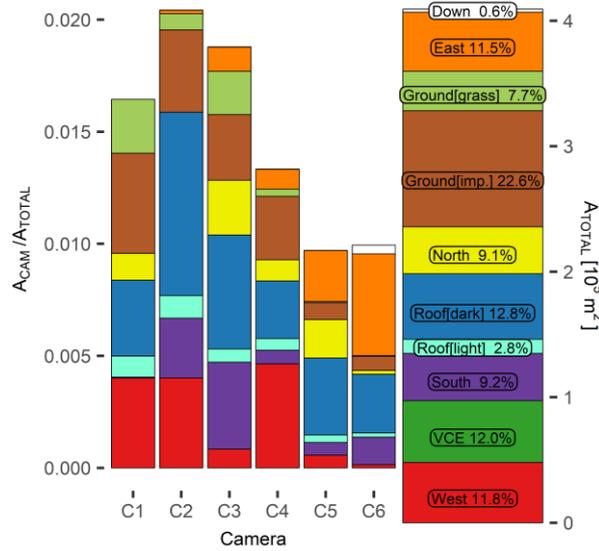


Fig 5. Total three-dimensional study surface area (A_{TOTAL}) and area seen by the LWIR cameras (A_{CAM}) (Table 2) classified by surface and orientation properties (colours).

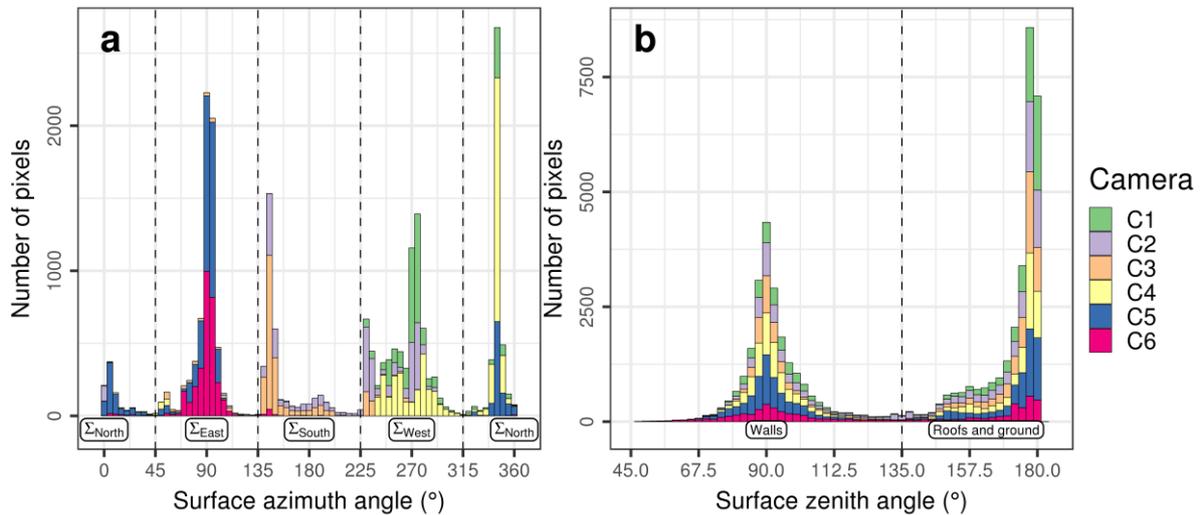
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251 Inter-camera differences in A_{CAM} result from camera siting height, zenith view angle and the
 252 occlusion of far-field surfaces by near-field objects. Located at 75 m agl with an oblique view angle,
 253 camera C2 has the largest source area (2 % of MW area, Fig 5) whereas C5 and C6, mounted at 37 m
 254 agl, have the smallest source areas (~ 1 % of MW each). Roof and ground surfaces are observed by all
 255 cameras. The oblique view angles mean vertical facets substantially contribute to the observational
 256 source area, but the actual vertical facets sampled depends on the camera azimuth. A camera can view
 257 surfaces with opposing directions (e.g. east and west) due to the grouping of the heterogeneous wall
 258 facings into the four cardinal directions.

259 For pixel-level source areas, the manual approach used to determine A_{CAM} (Fig 5) is too time
 260 consuming to conduct for each of the 1.15×10^5 individual pixels. Variations in surface area coverage
 261 across each camera IFOV (instantaneous field of view) are not accounted for and pixels are assumed
 262 to have equal source areas. The azimuth and zenith of DSM triangles within each camera pixel IFOV
 263 are given in Fig 6. The distribution of surface azimuth angles for the walls is uneven (Fig 6a). Some
 264 angles have many samples (maximum = 2677 pixels, for $342.5^\circ \rightarrow 347.5^\circ$) and others far fewer
 265 (minimum = 130 pixels, for $127.5^\circ \rightarrow 132.5^\circ$) as building walls have a few fixed directions and
 266 sensors have limited views (Table 2). Given the complexity of the study area geometry, the azimuthal
 267 facings are well distributed within each wall orientation bin (Fig 6a, between vertical dashed lines)
 268 except for the Σ_{South} where a view bias of southeast facing ($\theta \approx 135^\circ \rightarrow 150^\circ$, Fig 6a) surfaces is
 269 found. This is explained by the southwest-to-northeast street orientation sampled by the northward
 270 facing cameras (C2 and C3).

271 Sloped roofs, chimneys, balconies and other micro-scale geometry resolved in the DSM widen the
 272 surface zenith angle distribution (Fig 6b). The incorrect classification of highly sloped roofs as walls
 273 and the DSM “rounding” of corners over short (< 1 m) distances also contribute towards this broad

274 surface zenith angle distribution. Most observed walls are vertical (median 90.83°) with variability
 275 ($\pm 11.07^\circ$ standard deviation) from the sub-facet wall geometry (e.g. balconies). Roof pixels are
 276 mainly flat (median 176.74°). Here, slight slopes (e.g. 8579 pixels sample roofs with surface zenith
 277 angle between 177.50° and 178.25°) may result from inaccuracies in the DSM, as these pixels most
 278 likely view flat roofs in the RW.



279
 280 Fig 6. Frequency of pixels by surface orientations within the instantaneous field of view (IFOV) of each camera (excluding
 281 vegetation canopy elements (VCE) but including “mixed” and “masked” pixels) for (a) azimuth facing (zenith
 282 angle $< 135^\circ$), and (b) zenith angles of pixels. Azimuth angle of 0° (180°) is north (south) for WGS84 UTM grid
 283 zone 31N. Pixels with a zenith angle of 90° (180°) face vertically (horizontally).

284 4. Surface temperature variability by class

285 To quantify the role of surface class on T_s variability, the permutations of surface class in the
 286 observations (Table 3) are considered by scale:

- 287 1) building scale variability (facet, orientation, and material Σ , e.g. Fig 2b),
- 288 2) sub-facet variability within a surface orientation (e.g. different roof slopes) related to the sun-
 289 surface geometry ($\overline{\text{BRF}}$, e.g. Fig 2c), and
- 290 3) shadow history with high spatial resolution (t_{shd} , e.g. Fig 2d).

291 4.1 Variability from surface orientation and material at the building scale

292 Across all pre-classified observations (Fig 7a, white) the overall T_s difference is 37.5 K between the
 293 5th percentile (P_5) and P_{95} during the period 12:00 – 12:55 (hereafter referred to by time ending, i.e.
 294 13:00). Mixed pixels (Fig 7a, grey), primarily walls with complex small-scale features (e.g. balconies
 295 - C6, Fig 2a, b), are generally cooler than roof and ground surfaces, with a smaller hourly and diurnal
 296 range than the pre-classified temperatures. Hilland and Voogt (2020) resolve these small-scale
 297 features and find self-shading significantly reduces facet averaged T_s by around 1 - 6 K.

298 With our coarsest surface classification (i.e. building facets, orientations and materials) roof T_s , as
 299 expected (Voogt and Grimmond, 2000; Christen *et al.*, 2012; Adderley *et al.*, 2015), has the greatest
 300 diurnal T_s range (Fig 7b, median $\Sigma_{\text{roof[dark]}}$ $290.6 \rightarrow 329.0$ K). T_s across $\Sigma_{\text{roof[dark]}}$ pixels consistently

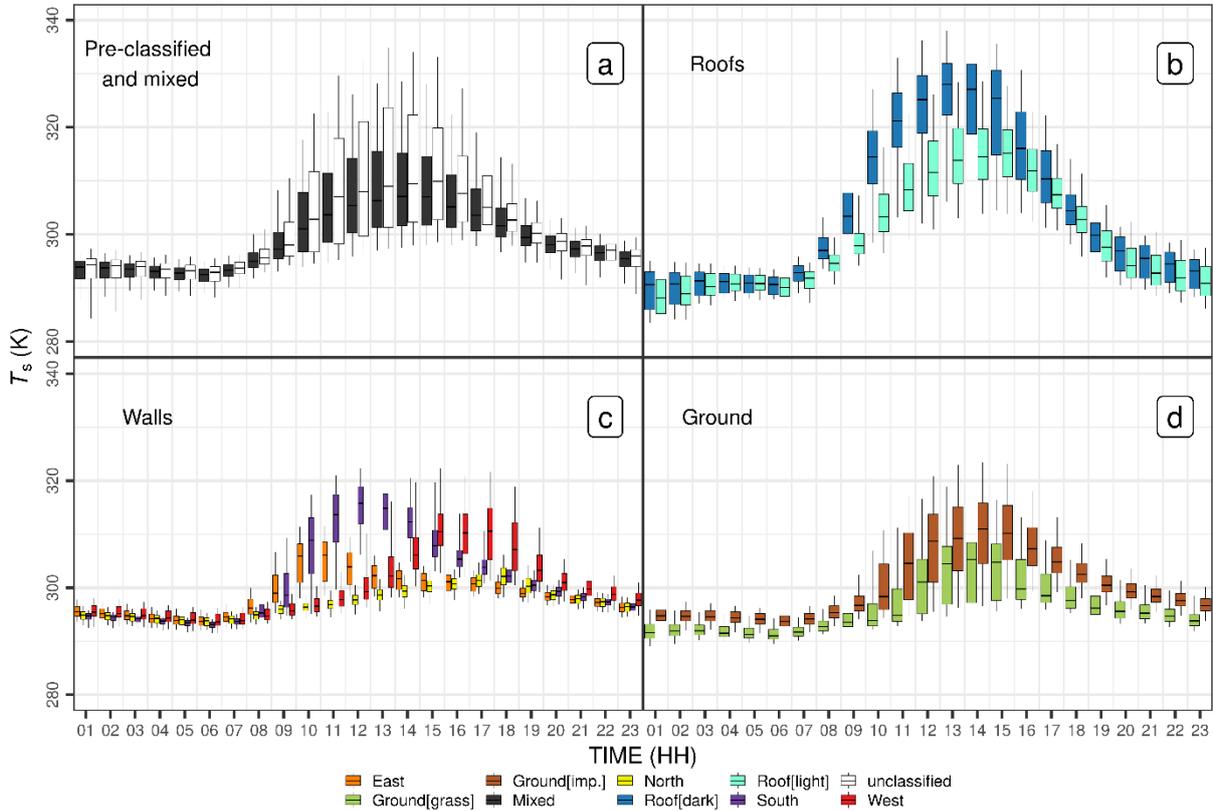
301 shows most variation at all times. Driven by insolation, intra-facet T_s variability for $\Sigma_{\text{roof[dark]}}$ is
302 between 302.1 and 336.3 K (P_5 and P_{95}) at 12:00, with $P_{95} - P_5$ differences consistently over 20 K
303 between 10:00 and 16:00. The higher albedo of $\Sigma_{\text{roof[light]}}$ surfaces means less shortwave radiation is
304 absorbed which leads to lower T_s with median $\Sigma_{\text{roof[light]}}$ (313.8 K) at 13:00 being 14.2 K lower than the
305 coinciding $\Sigma_{\text{roof[dark]}}$ temperature (Fig 7b). Prior to an overcast period in the afternoon (15:30 – 15:55)
306 the two roof types have distinct T_s distributions. The fewer $\Sigma_{\text{roof[light]}}$ pixels are mainly sunlit
307 throughout the day, whereas $\Sigma_{\text{roof[dark]}}$ areas have some within-canopy surfaces affected by prolonged
308 (> 1 h) shadowing. Overcast conditions cause the distributions to slightly converge as the contrasting
309 albedos have reduced effect when only diffuse incident solar radiation is incident. The subsequent
310 lower sun angles reduce the overall shortwave radiative forcing.

311 Grass ($\Sigma_{\text{Ground[grass]}}$) T_s has a smaller diurnal range than impervious ground ($\Sigma_{\text{Ground[imp.]}}$). Grass
312 temperatures are affected by both evaporative cooling and shadowing from grass blades (i.e. leaf area
313 index is greater than 1) whereas the impervious areas lack moisture (4 days since rainfall). Also, the
314 generally higher heat capacities of $\Sigma_{\text{Ground[imp.]}}$ cause more heat to be stored during the day and released
315 slowly over night. Uncertainty in grass T_s may arise from a potential sample bias as only one camera
316 (C1) views this surface class whereas all cameras see some $\Sigma_{\text{Ground[imp.]}}$. The relatively coarse (4 m)
317 land cover dataset (Lindberg and Grimmond, 2011) may introduce unquantified classification
318 uncertainties.

319 Considering wall pixels by cardinal orientation, Σ_{East} (Σ_{West}) pixels are warmest during morning
320 (afternoon), with median T_s reaching 306.1 (310.6) K at 11:00 (17:00). Σ_{West} surfaces peak at higher
321 temperatures than Σ_{East} , as the latter are among the first to be heated in the morning while Σ_{West}
322 surfaces have already been heated throughout the day. Σ_{West} remains warm past sunset (sunset at
323 ~18:55 UTC) and is 1.2 K warmer than Σ_{North} at 23:00 (differences in per-pixel median). This is
324 reasonable given Σ_{North} pixels are mainly shaded throughout the day so that their T_s is consistently low
325 with less variability. Shortly prior to sunset, Σ_{North} surfaces receive a little direct solar irradiation
326 which causes their T_s to be slightly greater than that of Σ_{East} pixels in the evening. The T_s medians
327 across wall orientations consistently differ by over 10 K between 10:00 and 15:00 (maximum
328 difference is 18.1 K at 12:00).

329 The sampling bias of south-east walls (Section 3) causes the median T_s for Σ_{South} to peak (315.8 K) at
330 12:00, i.e. earlier than would be expected for a wall distribution centred around 180° azimuth. Before
331 sunrise, median T_s differences between wall orientations are less than 0.8 K but are up to 4.9 K
332 warmer than $\Sigma_{\text{Roof[dark]}}$ at 01:00 during a clear-sky nocturnal period (consistent with e.g. Lagouarde *et*
333 *al.*, 2004). During daytime, walls are generally much cooler than roofs. Their complex geometry and
334 material compositions contribute to wall T_s variability. The study area roofs are mostly planar with
335 small features (e.g. chimneys and air conditioning units) whereas walls have many balconies and

336 other shade-causing features that reduce their overall temperature. As glass emissivity is unaccounted
 337 for, wall T_s may be overestimated (Morrison *et al.*, 2020). Glass and windows (“ Σ_{Glass} ”) were not
 338 classified as the resolution of data used to construct the DSM (Google Earth images, Morrison *et al.*,
 339 2020) is too coarse. No buildings in the study area have fully glazed walls and glass windows are
 340 assumed to be evenly sampled across all cameras.



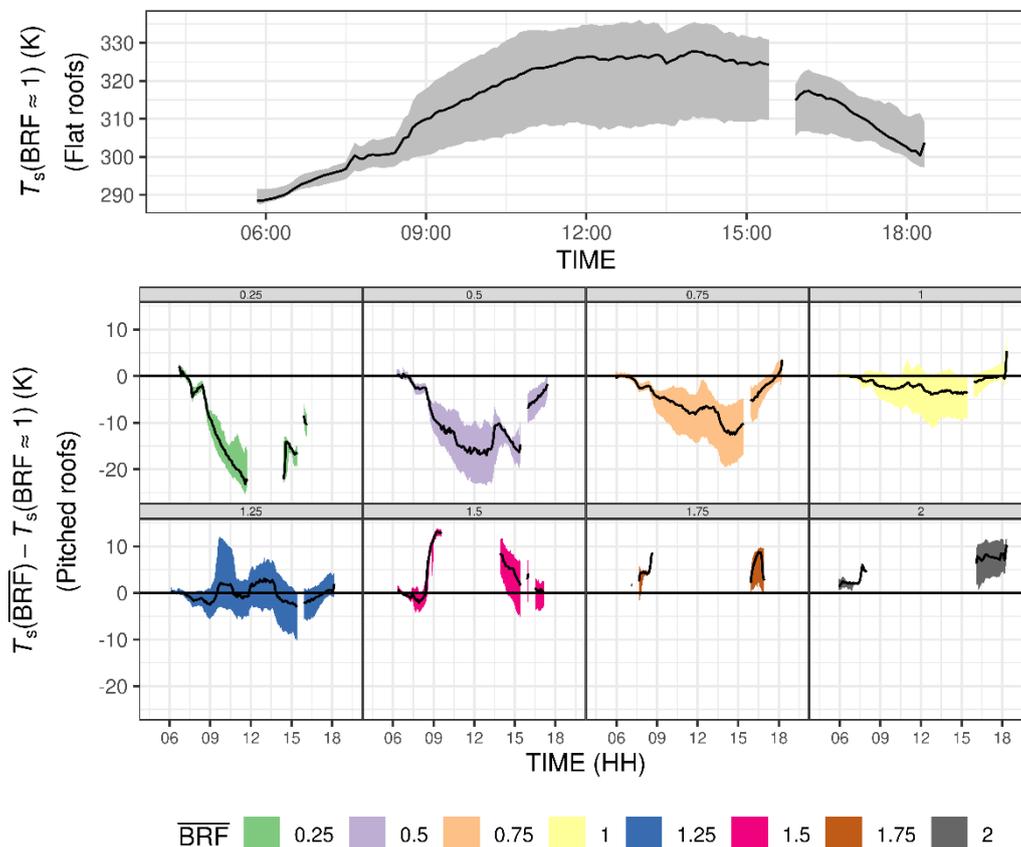
341 Fig 7. Variability of LWIR camera derived surface temperature (T_s) for 27th August with observations classified as (a)
 342 unclassified (white) (except vegetation canopy elements and “masked” and “mixed” (grey) pixels), (b) roofs,
 343 and (c) walls, and (d) ground. Boxplots use data from all camera images (5 min samples) by group (colour) during 1 h (e.g. first hour is
 344 00:00 → 00:55 for Time (HH) “01” between vertical lines) with interquartile range (box), median (horizontal line) and 5
 345 and 95 percentiles (whiskers) of pixel values.

347 4.2 Variability from shortwave irradiance

348 T_s by facet (orientation and material) have positive correlation with irradiance using sun-surface
 349 geometry (bidirectional reflectance factor, $\overline{\text{BRF}}$) (cf. Fig 2a, c). To assess the importance of BRF as a
 350 driver for T_s of the low albedo roofs ($\Sigma_{\text{Roof[dark]}}$), the difference between sunlit flat [$T_s(\text{BRF} \approx 1)$] and
 351 all other binned sun-surface geometry configurations [$T_s(\overline{\text{BRF}})$] for roofs (Fig 8) is calculated through
 352 a day. Overall, there is clear separation in T_s between $\overline{\text{BRF}}$ bins. At 09:15, median T_s differences
 353 between sloped and flat sunlit roofs reach 13.2 K [$T_s(\overline{\text{BRF}} = 1.5) - T_s(\text{BRF} \approx 1)$, Fig 8]. Sloped roofs
 354 with $\overline{\text{BRF}} < 1$ but still sunlit have median T_s up to 23.3 K cooler than the flat roofs at 11:55.
 355 Contributions to the observed T_s variability within each $\overline{\text{BRF}}$ bin at a given timestep are linked to the
 356 variable time in sun (Fig 2d), differences in surface albedo and emissivity within the $\Sigma_{\text{Roof[dark]}}$ surface
 357 property, and uncertainties in atmosphere and emissivity corrections (Morrison *et al.*, 2020).

358 During the overcast period (15:30 – 15:55) when $\overline{\text{BRF}} = -1$ for all surfaces, there are smaller
 359 differences in $T_s(\overline{\text{BRF}})$ which persists into the evening (Fig 8). A subset of all possible roof slope
 360 angles are sampled, meaning some arrangements of sun-surface angles (and therefore $\overline{\text{BRF}}$) are not
 361 observed for sloped roofs. This results in gaps of $T_s(\overline{\text{BRF}})$ at times (e.g. $T_s(\overline{\text{BRF}} = 0.25)$) for around
 362 12:00 → 14:00). Large gaps (> 4 h) for high BRF bins ($\overline{\text{BRF}} > 1.25$) occur with high sun angles (i.e.
 363 peaks in $E_{\lambda}^{\downarrow, \text{dir}}$, Eqn. 1). During these gaps the near-flat roofs are irradiated most and $T_s(\overline{\text{BRF}} = 1.25)$ is
 364 the highest physically possible bin around midday ($\pm \sim 2.5$ h) for the study site latitude and
 365 corresponding solar elevation maximum.

366 Applied to vertical facets (Supplementary material 1), this sun-surface geometry analysis shows most
 367 T_s variation is captured by wall orientation (Fig 7c). For ground surfaces, most observations are of flat
 368 ground (i.e. $\text{BRF} \approx 1$).



369
 370 Fig 8. Observed daytime roof surface temperature (T_s) for 27th August for pixels classified with bidirectional reflectance
 371 factor (BRF, Schaepman-Strub *et al.*, 2006) (top) equivalent to solar irradiance for a flat surface ($\text{BRF} \approx 1$) and (bottom)
 372 by $\overline{\text{BRF}}$ (bin width 0.25) as difference from $\text{BRF} \approx 1$ (i.e. across all observed sun-surface geometries). DART calculated
 373 BRF assuming Lambertian surfaces.

374 4.3 Variability from shadow history

375 Shadow history has a potentially significant impact on T_s variability given the large and variable
 376 thermal inertia of urban materials (e.g. concrete, Arnfield and Grimmond, 1998). We explore the
 377 micro-scale persistence effects of shadows on upwelling longwave radiation with thermography

378 (Meier *et al.*, 2010) with multiple cameras and objectively determined shadow distributions across the
379 images.

380 For the study day, 1.15×10^6 per-pixel cooling events $[\tau(x, y, t, \Sigma)]$ are identified from all cameras
381 (Fig 9). The model fits for each cooling event (Section 2.3) have mean absolute error (MAE) of 0.7 K
382 (ground, roof) or 0.6 K (walls) and are linear (red dashed line, Fig 9 row 1) across the range of T_s
383 differences (approx. $0 \rightarrow 30$ K). A small number of points have negative differences, indicating the
384 shaded ambient T_s is warmer than the recently shaded T_s . Through manual inspection, negative
385 differences for roofs pixels are associated with microscale features in the foreground roof of C6
386 (approx. centre of image, Fig 2a). These roof features may have low emissivity materials or complex
387 geometry unresolved by the DSM. Negative differences for walls are explained by C2's $\Sigma_{\text{West}}(x, y)$
388 pixels near the building with $\Sigma_{\text{Roof[light]}}$ (Fig 2b). This concrete wall extends above the canyon height so
389 that the relatively high sky view factor and direct solar illumination until sunset are likely causing
390 recently shaded T_s to be lower temperature than the ambient reference. The latter is more
391 representative of warmer inside-canyon walls. Overall, these departures from exponential cooling give
392 the flat “tail” to the scatter (e.g. Fig. 9, wall, row 1), as negative modelled values are not permitted.
393 Negative differences account for 1.3 % of all cooling events (sunlit - shaded difference of -2.5 K at
394 P₅).

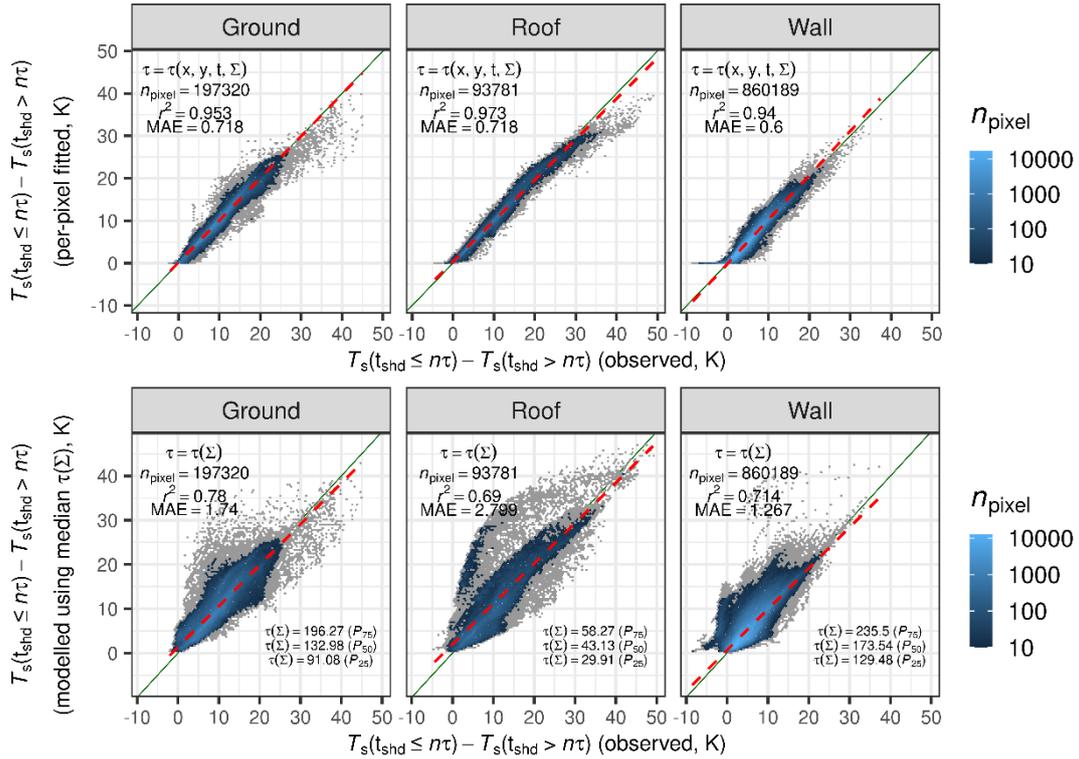


Fig 9. Surface temperature (T_s) cooling rates observed (x axis) and estimated (using Eqn. 3) for each pixel with pixels numbers (n_{pixel}) indicated (colours) with (row 1) fitted time constant τ per pixel [$\tau(x, y, t, \Sigma)$] and (row 2) modelled time constant as median $\tau(x, y, t, \Sigma)$ per surface type [$\tau(\Sigma)$] for (column 1) ground (grass and impervious), (column 2) roof (light and dark) and (column 3) walls (N, E, S, W). Statistics: coefficient of determination (r^2), mean absolute error (MAE, K).

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401 The generalised values of τ [$\tau(\Sigma)$] (Fig 9 row 2 labels), determined from the median of $\tau(x, y, t, \Sigma)$
 402 pixels (Section 2.3), allow inter-facet T_s cooling rates to be compared. Roofs generally cool much
 403 faster ($\tau(\Sigma_{\text{Roof}}) = 43.13$ min) than ground ($\tau(\Sigma_{\text{Ground}}) = 132.98$ min) and walls, which cool around four
 404 times slower ($\tau(\Sigma_{\text{Walls}}) = 173.54$ min). As $\tau(x, y, t, \Sigma)$ is highly variable (e.g. $\tau(\Sigma_{\text{Ground}})$ is 91.08 \rightarrow
 405 196.27 min for $P_{25} \rightarrow P_{75}$), using these generalised median values of $\tau(x, y, t, \Sigma)$ results in a greater
 406 spread between observed and modelled results (Fig 9 cf. row 1 and 2). There is generally good
 407 agreement between observed cooling rates and the generalised modelled results (Fig 9 row 2) but with
 408 some large (> 10 K) departures when facets have distinctly different thermal properties. Uncertainty is
 409 increased for roofs as their shading during daytime can only be from micro-scale roof geometry or
 410 from nearby taller buildings (e.g. Fig 2b, foreground of C2 and C3) which is mostly confined to short
 411 periods. This reduces the number of pixels available for the ambient T_s estimation (Section 2.3).
 412 Additionally, the emissivity correction uncertainty is greatest for roof surfaces because of the large
 413 contrast between LWIR irradiance (from the relatively cool sky) and LWIR exitance (Morrison *et al.*,
 414 2020).

415 Instances of poor model agreement for ground pixels may arise from the highly contrasting material
 416 properties (impervious and grass), whereas for walls the more complex surface geometry may lead to
 417 uncertainties in shadow patterns and history. Walls also have a mix of glass and masonry/concrete
 418 with their contrasting thermal properties and cooling rates not accounted for.

419 The cooling rate model and the spread in Fig 9 (row 2) are summarised (Table 5) using a subset of
 420 observations (P_{95} differences between recently shaded and ambient after 10 minutes in shade, to
 421 represent surfaces that have been heated by the sun throughout the day) modelled at various times in
 422 shade using $\tau(\Sigma)$ values. After 10 min, these recently shaded roofs differ most to the ambient
 423 temperature (27.5 K warmer than ambient). They exponentially cool the fastest (2.1 K warmer than
 424 ambient after 90 min using $\tau(\Sigma_{\text{Roof}})$ P_{50} , 0.7 K \rightarrow 4.1 K across interquartile range - IQR) as $\tau(\Sigma_{\text{Roof}})$ is
 425 lower than $\tau(\Sigma_{\text{Wall}})$ and $\tau(\Sigma_{\text{Ground}})$. The higher $\tau(\Sigma)$ for walls and ground means there are still significant
 426 differences to the ambient temperature after long periods of cooling. After 90 min the walls are 8.8 K
 427 (7.1 K \rightarrow 10.3 K IQR) warmer than ambient.

428 Table 5. Differences in surface temperature (T_s) between recently shaded surfaces (i.e. short t_{shd} - time in shade) and a
 429 reference ambient $T_s(t_{\text{shd}} > n\tau)$ for 95th percentile (P_{95}) of observed thermal camera measurements in central London
 430 (27th August 2017) modelled (Section 2.3) at t_{shd} of 30, 60 and 90 min using observationally derived cooling time
 431 constants (τ) for each surface type. E.g. where recently shaded ground is 21.6 K warmer than ambient after $t_{\text{shd}} = 10$
 432 min, this difference exponentially reduces to 18.6 K after 30 min (17.3 K \rightarrow 19.5 K interquartile range using 196.27
 433 min \rightarrow 91.08 min time constants) using time constant $\tau(\Sigma) = 132.98$ (Fig 9 row 2 ‘‘Ground’’ label) and assuming no
 434 change in ambient temperature. See Fig 9 for all $\tau(\Sigma)$ percentiles and Eqn. 3 for exponential cooling model.

| Recently shaded - ambient $T_s(t_{\text{shd}} \leq n\tau) - T_s(t_{\text{shd}} > n\tau)$ (K) | Time in shade (t_{shd}) | | | | | | | | | |
|---|------------------------------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| | 10 min | 30 min | | | 60 min | | | 90 min | | |
| | observed | P_{25} | P_{50} | P_{75} | P_{25} | P_{50} | P_{75} | P_{25} | P_{50} | P_{75} |
| Ground | 21.6 | 17.3 | 18.6 | 19.5 | 12.5 | 14.8 | 16.7 | 6.5 | 9.4 | 12.3 |
| Roof | 27.5 | 14.1 | 17.3 | 19.5 | 5.2 | 8.6 | 11.7 | 0.7 | 2.1 | 4.1 |
| Walls | 16.5 | 14.1 | 14.7 | 15.2 | 11.2 | 12.4 | 13.3 | 7.1 | 8.8 | 10.3 |

435
 436 Previous observations acknowledge that shaded surface temperatures exhibit variation from shadow
 437 histories (Voogt, 2008; Morrison *et al.*, 2018), but often aggregate the shaded temperatures to a single
 438 value. This work demonstrates the possibility to stratify shaded temperatures instead by shadow
 439 history using a simple exponential rate of cooling. Variability in τ is directly related to variability in
 440 heat transfer rate (radiative, convective, and conductive), material heat capacities, density, volume,
 441 and overall mass of the observed surface structures. For example, rapid cooling rate of roofs (median
 442 cooling time constants $\tau(\Sigma_{\text{Roof}}) = 43.13$ min) may be explained by a lower mass (cf. walls, Xu and
 443 Asawa, 2020) facilitating conductive heat loss, higher sky view factor (facilitating radiative heat
 444 transfer), and exposure to higher wind speeds (facilitating convective heat transfer).

445 5. Conclusions

446 Analysis of a fusion of observation (ground-based thermography) and modelling (urban geometry,
 447 material properties, sensor views and radiative transfer processes) data on a mainly clear-sky summer
 448 day in central London are used to explore various drivers of surface temperature (T_s) variability. With
 449 a very high level of detail surface description and integrated sensor view modelling, the camera
 450 source area analysis is unprecedented for such a complex (i.e. realistic) urban setting. General and
 451 study specific conclusions about the observation process are:

- 452 • Cameras installed on higher buildings have a better vantage and larger source area.

- 453 ○ In this study, the source area is 15.6 % roofs, 41.6 % walls (~10 % per cardinal
454 direction) and 22.6 % ground (remainder above ground vegetation).
455 ○ Even with six cameras the source area is only 9.5 % of the overall area (430 m x 430
456 m horizontal extent).
457 ○ All pixels are assumed to sample equal portions of the surface yet in reality the
458 surface area covered by a pixel varies across the image due to viewing geometry.
459 Future work should investigate methods to weight aggregated observations by per-
460 pixel source area.

461 Objective image classification separates drivers of T_s variability without requiring manual image
462 classification or statistical inference.

- 463 • Observed T_s is highly variable.
 - 464 ○ In this study the 5th - 95th percentile differences in per-pixel T_s observations reach up
465 to 37.5 K during daytime.
 - 466 ○ Diurnal patterns of T_s for surfaces with different orientation show general agreement
467 with prior studies at similar latitude.

468 Highly detailed image classification enables T_s variability to be quantified in direct relation to the
469 sun-surface geometry features, including the amount of short- and long-wave radiation incident
470 onto a surface, driving shadow patterns, direct solar irradiance and radiation trapping between
471 buildings.

- 472 • Material properties are especially important for roof surfaces with increased access to solar
473 radiation and high exposure to the cold sky. This effect is expected to be particularly
474 important for thermal spaceborne earth observation, where near-nadir remote sensing
475 observations have a view bias of horizontal facets.
- 476 • Variability of T_s is driven by surface orientation to the sun of the facet (e.g. walls, roofs,
477 ground) and sub-facet characteristics (e.g. flat or sloped roofs, high or low albedo roofs).
- 478 • Variation in surface temperature across a single facet can be of similar magnitude to the
479 variation between the median temperatures of different facet types.
 - 480 ○ Across all roof pixels within a given hour (i.e. intra-roof) 5th - 95th percentile T_s
481 differences are consistently over 20 K between 10:00 and 16:00 (max 34.2 K between
482 11:00 and 11:55)
 - 483 ○ Intra-roof variation is driven by sun-surface geometry effects. T_s differences between
484 flat and sloped roofs reach 23.3 K around midday.
 - 485 ○ Pixel-level temperatures of walls stratified by cardinal direction and aggregated to
486 median values (i.e. inter-wall) differ by up to 18.1 K between north (median 297.7 K)
487 and south (median 315.8 K) facets around midday. Including roof and ground face T_s ,

488 median differences reach 29.3 K at 13:00 between the low albedo roof (median 328.0
489 K) and north facing wall (median 298.7 K).

490 The second important driver of T_s variability are shadows. For the first time, the effect of shadows
491 through time on T_s is quantified across a real convoluted urban surface.

- 492 • The history of surface shadows greatly affects T_s . Recently shaded roof surfaces are up to 27.5 K
493 warmer than those in shade for long periods.
- 494 • Cooling characteristics were modelled from observations using exponential functions with time
495 constants (τ) estimated relative to long-term shaded surface temperatures. Clear contrasts were
496 found between facet types: roofs on average cool much faster $\tau(\Sigma_{\text{Roof}}) = 43.13$ min than ground
497 $\tau(\Sigma_{\text{Ground}}) = 132.98$ min and walls $\tau(\Sigma_{\text{Walls}}) = 173.54$ min.
- 498 • Surfaces shaded at sunset will have cooled to within 5 % of the ambient temperature by $\sim 3\tau$ i.e.
499 over 6 h and 8.5 h into the night for ground and walls, respectively.
- 500 • This shadow history methodology could be extended to study recently sunlit temperatures.

501 Material properties determine the amount of incoming energy absorbed.

- 502 • Using simple albedo characteristics (i.e. two classes “light” (high albedo) and “dark” (low
503 albedo); excluding any metal or glass) clearly separates observed temperature distributions.
 - 504 ○ Dark roofs are up to 14.2 K warmer during the day as more solar radiation is absorbed.
- 505 • Material classification would benefit from more detailed data (e.g. surface optical material
506 properties), particularly for glass and windows which can directionally scatter longwave radiation
507 (e.g. specular reflections) and confound the T_s retrieval (Morrison *et al.*, 2020). Further
508 classification requires more detailed visible imagery from e.g. Google Street view, (Li *et al.*,
509 2018; Gong *et al.*, 2018), study-specific vehicle traverses (Hilland and Voogt, 2020) or manual
510 inspection (Christen *et al.*, 2012).

511 Overall, the combination of a relatively large fraction of vegetation, complex geometry and associated
512 T_s distributions give a unique temporally continuous dataset. Observations and the underlying
513 methods for their retrieval and classification could be used as input and to evaluate unstably stratified
514 large eddy simulation modelling (Gronemeier *et al.*, 2017) and building energy balance models
515 (Bueno *et al.*, 2012), or input to radiative transfer models such as DART (Gastellu-Etchegorry *et al.*,
516 2015) for evaluation of effective thermal anisotropy (Krayenhoff and Voogt, 2016; Morrison *et al.*,
517 2018; Wang *et al.*, 2018).

518 These data provide useful insights for meso-scale weather and larger scale climate models which
519 simplify the urban surface to facets (Masson, 2000; Harshan *et al.*, 2018) assuming flat roofs with a
520 uniform height (Harman *et al.*, 2004; Krayenhoff and Voogt, 2007). Both the extent of intra-facet
521 surface temperature variability and the net surface cooling rate variability provide some insights into

522 the processes that are “averaged” into composite values. Through ensemble modelling, the
523 implications of this variability on averaged flux calculations and therefore weather/climate predictions
524 should be assessed. For many of the larger spatial and temporal extent applications, further
525 observations should assess how representative our study results are with respect to time of year and
526 location (across London, other cities).

527

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