

Intensity change of binary Tropical Cyclones (TCs) in idealized numerical simulations: two initially identical mature TCs

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1	Intensity Change of Binary Tropical Cyclones (TCs) in Idealized Numerical
2	Simulations: Two Initially Identical Mature TCs
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Abstract

This study investigates the intensity change of binary tropical cyclones (TCs) in idealized 24 25 cloud-resolving simulations. Four simulations of binary interaction between two initially identical mature TCs of about 70 ms⁻¹ with initial separation distance varying from 480 to 840 km are 26 conducted in a quiescent *f*-plane environment. Results show that two identical TCs finally merge 27 28 if their initial separation distance is within 600 km. The binary TCs presents two weakening stages 29 (stages 1 and 3) with a quasi-steady evolution (stage 2) in between. Such intensity change of one TC is correlated with the upper-layer vertical wind shear (VWS) associated with the upper-level 30 anticyclone (ULA) of the other TC. The potential temperature budget shows that eddy radial 31 32 advection of potential temperature induced by large upper-layer VWS contributes to the weakening of the upper-level warm core and thereby the weakening of binary TCs in stage 1. In stage 2, the 33 upper-layer VWS first weakens and then re-strengthens with relatively weak magnitude, leading to 34 35 a quasi-steady intensity evolution. In stage 3, due to the increasing upper-layer VWS, the non-36 merging binary TCs weaken again until their separation distance exceeds the local Rossby radius 37 of deformation of the ULA (about 1600 km), which can serve as a dynamical critical distance 38 within which direct interaction can occur between two TCs. In the merging cases, the binary TCs 39 weaken prior to merging because highly asymmetric structure develops as a result of strong horizontal deformation of the inner core. However, the merged system intensifies shortly after 40 41 merging.

43 **1. Introduction**

When two tropical cyclones (TCs) interact with each other, errors in both track and intensity 44 forecasts are often larger than those for a single TC (Brand 1970; Jarrell et al. 1978; Liu and Tan 45 2016). Fujiwhara (1921, 1923, and 1931) first demonstrated the interaction of two vortices in 46 47 proximity in the tank experiments and found that the two cyclonic vortices rotated counterclockwise, moved toward each other, and finally merged (i.e., Fujiwhara effect). In the real 48 atmosphere, binary TCs are detected by using various statistical parameters such as their intensities, 49 relative locations, coexistence time and separation distance. The critical separation distance 50 determining whether two TCs belong to binary TCs ranges from 1300 to 1800 km (Brand 1970; 51 52 Dong and Neumann 1983; Wu et al. 2011; Jang and Chun 2015a; Ren et al. 2020). Within the critical separation distance, the motion of binary TCs presents mutual approaching, mutual cyclonic 53 orbiting, or mutual escaping (Brand 1970; Dong and Neumann 1983; Lander and Holland 1993, 54 55 hereafter LH93). Sometimes mutual anticyclonic rotation of binary TCs happens under the 56 influence of the large-scale environmental flow such as the subtropical high (Dong and Neumann 57 1983; LH93). Real case studies show that the weaker and smaller TC is susceptible to the stronger 58 and larger TC in a binary system, where the former looks like moving around the latter (Wu et al. 59 2003; Yang et al. 2008). Moreover, during the binary interaction, filamentation and deformation occurred in the weaker and smaller TC Typhoon Alex (1998), which finally became a spiral band 60 61 of the stronger and larger Typhoon Zeb (1998) on satellite images (Kuo et al. 2000). 62 More details relating to the motion and structure change of binary TCs have been investigated

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in idealized frameworks (Chang 1983; DeMaria and Chan 1984; Wang and Zhu 1989a,b; Waugh 63 1992; Dritschel and Waugh 1992; Ritchie and Holland 1993; Wang and Holland 1995, hereafter 64 WH95; Falkovich et al. 1995; Khain et al. 2000; Prieto et al. 2003; Shin et al. 2006; Jang and Chun 65 2015b, hereafter JC15b). Several barotropic dynamical processes have been discussed in the 66 67 literature. For example, the horizontal vorticity advection is key to whether the binary TCs may approach each other in nondivergent barotropic model (DeMaria and Chan 1984; Wang and Zhu 68 69 1989a,b; Shin et al. 2006), while competition between the deformation and filamentation from the opposite vortex and the restoring force of the vortex itself determines whether the two interacting 70 vortices merge or not (Dritschel and Waugh 1992; Waugh 1992; Ritchie and Holland 1993; Prieto 71 72 et al. 2003).

73 The binary interaction in three-dimensional models is more complicated by resolving the 74 baroclinic TC structure, surface friction, and diabatic heating (Chang 1983; Falkovich et al. 1995; 75 WH95). Compared with dry simulations, diabatic heating can modulate the vortex structure in 76 moist simulations, in which the vortices show relatively axisymmetric structure during the merging 77 (WH95; Khain et al. 2000). WH95 found that two identical TC vortices with the initial separation 78 distance less than 640 km on an *f*-plane experienced rapid mutual approaching and weakening 79 before merging. They also indicated that the merger of binary TCs was a bottom-up process where 80 the low-level vortices merged first, followed by the merging of the middle-level vortices with much 81 stronger filamentation. The simulation of WH95 also demonstrated a mutual orbiting process, followed by release and escape, or merging, which was consistent with the conceptual model of 82

binary interaction proposed by LH93. More recently, JC15b demonstrated that greater
environmental convective available potential energy and higher maximum potential intensity could
lead to stronger binary interaction, while the beta-effect could weaken the mutual approaching of
binary TCs by generating asymmetric structure.

Although previous studies have revealed many features of binary-TCs interaction, most of 87 them focused on the track characteristics of two interacting vortices. Limited studies have 88 investigated the intensity changes of binary TCs. In addition, the coarse model resolution and the 89 use of cumulus parameterization in previous studies are not adequate for understanding the 90 intensity change of binary TCs (e.g., WH95; Khain et al. 2000; JC15b). In this study, we will 91 92 examine the intensity change of two interacting TCs and understand the involved dynamical processes using an idealized three-dimensional full-physics model. The rest of the paper is 93 94 organized as follows. The numerical model and experimental design are described in section 2. 95 Section 3 discusses the main results with the focus on the storm structure and intensity changes of 96 the simulated binary TCs. Summary and conclusions are given in the last section.

97 2. Numerical model and experimental design

98 *a. Model setup*

In this study, the advanced Weather Research and Forecasting (WRF) model version 3.4
(Skamarock et al. 2008) was used to investigate the interaction between two TCs. The WRF model
is a three-dimensional nonhydrostatic, full-physics, atmospheric model. The model domain was
configured with two nested interactive meshes of 901×901 (D01) and 901×901 (D02) grid points,

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with their horizontal grid spacings of 9 and 3 km, respectively. The open lateral boundary condition 103 was utilized for D01. The model atmosphere had 50 vertical levels topped at the 25-km height 104 105 (about 28 hPa) with 18 vertical levels below the 3-km height. The model physics included the WRF 5-class microphysics scheme (WSM5; Hong et al. 2004) and the Yonsei University planetary 106 boundary layer (PBL) scheme (YSU; Hong et al. 2006). The Kain-Fritsch cumulus 107 108 parameterization scheme (Kain and Fritsch 1990) was applied only in D01. The scheme for drag 109 and enthalpy coefficients was *Donelan* Cd + *Constant* Ck (Donelan et al. 2004). The radiations were not activated in this study. All experiments were performed on an *f*-plane at 20°N over ocean 110 111 with a uniform sea surface temperature (SST) of 28°C.

112 *b. Initial vortex*

113 The initial axisymmetric vortex for all experiments of binary TCs was spun up from a single TC integration (ORIG). In ORIG, the Jordan sounding (Jordan 1958) was used as the unperturbed 114 environment. The initial vortex in ORIG had the radial profile of tangential wind following that in 115 Fiorino and Elsberry (1989). The maximum tangential wind speed was 30 m s⁻¹ at the radius of 120 116 117 km (RMW) with the exponential decaying factor of 1.0. The maximum wind decreased with height 118 to zero at about 100 hPa following Wang (2007). The vortex in ORIG was initially located at the center of the two meshes and spun up for 96 hours when the storm reached its mature stage. We 119 separated the axisymmetric vortex of the TC after the 96-h simulation as the initial vortex and used 120 121 the mean fields after removing the axisymmetric vortex as the environmental fields in all binary-122 TCs experiments. The vortex separation followed that in Liu and Tan (2016), which was an

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extension of the method introduced by Cha and Wang (2013) and included the following four steps. 123 First, a local three-point spatial filter was conducted, respectively, in the meridional and zonal 124 125 directions to separate the basic field and the disturbance field. Second, a cylindrical filter was applied to further extract the vortex component from the disturbance field. Third, the axisymmetric 126 TC vortex was calculated as the azimuthally averaged vortex component. Finally, the 127 128 environmental field was obtained by spatially averaging the total field excluding the axisymmetric 129 vortex. More details can be found in Cha and Wang (2013) and Liu and Tan (2016), and references therein. Figure 1a shows the obtained axisymmetric tangential and radial wind fields of the TC 130 vortex after the 96-h spinup in ORIG. The RMW at the top of the boundary layer was about 60 km 131 132 and tilted radially outward with height. The inflow was below 2 km, and the outflow occurred 133 mainly in the upper troposphere. The anticyclonic circulation in the upper troposphere (above the 14-km height) was outside of a radius of about 500 km from the TC surface center. The 134 135 environmental sounding was very close to the Jordan sounding (not shown).

To ensure the validity of the initial conditions composited by the axisymmetric TC vortex and the mean environmental field in our binary-TCs experiments, we first ran a simulation using a single TC initial condition as a reference (CTRL). Figure 1b compares the intensity evolutions of the simulated TCs in ORIG and CTRL. In ORIG, the TC intensified and reached its mature stage after about 90-h simulation. In CTRL, the vortex experienced some quick adjustment and then reached a steady-stage evolution as in ORIG. Although the intensity evolutions in terms of the maximum 10-m height wind speed (Vmax) and the minimum sea level pressure (MSLP) differ in details in CTRL and ORIG, the difference can be considered relatively small. This indicates that
the axisymmetric vortex obtained from the 96-h spinup in ORIG reached its mature phase. Thus,
any significant change in intensity in the binary-TCs simulations can be considered as a result of
the binary interaction when two TCs vortices were simultaneously introduced.

147 *c. Experimental design*

To investigate the interaction of binary TCs, we conducted four experiments with different initial separation distances, which were 480 (D480), 600 (D600), 720 (D720), and 840 km (D840), respectively. In each experiment, the two initial TCs, which were the same as that in CTRL above, were placed in the east-west direction. The centroid of the binary TCs was located at the center of D01 and D02. For the convenience of discussion, we named the WTC for the TC initially located to the west and the ETC for the TC initially located to the east.

154 Some parameters in the following analysis/discussions are defined here. The TC surface 155 center was simply defined as the location of the MSLP. We will discuss the TC intensity change in 156 terms of the change in MSLP rather than Vmax (e.g., WH95; Falkovich et al. 1995; Khain et al. 157 2000; JC15b) because the MSLP of one TC can be detected even when binary TCs are undergoing 158 merging process. The eye region was roughly defined as the area from the TC surface center to a 159 radius of 60 km, which was the same as the initial RMW at the low levels in the binary-TCs 160 experiments. The inner core was referred to the area from the TC surface center to a radius of 180 161 km, which was about three time of the initial RMW at the low levels (Wang 2008).

162 **3. Results**

163 *a. An overview*

Figure 2 shows the track and intensity evolutions of the binary TCs, together with the change 164 of the separation distance between the centers of two TCs. For a comparison, the intensity evolution 165 of a single TC in CTRL is also shown in Fig. 2. Both TCs mutually rotated cyclonically in all 166 experiments. The two TCs merged as a new TC after 22 h and 67 h in D480 and D600, respectively. 167 168 In D720 and D840, the binary TCs did not merge with their separation distance increasing with 169 time. As the separation distances increased, the cyclonic rotation also slowed down and the two 170 TCs eventually departed from each other without significant rotation, such as the case in D840 (Fig. 2g). These results are roughly consistent with previous studies (WH95; JC15b) and the conceptual 171 172 model of binary-TCs interaction in LH93.

173 We divided the intensity evolution into three stages (right panels in Fig. 2) depending on their interaction modes. Stage 1 is the first 10 h of the simulations during which the binary TCs 174 175 experienced the weakening in all experiments. Stage 2 is from 10 h to 55 h of the simulations when 176 the intensity of the binary TCs showed little change or experienced a quasi-steady evolution in 177 D600, D720 and D840. In stage 3, the binary TCs weakened again after 55 h in D600 (55–67 h), 178 D720 (55 h to the end) and D840 (55–78 h), and prior to merging from 10 h to 22 h of the simulation 179 in D480. Although the binary TCs in D480 weakened during the first 22 h of the simulation, the 180 physical processes that led to the two weakening periods were different. Note that an intensification 181 of the merged system occurred in both D480 and D600, which was also found in WH95. It is interesting that the two TCs in D840 after stage 3 intensified again when the separation distance 182

between the two TCs became larger than 1600 km (Fig. 2h). Since the temporal evolutions of the
two TCs in the binary experiments are similar and almost symmetric with respect to their centroid
due to their identical initial conditions, we take the WTC to discuss the intensity and structure
changes in the following discussion.

Figure 3 shows the mean potential temperature anomaly in the eye region of the WTC in the 187 four binary experiments. The potential temperature anomaly was calculated as the perturbation 188 relative to the environment, which was the mean potential temperature from the TC surface center 189 to 600-km radius, the same as that in Fu et al. (2019). Following Zhang and Chen (2012), we also 190 calculated the central sea level pressure rises induced by the upper-level (between the 9- and 16-191 192 km heights, ΔP_{μ}), lower-level (between the 2- and 6-km heights, ΔP_{μ}) and total-level warm core (ΔP) using the hydrostatic equation with the results shown in Fig. 3. The bias of the central sea 193 194 level pressure integrated from the hydrostatic equation and the MSLP from the model simulations 195 was less than 5 hPa. The TC presented a warm-core structure at the initial time with two maximum 196 positive potential temperature anomalies centered at the 10- and 15-km heights, respectively, in all 197 four experiments. Influenced by the ETC, the upper-level warm core of the WTC weakened during 198 stages 1 and 3 in all binary experiments and in the meantime both ΔP and ΔP_{μ} rose. In D600, 199 D720 and D840 (Figs. 3b–d), the upper-level warm core weakened and the lower-level warm core 200 strengthened in stage 2, but the potential temperature change in both upper- and lower-levels were quite small. This can be proven by the increasing of ΔP_u and decreasing of ΔP_l , and both were 201 202 largely offset. As a result, ΔP did not change much in stage 2. The warm core strengthened again as the merged TC intensified in D480 and D600 (Figs. 3a,b). After stage 3 in D840 (Fig. 3d) the warm core re-strengthened with both ΔP and ΔP_u slowly decreased until the end of the simulation.

206 The above results demonstrate that the intensity change of the binary TCs is consistent with 207 the evolution of the warm-core strength. Therefore, the key to understand the intensity change is 208 to understand what caused the change in the warm-core strength under the binary interaction. 209 Previous studies have demonstrated that the weakening of the TC warm core and eyewall entropy 210 is related to the asymmetric structures in the inner-core region and associated ventilation (Simpson 211 and Riehl 1958; Gray 1968; Frank and Ritchie 2001; Tang and Emanuel 2010; Gu et al. 2015). 212 Figure 4 shows the evolution of the inner-core mean relative wavenumber-1 kinetic energy (RKE, 213 defined as the percentage of the wavenumber-1 kinetic energy in the total kinetic energy) of the WTC. The percentages of higher-wavenumbers were quite smaller than the RKE (not shown). In 214 215 all experiments, the RKE was the largest at the 16-km height and smallest below the 9-km height, 216 indicating that the upper-level (between the 9- and 16-km heights or equivalent 300-100 hPa) RKE 217 was dominant. In stage 1, the RKE increased rapidly above the 14-km height, which was consistent 218 with the weakening of the TC in all experiments. In D600, D720 and D840, the upper-level RKE 219 shrank in stage 2 from 10 h to about 30 h of the simulations. Then the upper-level RKE re-220 strengthened and expanded downward. The development of upper-level RKE was prior to the 221 increase of the MSLP, suggesting that the development of asymmetric structure in the upper 222 troposphere was most likely responsible for the weakening of the binary TCs. In stage 3, the upper-

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level RKE and the MSLP increased again in all experiments. After stage 3, the RKE of the whole
TC vortex decreased sharply after the two TCs merged and re-intensified in D480 and D600 (Figs.
4a,b). Similar features were found after stage 3 in D840 (Fig. 4d) probably because the two TCs
were far away from each other.

The dominance of wavenumber-1 asymmetry indicates that vertical wind shear (VWS) was 227 228 playing an essential role in the structure change (Jones 1995; Wang and Holland 1996; Frank and 229 Ritchie 2001; Corbosiero and Molinari 2003; Reasor et al. 2004; Chen et al. 2006; Xu and Wang 230 2013; Zhang et al. 2013; DeHart et al. 2014; Gu et al. 2016). Therefore, it is necessary to examine whether the intensity change of binary TCs is related to the asymmetric structure and the VWS. 231 232 The VWS over one TC must from the baroclinic circulation of the other TC in the binary system 233 (Fig. 1), since there was no large scale environmental VWS in the simulations. Figure. 5 shows the evolution of the upper-layer VWS (between 100 and 300 hPa) and the commonly used deep-layer 234 235 VWS (between 200 and 850 hPa) averaged radially from the surface center to 600-km radius, 236 together with the 3-h MSLP change of the WTC in the four experiments. In stage 1, the WTC 237 weakened with the positive 3-h MSLP change when the upper-layer VWS increased and kept a 238 large magnitude in all experiments while the deep-layer VWS presented a decreasing trend in D480 239 and D600. In stage 2, the 3-h MSLP change was small and even a little bit negative, meaning that 240 the WTC did not further weaken but experienced a quasi-steady intensity evolution. Meanwhile, 241 the upper-layer VWS decreased first and then increased again while the deep-layer VWS continued to increase and remained large. In stage 3, the 3-h MSLP change was mostly positive, and the 242

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243	upper-layer VWS increased and was larger than that in stage 2 except for D480 and D600 in which
244	the upper-layer VWS decreased during the merging with a decrease in the deep-layer VWS.
245	Nevertheless, in comparison with the deep-layer VWS, the evolution of the upper-layer VWS is
246	more consistent with the 3-h MSLP change. Namely, the large or increasing upper-layer VWS
247	corresponds to the large and positive 3-h MSLP change, and the small or decreasing upper-layer
248	VWS corresponds to the small or even negative 3-h MSLP change. The correlation coefficients
249	between the upper-layer VWS and the 3-h MSLP change varied from 0.6 to 0.7 at 99% confidence
250	level in all four experiments based on the Student's t-test. This strongly suggests that the upper-
251	layer VWS is a good indicator of the intensity change of the two interacting strong TCs. Note that
252	the more detrimental effect of the upper-layer VWS on the intensity of a single mature TC has been
253	also found in previous studies (e.g., Xu and Wang 2013; Fu et al. 2019).
254	The above results show a strong relationship between the upper-layer VWS and the intensity
255	change of the simulated binary TCs. We hypothesize that the upper-layer VWS of one TC came

change of the simulated binary TCs. We hypothesize that the upper-layer VWS of one TC came mainly from the upper-layer anticyclonic circulation of the other TC in the binary system. Previous studies also mentioned the potential role of the VWS originated from the baroclinic structure of one TC imposed on the other TC in the binary system (WH95; Khain et al. 2000; JC15b). However, the physical processes that lead to the structure and intensity change of binary TCs have not been

investigated to any extent and will be analyzed in detail in the following subsections.

261 *b. Stage 1: The early weakening of the binary TCs*

In stage 1, one TC of the binary system was subject to the imposed vertical shear of tangential

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wind from the other TC, leading to the initial ventilation of the warm core of each TC. To illustrate
the impact of the ETC on the WTC, we interpolated the fields into a new coordinate system for the
binary TCs with the origin following the surface center of the WTC as shown in Fig. 6. Thus, the
ETC was always to the east of the WTC and the cyclonic (anticyclonic) tangential wind of the ETC
across the WTC center was northerly (southerly) wind in this new coordinate system.

268 Figure 7 shows the potential temperature averaged from the 9- to 16-km heights over the WTC 269 in D720 together with the asymmetric wind vectors at the 9- and 16-km heights, respectively. Here, 270 the asymmetric wind of the WTC was calculated as the difference between the storm-relative flow 271 (total horizontal winds relative to the moving vortex) and the azimuthal mean wind as in Fu et al. 272 (2019). Also plotted in Fig. 7 are the vortex center at the 16-km height and the mean upper-layer 273 VWS between the 16- and 9-km heights (very close to the VWS between 100 and 300 hPa). The vortex centers at the 9- and 16-km heights were defined as the centroid of PV for each TC in the 274 275 innermost domain. Other three experiments (not shown) have similar features to D720 in stage 1.

As shown in Fig. 7, the asymmetric winds at the 16-km height ventilated the warm anomalies in the TC core, leading to the weakening of the upper-level warm core in stage 1. The mean asymmetric winds at the 16-km height were roughly perpendicular to the orientation between the surface centers of the binary TCs. Note that the upper-level anticyclone (ULA) of the ETC was the strongest at a height of about 16 km (Fig. 1a) and had southerly winds to the west of the ETC. This is consistent with the asymmetric winds across the inner core of the WTC at the 16-km height in the early stage of the simulations, indicating the important role of the ETC's ULA on the WTC. Moreover, the ULA of the ETC induced the upper-layer VWS over the WTC, which was also mentioned in previous studies (WH95; Khain et al. 2000; JC15b). The upper-level the WTC tilted toward the downshear-left side of the upper-layer VWS. As a result, the differential advection of the upper-level circulation of the WTC by the VWS further enhanced the asymmetric flow crossing the warm core of the WTC. Note that the upper-layer VWS between the 16- and 9-km heights was almost equal to the mean asymmetric wind at the 16-km height because the asymmetric winds at the 9-km height were quite weak (Figs. 4 and 7) during stage 1.

290 To further confirm the ventilation of the upper-level warm core by the asymmetric flow, we 291 performed the potential temperature budget as given below following Stern and Zhang (2013)

$$\Delta \theta = \left(\dot{\theta}_{ADV} + \dot{\theta}_{HEAT} + \dot{\theta}_{PBL} + \dot{\theta}_{DIF}\right) \Delta t, \tag{1}$$

where $\Delta \theta$ is the actual change in the potential temperature (θ) during the time period Δt ; $\dot{\theta}_{ADV}$ is the total tendency due to horizontal and vertical advections of θ ; $\dot{\theta}_{HEAT}$ is the tendency from diabatic heating; $\dot{\theta}_{PBL}$ is the tendency from the boundary layer parameterization scheme; and $\dot{\theta}_{DIF}$ is the tendency due to subgrid-scale horizontal diffusion. The model potential temperature tendencies are from the model output at every 6 min, and the budget was conducted from 6 to 9 h. The results are consistent across all simulations and thus we choose D720 as an example in the following discussion.

300 The patterns in 3-h actual θ change (Fig. 8a) and the results from the right-hand side (*RHS*) 301 of Eq. (1) (Fig. 8b) are very similar, implying that the budget is reliable. The residual term 302 (difference between 3-h θ change and *RHS* of Eq. 1, Fig. 8c) shows some errors mostly near the 303 TC center above the 15-km height, probably due to the interpolation and/or the tilting of the vortex 304 at the upper levels. However, these errors do not have impact on our interpretation. Among all four terms on the RHS of Eq. (1) (Figs. 8d–f), only the total advection term ($\dot{\theta}_{ADV}$) induced significant 305 cooling in the upper-layer eye region and the whole eyewall (Fig. 8d). The cooling in the eyewall 306 by total advection was largely offset by diabatic heating (Fig. 8e). The boundary layer process 307 $(\dot{\theta}_{PBL})$ and horizontal diffusion $(\dot{\theta}_{DLF})$ caused warming in the inflow layer and cooling at the top of 308 the boundary layer (mainly contributed by $\dot{\theta}_{PBL}$ term) but their tendencies were quite small 309 compared to $\dot{\theta}_{ADV}$ and $\dot{\theta}_{HEAT}$ (Fig. 8f). The total advection ($\dot{\theta}_{ADV}$) can be further decomposed 310 into the azimuthal mean radial advection $(\dot{\theta}_{RADVM} = -\bar{u}(\partial/\partial r)\bar{\theta})$, the eddy radial advection 311 $(\dot{\theta}_{RADVE} = -(\partial/\partial r)(\overline{u'\theta'}) - (\overline{u'\theta'}/r)$ and the total vertical advection $(\dot{\theta}_{VADV})$; where \bar{u} and u'312 are azimuthal mean and asymmetric radial wind, $\bar{\theta}$ and θ' are azimuthal mean and asymmetric 313 potential temperature, and r is the radius from the surface TC center. $\dot{\theta}_{RADVM}$ was much smaller 314 315 than other two terms (Fig. 8g) because the azimuthal mean radial wind could neither pass through the TC eye region nor ventilate the warm core. Only $\dot{\theta}_{RADVE}$ contributed negatively to the 316 317 tendency of the upper-level warm core (Fig. 8h) because the asymmetric flow at the 16-km height brought the cold air in and took the warm air out of the eye region (Fig. 7). $\dot{\theta}_{VADV}$ had an opposite 318 distribution to $\dot{\theta}_{RADVE}$, but its magnitude was smaller than that of $\dot{\theta}_{RADVE}$, giving rise a net 319 320 negative advection tendency in the upper-level eye region and the whole eyewall. Therefore, based 321 on the potential temperature budget, we can conclude that the eddy radial advection of potential temperature ($\dot{\theta}_{RADVE}$) due to the upper-level asymmetries (Figs. 4 and 7) is the major process that 322

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323 caused the weakening of the upper-level warm core and thus the intensity of binary TCs in stage 1.
324 The asymmetries of one TC resulted from the upper-layer VWS (Fig. 5), which in turn was
325 originated from the baroclinic circulation of the other TC in the binary system (Fig. 7).

326 c. Stage 2: The quasi-steady intensity evolution of the binary TCs

During 10 to 55 h of the simulations, the binary TCs in D600, D720, and D840 experienced a 327 328 quasi-steady intensity evolution. We still take D720 as an example since the results are similar for 329 D600 and D840. The upper-level warm core of the WTC changed very slowly during this period (Figs. 3c and 9). The asymmetric flow at the 9-km height strengthened during this period, which 330 can also be found in Fig. 4c. The VWS between the 16- and 9-km heights decreased first and then 331 332 increased, with the shear direction changing with time from southwesterly to northerly. As a result, 333 the vortex centers at the 16- and 9-km heights gradually aligned and then departed again. This implies that the vortex tilting did not continue to increase in stage 2. The relatively weak upper-334 335 layer VWS could still lead to the slow weakening of the upper-level warm core and the intensity 336 of the TCs (Figs. 3c and 9), but its effect was largely counteracted by the faintly strengthening of 337 the lower-level warm core. Potential temperature budget (not shown) indicates that the strengthening of the lower-level warm core was contributed by $\dot{\theta}_{VADV}$, which was caused by the 338 339 relatively weak downward motion in the eye region. This downdraft was a consequence of the 340 reconstructed secondary circulation under the weakening of upper-level VWS. Therefore, the 341 intensity of binary TCs showed a quasi-steady intensity evolution in stage 2.

342 Changes in the upper-layer VWS over the WTC in stage 2 can be largely inferred from the

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evolution of asymmetric flow at the height of 9 km because the asymmetric flow over the WTC at 343 the 16-km height did not change much. At the beginning of stage 2 (Fig. 9a), the mean asymmetric 344 345 wind across the center of the WTC was weaker than that at the 16-km height and hence the upperlayer VWS was southwesterly. However, the asymmetric flow over the WTC at the 9-km height 346 strengthened and became southerly (Figs. 9b-e), which corresponded to the ULA of the ETC. This 347 led to a decrease in the difference of the mean winds between the 16- and 9-km heights over the 348 349 WTC, which means that the upper-layer VWS over the WTC decreased because the asymmetric flow at the 9-km height strengthened. As the asymmetric wind at the 9-km height continued 350 strengthening as the ULA of the ETC expanded downward (see discussion below) and became 351 352 stronger than that at the 16-km height, the upper-layer VWS over the WTC changed to northerly 353 with the shear magnitude increasing again (Figs. 9f-i).

Since the upper-layer VWS over the WTC results from the ULA of the ETC in the binary 354 355 system, it is necessary to examine how the ULA of the ETC evolved to lead to the variation of the 356 upper-layer VWS over the WTC in stage 2. Figure 10 shows the radius-height cross sections of the 357 azimuthal mean tangential and radial winds of the ETC on the near and opposite sides to the WTC 358 center. The near side of the ETC was defined as the quadrant close to the WTC and the opposite 359 side was the rest part of the ETC away from the WTC, as shown in light and dark gray zones in 360 Fig. 6, respectively. The interaction of binary TCs should have much stronger impact on the near 361 side, but relatively weaker impact on the opposite side of each TC. In stage 2, the opposite-side ULA of the ETC strengthened and expanded outward in D600, D720 and D840, similar to that for 362

a single TC simulated in CTRL (not shown), but weaker because the TC in the binary system 363 weakened due to binary interaction. The azimuthal mean anticyclonic tangential wind on the 364 opposite side of the ETC at the 9-km height also increased but was still weaker than that at the 16-365 km height, which is different from the asymmetric flow at the 9- and 16-km heights over the WTC. 366 367 This implies that the tangential wind of the ETC could not fully explain changes in the upper-layer 368 VWS over the WTC. Therefore, the binary interaction must play some role in changing the upper-369 layer VWS over the WTC. The azimuthal mean tangential wind on the near side of the ETC was 370 quite different from that on the opposite side. On the near side, the ULA of the ETC expanded downward and the azimuthal mean anticyclonic tangential wind at the 9-km height became stronger 371 372 over the WTC surface center in D600, D720 and D840 (Figs. 10a,d,g), leading to a decrease in the 373 upper-layer vertical shear of the azimuthal mean tangential wind of the ETC between the 16- and 9-km heights over the WTC. As the azimuthal mean anticyclonic tangential wind of the ETC at the 374 375 9-km height continued to strengthen and became stronger than that at the 16-km height (Figs. 376 10e,f,h,i), the upper-layer vertical shear of the azimuthal mean tangential wind of the ETC over the 377 WTC turned to the opposite direction and increased again in D720 and D840. This is consistent 378 with changes in the asymmetric flows at the 9- and 16-km heights (Fig. 9) and the upper-layer 379 VWS over the WTC (Figs. 5c,d) in D720 and D840. Different from that in D720 and D840, as the 380 two TCs in D600 approached each other, the WTC entered the area of the upper-level outflow of 381 the ETC by the end of stage 2 (Fig. 10c). The outflow of the ETC at the 16-km height was stronger 382 than that at the 9-km height over the WTC, resulting in a re-strengthening of the upper-layer VWS

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383 over the WTC in D600.

384 Note that at the beginning of the simulations, the difference in the azimuthal mean tangential wind of the ETC between the near and opposite sides is primarily due to the superposition of winds 385 of the two TCs, that is, the near-side ULA of the ETC was strengthened by the superposition of the 386 387 cyclonic circulation on the near side of the WTC. However, this cannot explain why the ULA expanded downward. We hypothesize that the weakening of the secondary circulation in each TC, 388 389 which caused downdraft anomaly in the near side of each TC and induced the downward advection 390 of the ULA. Figure 11 shows the distributions of the vertical motion vertically averaged between the 16- and 9-km heights over the WTC in D600, D720, and D840 at 20-h interval from 10 h to 50 391 392 h of the simulations. In stage 2, the updraft on the near side in the WTC eyewall became weaker 393 than that on the opposite side. Downward motion anomalies occurred on the near side of the WTC, especially in the southeast quadrant because of the confluence of the upper-level outflows of the 394 395 WTC and the ETC. This resulted in the weakening of the secondary circulation of both TCs, and 396 thereby the weakening of updraft on the near side of the WTC. The downward motion anomaly 397 favored the downward penetration of the ULA (and southerly) of the ETC from the top down. This 398 thus led to changes in the upper-layer VWS over the WTC as mentioned above.

The above process can be confirmed by the meridional wind (*V*) budget in the binarycoordinate system as defined earlier. The budget equation can be given as:

401
$$\Delta V = \left(\dot{V}_{HADV} + \dot{V}_{VADV} + \dot{V}_{PRES} + \dot{V}_{CORI} + \dot{V}_{PBL} + \dot{V}_{DIF}\right)\Delta t, \qquad (2)$$

402 where ΔV is the actual change in V over a given period Δt ; \dot{V}_{HADV} and \dot{V}_{VADV} are the

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tendencies due to horizontal and vertical advections, respectively; \dot{V}_{PRES} and \dot{V}_{CORI} are the 403 tendencies due to pressure gradient and Coriolis forces, respectively; \dot{V}_{PBL} is the tendency from 404 the boundary layer parameterization scheme; and \dot{V}_{DIF} is the tendency due to subgrid-scale 405 horizontal diffusion. All terms of the RHS of Eq. (2) are based on the model output at every 6 min 406 407 as in the potential temperature budget. Figure 12 shows the V budget of the WTC at the 9- and 408 16-km heights in D600, D720 and D840 in stage 2 (42–48 h). The difference between the model 409 V change and the sum on the RHS of Eq. (2) integrated from 42- to 48-h simulations was quite small. At the 9-km height, all three experiments show the increasing in V (southerly or 410 anticyclonic tangential wind relative to the ETC). \dot{V}_{VADV} was positive during the budget period 411 412 and was the primary cause for the increase in V (namely southerly strengthened). Other terms on 413 the RHS of Eq. (2) contributed little or even negative tendency to the southerly wind. At the 16km height, V changed little in D720 (Fig. 12d) and decreased in both D600 and D840 (Figs. 12b,f). 414 The tendencies contributed by \dot{V}_{PRES} and \dot{V}_{HADV} were largely offset in both D720 and D840. 415 416 Therefore, the momentum budget of meridional wind demonstrates that the enhancement of 417 asymmetric southerly at the 9-km height over the WTC mainly resulted from the downward 418 advection of the near-side ULA of the ETC in stage 2. Namely, the binary interaction weakened 419 the near-side vertical secondary circulation of each TC in stage 2, causing the downward expansion 420 of the near-side ULA. As a result, the upper-layer VWS over each TC weakened first and then re-421 strengthened, leading to marginally changes in the upper-level warm core and the intensity of the binary TCs. 422

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423 *d. Stage 3a: The second weakening of the non-merging binary TCs*

The TCs in the two non-merging binary experiments (D720 and D840) experienced the second 424 425 weakening (stage 3). This stage can be considered as a continuation of stage 2 because the upperlayer VWS continued strengthening and remained large by the end of stage 2 (Figs. 5c,d). The 426 427 binary TCs in both D720 and D840 experienced a weakening in stage 3 as in stage 1. The large upper-layer VWS led to the strengthening of the RKE above the 9-km height (Figs. 4c,d). The 428 potential temperature budget shown in Fig. 13 indicates that $\dot{\theta}_{RADVE}$ weakened the warm core at 429 the 15- and 9-km heights of the WTC. Compared with stage 1, the weakening of the warm core at 430 the 9-km height caused by $\dot{\theta}_{RADVE}$ in stage 3 further confirms that the binary interaction resulted 431 432 in downward expansion of the near-side ULA as discussed for stage 2 in section 3c.

After stage 3 in D840, the upper-layer VWS decreased and the binary TCs deepened (Fig. 5d) 433 until the end of the simulation when the separation distance between the two TCs increased over 434 435 1600 km (Fig. 2h). We also examined additional experiments with the same initial vortices but 436 different initial separation distances and found that the overall behavior of the binary TCs are quite 437 similar (not shown) with the weakening terminated once their separation distance exceeding about 438 1600 km. This seems to be a critical separation distance in our experiments and is consistent with 439 some relevant statistical analyses of binary-TCs interaction based on observations (Brand 1970; Dong and Neumann 1983; Wu et al. 2011; Jang and Chun 2015a; Ren et al. 2020). Since the ULA 440 441 of one TC affects the intensity of the other TC in the binary system, we further introduce the local 442 Rossby radius of deformation L_R (= NH/I, where N is the Brunt-Väisälä frequency; H is the

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scale height; and I is the inertial stability) of the azimuthal mean ULA for understanding the 443 dynamics. *NH* is 60 m s⁻¹ the same as that in Bell et al. (2012), and $I = \sqrt{(f+\zeta)(f+\frac{2\overline{\nu}}{r})}$, 444 where ζ is the relative vorticity and \bar{v} is the azimuthal mean tangential wind) is calculated from 445 the model output. We did not use the near-side azimuthal mean ULA because once the two TCs 446 were far enough away from each other, the difference of the azimuthal mean ULA on the near and 447 opposite sides was negligible. We can estimate L_R to be 1500–1700 km, comparable to 1600 km in 448 our experiments. Note that L_R is much smaller in the middle–lower troposphere than in the outflow 449 layer because of the much larger inertial stability. Therefore, it is expected that once the separation 450 distance between the two TCs becomes larger than the horizontal scale L_R determined by the ULA, 451 452 the binary interaction and the associated intensity change would become very weak and can be ignored. 453

454 *e. Stage 3b: The weakening of the binary TCs during merging*

From 10 h to 22 h of the simulation in D480 and from 55 h to 67 h of the simulation in D600, 455 456 the binary TCs experienced a weakening period prior to their merger. During this stage, the two TCs presented increasingly asymmetric structure as they approached each other with their 457 458 separation distance decreasing rapidly, consistent with the weakening of the two TCs. Since the 459 structure and intensity evolutions are similar in D480 and D600, we take D480 as an example to 460 describe the merging process. Figure 14 shows the simulated maximum radar reflectivity in D480 prior to merging. The binary TCs showed an "8" shaped rainband structure. The eyewall on the 461 near side of each TC was weaker than that on the opposite side and gradually weakened but 462

suddenly disappeared before merging. The partial eyewalls of the two TCs finally formed a new 463 closed eyewall of the merged TC system. Figure 15 shows the PV distributions in D480 at four 464 different heights. In the boundary layer (at the 1-km height) in D480 (Fig. 15a), the two vortices 465 presented weak deformation at 18 h of the simulation but then accelerated the rotation with more 466 and more deformation and filamentation until they merged (Figs. 15b-c). The similar deformation 467 468 and filamentation also occurred in the lower- (at the 2-km height, Figs. 15d-f) and middletroposphere (at the 5-km height, Figs. 15g-i), but both were weaker and the merging of the two 469 vortices lagged that in the boundary layer. Going to higher levels, the PV structure (Figs.15j-l) was 470 more asymmetric as the circulation in the upper troposphere (at the 9-km height) was much weaker. 471 472 The two vortices at the upper level rotated more slowly than that at the lower- and middle-levels, 473 implying a large vertical tilt of the TC vortices. Different from those in the middle-lower troposphere, the PV field at the 9-km height shows no merging but strong deformation and 474 475 filamentation, leading to banded structure as the low-level vortices merged. The results thus 476 demonstrate a bottom-up merging process of the binary TCs in the simulations, which is consistent 477 with the findings in WH95.

Figure 16 shows the vertical cross sections of the total wind speed through the surface vortex centers of the two TCs in D480. The eyewalls as inferred by large wind speed on the near side of the binary TCs weakened from the top down partly due to the vertical tilt of the TC vortices. Meanwhile, both TC vortices became more asymmetric. This highly asymmetric TC structure resulted primarily from the strong shearing deformation of the TC vortices, a process well studied

with both barotropic and baroclinic models in the literature (Holland and Dietachmayer 1993; 483 WH95; Falkovich et al. 1995; Khain et al. 2000; Prieto et al. 2003; Shin et al. 2006). After the two 484 TCs merged, the new eye was larger than the eye of either TC prior to merging. The merger 485 occurred very rapidly and the new TC became more and more axisymmetric and also experienced 486 487 intensification after merger. These are consistent with those documented in previous studies (WH95; Khain et al. 2000) and can also be seen from Figs. 2a-d. Therefore, the weakening and 488 489 structure change of the binary TCs prior to merging, including the highly asymmetric rainbands, the near-side eyewall weakening and breakdown from the top down, and the large tilt, were due to 490 the combined effect of large VWS and strong horizontal shearing deformation of the drastic binary 491 492 interaction when the two TCs approached rapidly toward merging.

493 4. Conclusions and Discussion

In this study, the intensity change of binary TCs has been investigated using a three-494 495 dimensional numerical model with a finest grid spacing of 3 km under idealized conditions on an 496 *f*-plane with a constant sea surface temperature and in a quiescent environment. To allow more 497 realistic binary interaction, we first simulated a single TC for 96 h until it reached its mature stage 498 with the fully-developed secondary circulation and used its axisymmetric vortex as the initial TCs 499 in the binary experiments. Four experiments were performed with the initial separation distances 500 between the two identical TCs being 480 (D480), 600 (D600), 720 (D720), and 840 km (D840), 501 respectively. Results show that the two TCs approached each other and merged only in D480 and D600. In D720, the two TCs rotated cyclonically but with their separation distance increasing with 502

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time. In D840, the two TCs rotated cyclonically in the early stage but then anticyclonically and moved away (escaped) from each other. These three interaction modes are very similar to the conceptual model of binary TC interaction proposed by LH93.

506 The intensity of the binary TCs experienced three stages and the intensity change was well 507 correlated with the VWS in the upper troposphere between 100 and 300 hPa over the inner core of 508 each TC. The first stage was the weakening of the binary TCs during the first 10 h of the simulations. 509 In this stage, the vertical shear of the tangential wind from one TC imposed a large upper-layer 510 VWS on the other TC, leading to the ventilation and weakening of the warm core through both 511 horizontal advection and eddy flux of the potential temperature. Such a mutual interaction led to 512 the weakening of the two TCs. The second stage was the quasi-steady intensity evolution in the 513 three binary experiments (D600, D720 and D840) from 10 h to 55 h, when the two TCs did not yet or never merge. During this stage, the upper-layer VWS decreased first due to the enhanced 514 515 asymmetric flow at the 9-km height. The increasing asymmetric flow resulted mainly from the 516 outward and downward expansion of the ULA due to the superposition of the two TCs' circulations 517 and the binary interaction. As a result, the vertical tilt of the TC vortex largely decreased, the warm 518 core remained its strength, and the TCs experienced little intensity change. In the merging cases of 519 D480 and D600, the two TCs continued weakening until the two TCs merged. The weakening was 520 mainly due to both the VWS and shearing deformation of the cyclonic circulation as previously 521 studied. After merging in D480 and D600, the new TC system experienced intensification due to the continuous axisymmetrization. The non-merging binary TCs in D720 and D840 weakened 522

again after the quasi-steady intensity evolution as the asymmetric flow at the 9-km height induced 523 by the ULA of the opposite TC continued increasing. This led to the increase in the upper-layer 524 525 VWS over each TC and thus the weakening of the warm core and the TCs. The intensity of the binary TCs in D840 did not decrease further after 78 h of the simulation because the interaction of 526 the binary TCs became very weak after their separation distance increased to 1600 km, which is 527 528 comparable and even larger than the local Rossby radius of deformation (L_R) of the upper-level 529 anticyclonic circulation of the TCs. Therefore, L_R determines the horizontal scale of the ULA and can be used as a measure to determine whether the two TCs could experience direct binary 530 interaction. 531

532 Note that the intensity change of binary TCs is investigated under idealized conditions in this study. It is unclear whether the importance of upper-layer VWS in the binary interaction is a model 533 result or also true in real binary TCs. The initial vortex in our experiments was as intense as 895 534 hPa in its MSLP (about 70 m s⁻¹ in the maximum near-surface wind speed), which seems to be 535 536 "unrealistically strong" in the real atmosphere. We used such a strong TC because it is in its mature 537 stage of a simulated TC with well-developed primary and secondary circulations. This can ensure 538 a strong binary interaction and overcome the initial model spinup of a weak TC and also the intensity change of the binary TCs can be attributed to the binary interaction because the single TC 539 540 would experience a quasi-steady intensity evolution. Note that we also conducted a series experiments of relatively weak binary TCs (initial maximum near-surface wind speed of 35 m s⁻¹, 541 not shown), the two TCs showed similar intensity evolutions as those shown in this study. In 542

addition, the detailed merging processes have not been analyzed in this study as they seem to be 543 similar to what revealed in previous studies (e.g., WH95; Khain et al. 2000; JC15b). Previous 544 studies (Yang et al. 2008; Jang and Chun 2013; Liu and Tan 2016) also suggested that the structure 545 and intensity changes of binary TCs could be sensitive to the initial TC structure and intensity in 546 real atmosphere. Therefore, how sensitive the binary TC interaction is to the structure of the TCs 547 and the relative intensity and size of the two TC vortices needs to be addressed in future studies. 548 549 In addition, the binary interaction is often affected by the environmental flow and latitudinal dependence of the Coriolis parameter (e.g., WH95; Khain et al. 2000; JC15b). In those cases, the 550 initial orientation and relative intensity of the two TCs may become also important (WH95). In 551 552 addition, it is also worth noting that the role of the L_R of the ULA in distinguishing the direct binary 553 interactions is found in fully-physics moist simulations, in case of binary interaction of dry TC-like vortices the ULA may be very weak or even not exist at all. It is unclear what scaling parameters 554 555 can be used to distinguish the direct interaction for dry vortices. These will be examined in our 556 future studies.

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715 **Figure Captions**

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720

Figure 1. (a) Radial-height distribution of the azimuthal mean radial (m s⁻¹, interval of 5 m s⁻¹, 716 shading) and tangential (m s⁻¹, contours) winds of the TC at the initial time in CTRL (after a

96-h spinup of the model TC vortex). Positive values (solid) with contour intervals of 5 m s⁻¹ 718

are for cyclonic circulation and negative values (dashed) with contour intervals of 2 m s⁻¹ are 719

for anticyclonic circulation. (b) The temporal evolutions of the Vmax (m s⁻¹) at the 10-m height

and the MSLP (hPa) in ORIG (gray) and CTRL (black). The ORIG simulation started from -721

722 96 h and the CTRL simulation started from 0 h (see more details in the text).

723 Figure 2. The left panels show tracks of binary TCs in (a) D480, (c) D600, (e) D720, and (g) D840, 724 respectively. The blue curves are for the WTC and the red curves are for the ETC. The right

725 panels show the intensity evolutions of the WTC (blue) and the ETC (red) in (b) D480, (d)

726 D600, (f) D720, and (h) D840, together with the intensity evolution of the TC in CTRL (black).

727 The gray curves in (b) and (d) represent the intensity of the merged TC. The green curves denote 728 the separation distance between the two TCs. The dashed vertical lines separate the three stages 729 of the intensity evolution discussed in section 3.

730 Figure 3. Time-height cross sections of the potential temperature perturbation (K, shading) 731 averaged within the eye region ($r \le 60 \text{ km}$) of the WTC in (a) D480, (b) D600, (c) D720, and 732 (d) D840, along with the time evolution of the central sea level pressure changes (solid line) 733 and stage separation lines (dashed vertical lines). The central sea level pressure changes are relative to the initial time and caused by the total-level (ΔP , black line), upper-level (ΔP_{μ} , red 734 735 line), and lower-level (ΔP_1 , blue line), respectively.

- **Figure 4.** Time-height cross sections of the RKE (%, shading) averaged within the inner core ($r \leq$ 736 737 180 km), together with the evolution of the MSLP (solid line) and stage separation lines 738 (dashed vertical lines).
- 739 Figure 5. Time evolution of VWS between 200 and 850 hPa (black dashed line) and that between 740 100 and 300 hPa (black solid line) over the WTC and the 3-h MSLP change (gray curves with red and blue dots) in (a) D480, (b) D600, (c) D720, and (d) D840. The red and blue dots signify 741

intensification (negative 3-h MSLP change) and weakening (positive 3-h MSLP change),respectively.

Figure 6. Schematic diagram of the horizontal coordinate system in the analysis for binary TCs.
The origin is located at the surface center of the WTC. The x-axis is from the WTC to the ETC.
The y-axis is perpendicularly toward the left of the direction from the WTC to the ETC. The
near side (light gray zone) is the nearest quadrant of the two TCs and the opposite side (dark
gray zone) is the remaining part. We define the zonal wind being along the x-direction and
meridional wind being along the y-direction.

750 Figure 7. Potential temperature (K, shading) of the WTC vertically averaged between the 9- and 751 16-km heights at (a) 4 and (b) 8 h of the simulation in D720. The center of each panel is the 752 vortex center at the 9-km height. The red and blue arrows represent the asymmetric flow at the 16- and 9-km heights, respectively. The black hollow circle denotes vortex center at the 16-km 753 754 height. The black arrow in the lower left corner of each panel is the VWS (twice longer) 755 between the 16- and 9-km heights averaged within a radius of 600 km from the surface center. 756 Figure 8. Radial-height distribution of potential temperature budget terms (K, shading). Upper row: 757 Azimuthal mean of (a) the actual 3-h potential temperature change, (b) the sum of the RHS of 758 Eq. (1), and (c) budget errors. Middle row: Azimuthal mean potential temperature tendencies 759 due to (d) total advection $(\dot{\theta}_{ADV})$, (e) diabatic heating $(\dot{\theta}_{HEAT})$, and (f) the sum of the boundary layer process and horizontal diffusion $(\dot{\theta}_{PBL} + \dot{\theta}_{DIF})$. Lower row: Azimuthal mean tendencies 760 due to (g) the azimuthal mean radial advection ($\dot{\theta}_{RADVM}$), (h) eddy radial advection ($\dot{\theta}_{RADVE}$), 761 and (i) total vertical advection ($\dot{\theta}_{VADV}$). All terms are budgeted for the WTC and integrated for 762 3-h period from 6 to 9 h of the simulation in D720. 763

Figure 9. Same as Fig. 7, but from 10 to 50 h of the simulation at 5-h interval.

Figure 10. Same as Fig. 1a, but for the ETC from 10 to 50 h of the simulations at 20-h interval in
(a-c) D600, (d-f) D720, and (g-i) D840. The left half in each panel is the azimuthal mean on
the near side and the right half is that on the opposite side. The green line denotes the location
of the WTC surface center. The result is from the outermost domain as the ULA covers a large

769 area.

- Figure 11. Vertical motion (m s⁻¹) distribution relative to the surface center of the WTC vertically
 averaged between the 9- and 16-km heights from 10 to 50 h of the simulations at 20-h interval
 in (a-c) D600, (d-f) D720, and (g-i) D840.
- Figure 12. Time evolutions of the actual inner-core mean meridional wind (V) change (MODE,
- 774dashed gray line) relative to 42 h of the simulation of the WTC, the sum of the azimuthal775mean RHS of Eq. (2) (black solid line), \dot{V}_{HADV} (blue solid line), \dot{V}_{VADV} (red solid line),776 \dot{V}_{PRES} (yellow solid line), \dot{V}_{CORI} (pink solid line), \dot{V}_{PBL} (purple solid line), and \dot{V}_{DIF} (green
- solid line) in Eq. (2) in (a, b) D600, (c, d) D720, and (e, f) D840 at the 9- (left) and 16-km (right)
- heights. See text for detail.
- Figure 13. Same as Fig. 8, but all tendencies are integrated from 66 to 69 h of the simulation inD720.
- Figure 14. Horizontal distributions of simulated maximum radar reflectivity (dBZ) every hour
 from 19 to 22 h in D480.
- 783 Figure 15. Horizontal distributions of PV (PVU) at the (a-c) 1-, (d-f) 2-, (g-i) 5-, and (j-l) 9-km
- heights in D480. The left, middle, and right columns are at 18, 20, and 22 h of the simulation,respectively.
- **Figure 16.** Vertical cross sections of total wind speed (m s⁻¹) along the x-axis from the WTC (left)
- to the ETC (right) from 12 to 22 h of the simulation at 2-h interval in D480.



Figure 1. (a) Radial-height distribution of the azimuthal mean radial (m s⁻¹, interval of 5 m s⁻¹, shading) and tangential (m s⁻¹, contours) winds of the TC at the initial time in CTRL (after a 96-h spinup of the model TC vortex). Positive values (solid) with contour intervals of 5 m s⁻¹ are for cyclonic circulation and negative values (dashed) with contour intervals of 2 m s⁻¹ are for anticyclonic circulation. (b) The temporal evolutions of the Vmax (m s⁻¹) at the 10-m height and the MSLP (hPa) in ORIG (gray) and CTRL (black). The ORIG simulation started from – 96 h and the CTRL simulation started from 0 h (see more details in the text).





Figure 2. The left panels show tracks of the binary TCs in (a) D480, (c) D600, (e) D720, and (g)
D840, respectively. The blue curves are for the WTC and the red curves are for the ETC. The
right panels show the intensity evolutions of the WTC (blue) and the ETC (red) in (b) D480,
(d) D600, (f) D720, and (h) D840, together with the intensity evolution of the TC in CTRL
(black). The gray curves in (b) and (d) represent the intensity of the merged TC. The green
curves denote the separation distance between the two TCs. The dashed vertical lines separate
the three stages of the intensity evolution discussed in section 3.



Figure 3. Time-height cross sections of the potential temperature perturbation (K, shading) averaged within the eye region ($r \le 60 \text{ km}$) of the WTC in (a) D480, (b) D600, (c) D720, and (d) D840, along with the time evolution of the central sea level pressure changes (solid line) and stage separation lines (dashed vertical lines). The central sea level pressure changes are relative to the initial time and caused by the total-level (ΔP , black line), upper-level (ΔP_u , red line), and lower-level (ΔP_l , blue line), respectively.

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813 Figure 4. Time-height cross sections of the RKE (%, shading) averaged within the inner core ($r \le 180 \ km$), together with the evolution of the MSLP (solid line) and stage separation lines 815 (dashed vertical lines).

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Figure 5. Time evolution of VWS between 200 and 850 hPa (black dashed line) and that between
100 and 300 hPa (black solid line) over the WTC and the 3-h MSLP change (gray curves with
red and blue dots) in (a) D480, (b) D600, (c) D720, and (d) D840. The red and blue dots signify
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meridional wind being along the y-direction.



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Figure 7. Potential temperature (K, shading) of the WTC vertically averaged between the 9- and
16-km heights at (a) 4 and (b) 8 h of the simulation in D720. The center of each panel is the
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16- and 9-km heights, respectively. The black hollow circle denotes vortex center at the 16km height. The black arrow in the lower left corner of each panel is the VWS (twice longer)
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838 Figure 8. Radial-height distribution of potential temperature budget terms (K, shading). Upper row: Azimuthal mean of (a) the actual 3-h potential temperature change, (b) the sum of the RHS of 839 Eq. (1), and (c) budget errors. Middle row: Azimuthal mean potential temperature tendencies 840 due to (d) total advection $(\dot{\theta}_{ADV})$, (e) diabatic heating $(\dot{\theta}_{HEAT})$, and (f) the sum of the boundary 841 layer process and horizontal diffusion $(\dot{\theta}_{PBL} + \dot{\theta}_{DIF})$. Lower row: Azimuthal mean tendencies 842 due to (g) the azimuthal mean radial advection ($\dot{\theta}_{RADVM}$), (h) eddy radial advection ($\dot{\theta}_{RADVE}$), 843 and (i) total vertical advection ($\dot{\theta}_{VADV}$). All terms are budgeted for the WTC and integrated for 844 845 3-h period from 6 to 9 h of the simulation in D720.



Figure 9. Same as Fig. 7, but from 10 to 50 h of the simulation at 5-h interval.

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Figure 10. Same as Fig. 1a, but for the ETC from 10 to 50 h of the simulations at 20-h interval in
(a-c) D600, (d-f) D720, and (g-i) D840. The left half in each panel is the azimuthal mean on
the near side and the right half is that on the opposite side. The green line denotes the location
of the WTC surface center. The result is from the outermost domain as the ULA covers a large
area.

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Figure 11. Vertical motion (m s⁻¹) distribution relative to the surface center of the WTC vertically
averaged between the 9- and 16-km heights from 10 to 50 h of the simulations at 20-h interval
in (a-c) D600, (d-f) D720, and (g-i) D840.



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Figure 12. Time evolutions of the actual inner-core mean meridional wind (V) change (MODE, dashed gray line) relative to 42 h of the simulation of the WTC, the sum of the azimuthal mean *RHS* of Eq. (2) (black solid line), \dot{V}_{HADV} (blue solid line), \dot{V}_{VADV} (red solid line), \dot{V}_{PRES} (yellow solid line), \dot{V}_{CORI} (pink solid line), \dot{V}_{PBL} (purple solid line), and \dot{V}_{DIF} (green solid line) in Eq. (2) in (a, b) D600, (c, d) D720, and (e, f) D840 at the 9- (left) and 16-km (right) heights. See text for details.





Figure 14. Horizontal distributions of simulated maximum radar reflectivity (dBZ) every hour
from 19 to 22 h in D480.

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Figure 15. Horizontal distributions of PV (PVU) at the (a-c) 1-, (d-f) 2-, (g-i) 5-, and (j-l) 9-km
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