

## Water vapour self-continuum in nearvisible IR absorption bands: measurements and semiempirical model of water dimer absorption

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Simonova, A. A., Ptashnik, I. V., Elsey, J., McPheat, R. A., Shine, K. P. ORCID: https://orcid.org/0000-0003-2672-9978 and Smith, K. M. (2022) Water vapour self-continuum in nearvisible IR absorption bands: measurements and semiempirical model of water dimer absorption. Journal of Quantitative Spectroscopy and Radiative Transfer, 277. 107957. ISSN 00224073 doi: 10.1016/j.jqsrt.2021.107957 Available at https://centaur.reading.ac.uk/101004/

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Publisher: Elsevier

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1 2	Water vapour self-continuum in near-visible IR absorption bands: Measurements and semiempirical model of water dimer absorption
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12	Corresponding author: Igor V. Ptashnik (piv@iao.ru)
13 14	Abstract
15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33	The nature of the water vapour continuum has been of great scientific interest for more than 60 years. Here, water vapour self-continuum absorption spectra are retrieved at temperatures of 398 K and 431 K and at vapour pressures from 1000 to 4155 mbar in the 8800 and 10600 cm <sup>-1</sup> absorption bands using high-resolution FTS measurements. For the observed conditions, the MT_CKD-3.2 model underestimates the observed continuum on average by $1.5-2$ times. We use the hypothesis that water dimers contribute to the continuum absorption to simulate the experimentally-retrieved self-continuum absorption spectra, and to explain their characteristic temperature dependence and spectral behaviour. The values of the effective equilibrium constant are derived for the observed temperatures. We find that the dimer-based model fits well to the measured self-continuum from this and previous studies, but requires a higher effective equilibrium constant compared to the modern estimates within the temperature range (268-431 K) and spectral region studied. It is shown that water dimers are likely responsible for up to 50% of the observed continuum within these bands. Possible causes of the incomplete explanation of the continuum are discussed. Extrapolating these measurements to atmospheric temperatures using the dimer-based model, we find that the newly-derived self-continuum reduces calculated surface irradiances by 0.016 W m <sup>-2</sup> more than the MT_CKD-3.2 self-continuum in the 8800 cm <sup>-1</sup> band for overhead-Sun mid-latitude summer conditions, corresponding to a 12.5% enhancement of the self-continuum radiative effect. The change integrated across the 10600 cm <sup>-1</sup> band is about 1%, but with significant differences spectrally.
34 35 36	<b>Keywords:</b> continuum absorption, water vapor, absorption band, water dimer, line wings, semiempirical model

37 1. Introduction

As one of the main gaseous absorbers of solar radiation, water vapour plays an important role 38 in radiative processes occurring in the Earth's atmosphere. Positive feedback between water vapour 39 concentration and temperature of the Earth's surface significantly affects the weather and climate of 40 the Earth. Part of the water vapour absorption, the so-called water vapour continuum, has been a 41 special subject of study since it was first measured in the mid-infrared atmospheric window (8-14 42 µm) in 1918 [1]. Whilst we have a good understanding of the mechanisms responsible for water 43 vapour absorption lines, the physics underlying the water vapour continuum is not yet as clear. The 44

intensity of the latter is characterized by a slowly varying spectral dependence that makes a small 45 contribution to the total absorption of solar radiation by water vapour in the Earth's atmosphere (up 46 to 3% in the global average) [2]. The spectrum of water vapour continuum absorption can be divided 47 into so-called *self* and *foreign* components. The former is a result of interactions between water 48 molecules, while the latter is caused by the interaction of water molecules with other gases, most 49 50 notably nitrogen and oxygen in the Earth's atmosphere. This paper focuses on improved understanding of the water vapour *self-continuum*. Despite the much stronger intensity of water 51 absorption lines compared to the underlying continuum, there are particular features of the latter that 52 allow it to be spectrally discerned. A strong negative exponential temperature dependence and 53 quadratic pressure dependence of the water vapour self-continuum absorption are among such 54 features. 55

From an atmospheric radiative transfer perspective, the most relevant contributions of the selfcontinuum absorption to the water vapour absorption spectrum are located predominantly in the atmospheric window regions, where the spectral lines are relatively weak. In these atmospheric windows, there is significant interest in the continuum absorption for several applications. For example, the continuum strongly impacts the radiative balance of the atmosphere, affects the propagation of laser radiation through the atmosphere and can interfere with the retrieval of atmospheric gases, aerosols and clouds by optical methods [3].

Depending on the spectral region, the continuum within water absorption bands is between two 63 and three orders of magnitude weaker than the overlying spectral lines. Nevertheless, even within 64 these bands, the continuum absorption can be comparable with the local line absorption or even 65 dominate it in many microwindows between spectral lines, which makes it distinguishable in 66 measurements with sufficient spectral resolution. The first laboratory identification of water dimer 67 spectral features in the in-band near-IR self-continuum was presented in [4,5] using the calculated 68 dimer spectrum from [6]. Since then, distinct spectral peaks have been discovered in the 69 measurements of the continuum absorption spectrum within other near-IR water vapour bands [4,7-70 9], which have allowed conclusions to be drawn about the nature of this component of the 71 continuum. Therefore, the investigation of the continuum absorption within the bands has 72 significance for our fundamental understanding of the underlying physics. 73

There are two physical mechanisms that are most often cited as being responsible for the 74 continuum absorption in the IR and mm-wave spectral regions, both of which likely contribute to a 75 76 certain extent in different spectral regions: (a) the cumulative absorption of the far wings of strong water monomer spectral lines [10-15], and (b) bound and quasibound water dimers<sup>1</sup> (b- and q-77 dimers, respectively) [7–9.16–21]. The first of these mechanisms, far-wing absorption, results from 78 energetic collisions between water molecules, which perturb rovibrational energy levels. There are 79 80 two main approaches to the far-wing hypothesis: asymptotic [12,15] and quasistatic [13,14]. Both approaches operate in terms of intermolecular potential and use a set of parameters derived by fitting 81 models to experimental data. A satisfactory agreement of the far-wing model with the experimental 82 continuum has been shown [22,23] in some atmospheric windows in the far and middle IR spectral 83 regions. However, the existing far-wing models cannot provide sufficient accuracy in predicting the 84 intensity or temperature dependence of the continuum absorption over a wide spectral region without 85

<sup>&</sup>lt;sup>1</sup>Bound (or stable) dimers require a third-body collision for their formation; quasibound (or metastable) dimers relate to multiple-approach pair collisions resulting in the temporary stabilization of a pair which has total internal energy in excess of the dissociation threshold.

a number of experimentally fitted *ad hoc* parameters that cannot be verified from independentsources.

The second mechanism, which is based on water dimer absorption, describes the main 88 temperature and spectral dependences of the continuum absorption well (see, for instance, [24]) after 89 adjusting just two physically-based parameters (the dimer equilibrium constants) to fit the 90 91 experimental data. Bound and quasibound dimers exhibit different properties (e.g. dissociation energy and lifetime), and consequently they are expected to have different spectral features. 92 Moreover, a statistical approach shows that absorption from either of these states can be the dominant 93 contributor tocontinuum absorption depending on the thermodynamic conditions [19]; b-dimers 94 dominate at lower temperatures and q-dimers are more prevalent at higher temperatures. The 95 'transition' temperature depends on the intermolecular potential and is different for different 96 97 molecular pairs. For example, for water dimers the transition temperature is expected to be close to room temperature [19]. 98

The absorption by water dimers is a dominant mechanism of so-called bimolecular absorption 99 by water vapour (see, for instance, [19]) at near atmospheric conditions. With increasing temperature, 100 the contribution of the third form of bimolecular absorption-free H<sub>2</sub>O pairs<sup>2</sup>-begins to increase: from 101 negligible at room temperature to dominant at very high temperatures. Since this mechanism 102 103 becomes noticeable only at temperatures much greater than the temperature range of 398-431 K 104 investigated here, it is not considered further. Earlier considerations of the possible absorption of solar radiation by water dimers in the visible and near-IR regions were presented in [25,26] based on 105 the first calculated water dimer vibrational spectra. To this day, quantum-chemical calculations of 106 water dimer spectra are still challenging, especially at higher wavenumbers (in near-infrared and 107 visible regions). Nevertheless, quantum-chemical and quantum-mechanical calculations [27-29] that 108 are now available together with the experimental data in the microwave [30,31], mid-infrared [3,32] 109 110 and near-infrared [4–8] spectral regions, demonstrate the explicit involvement of water dimers in the water vapour continuum spectrum. 111

For practical applications, the MT CKD continuum model is commonly used [33]. It is a 112 semiempirical model, which modifies the Lorentzian profile in the line wings using a special  $\gamma$ -113 function, assuming a so-called "weak interaction" between molecules, which is more important for 114 the in-band continuum, and makes a number of other empirical adjustments to fit the model to 115 experimental data. The model has therefore changed significantly since it was described in [33] as 116 new observations have become available; however many of these changes are not yet described in the 117 literature. In the spectral regions analysed here the MT CKD continuum has not been subjected to 118 any experimental constraints and needs to be evaluated using observations. Although MT CKD is 119 primarily intended for application at atmospheric temperatures, the form of its temperature 120 dependence is based on extrapolation of laboratory measurements made between temperatures of 296 121 122 and 338 K [33] in bands at lower wavenumbers and hence it may not be appropriate in other bands or at other temperatures. 123

This paper focuses on the investigation of the water vapour self-continuum absorption at elevated temperatures (398 and 431 K) and pressures (1000-4155 mbar) in the near-visible absorption bands centred at 8800 and 10600 cm<sup>-1</sup> (1.13 and 0.94  $\mu$ m) using laboratory observations. To our knowledge these are the first reported measurements of the self-continuum in these bands. These

<sup>&</sup>lt;sup>2</sup> Free pairs are two water monomers, which experience one-off collisions and influence each other weakly.

measurements are then interpreted in terms of the water dimer hypothesis. This work is an extension of earlier investigations [24] on the origin of the continuum in the 1600 and 3600 cm<sup>-1</sup> (6.25 and 2.7  $\mu$ m) absorption bands at close to room temperature. Finally, calculations of the atmospheric absorption due to this continuum are presented, by using a dimer-based model to extrapolate the measurements to atmospheric conditions.

The paper structure is the following. Section 2 contains the main details of the measurements. In Section 3, the measurement errors are considered. The retrieval procedure of the water vapour continuum is described in Section 4. The water dimer model of the continuum is presented in Section 5 and is discussed in Section 6. Section 7 contains the estimate of the effect of the newly-retrieved water vapour continuum to the atmospheric absorption. Conclusions are summarized in Section 8. The retrieved water vapour continuum data are given in the Appendix and in the Supplementary Materials 1 and 2.

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#### 2. Experiment

The pure water vapour absorption spectra were obtained at the Molecular Spectroscopy 142 143 Facility, Rutherford Appleton Laboratory (UK) in the near-visible spectral region 8500–13000 cm<sup>-1</sup>. The experimental setup included a Bruker IFS 125HR Fourier Transform spectrometer (FTS), 144 145 multipass absorption cell with optical path lengths of 9.7 and 17.7 m, Si-diode detector, 50 W quartz tungsten halogen bulb and vacuum system. In order to detect the weak continuum absorption in these 146 absorption bands, the measurements were carried out at elevated water vapour pressures up to 4155 147 mbar and temperatures of 398 and 431 K (see measurement details in Table 1). The relative humidity 148 did not exceed 75% to avoid water vapour condensation on the cell walls; the mirrors were also 149 150 checked visually for any evidence of condensation. The total optical path lengths in the multipass absorption cell were 9.7 m for pressures above 3000 mbar and 17.7 m for lower pressures. The 151 spectral resolution varied from 0.1 to 0.4 cm<sup>-1</sup> depending on pressure and was about 0.2–0.25 of an 152 153 average halfwidth of a spectral line.

A set of absorption spectra of pure water vapour at various pressures and temperatures were 154 obtained. Each measurement was conducted in three stages to reduce the error in determining the 155 baseline: (1) a background absorption spectrum of pure argon at the same pressure as the water 156 157 vapour pressure in step 2; (2) a sample absorption spectrum of pure water vapour; (3) repeat of stage 1. The background measurements with argon were found to be more effective than measurements of 158 an empty cell. Argon does not absorb radiation in this spectral region and was therefore useful to 159 minimise possible effects of cell deformation on optical alignment caused by the elevated gas 160 pressures. The baseline spectrum was derived as an average of the two background spectra. 161

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Table 1 Thermodynamic conditions and configuration of pure water vapour absorption spectra measurements

Temperature, K	Spectral interval, cm <sup>-1</sup>	Pressure, mbar	Optical length, m	Resolution, cm <sup>-1</sup>		
398	8505–9200, 10135–11110	1000 (6% ↓) 1370 (8.7%↓)	17.7	0.1 0.2		
431	8530–9195, 10055–11110	$\begin{array}{c} 1080 (3\% \uparrow) \\ 1580 (3\% \uparrow) \\ 2070 (1.5\% \uparrow) \\ 2101 (1.3\% \uparrow) \end{array}$	17.7	0.1 0.2 0.2 0.2		
		3145 (2.4% ↑) 4155 (3% ↑)	9.7	0.4 0.4		

\* The pressures given here are the spectroscopically-adjusted values using the method described in Section 3.2. The arrows indicate the reduction (↓) or increase (↑) due to this adjustment.

167 The experimental optical depth of water vapour absorption  $\tau(v, T)$  at wavenumber v and 168 temperature *T* was derived from the Beer–Lambert law. An example of an optical depth spectrum of 169 water vapour in the spectral region investigated is shown in Fig.1.

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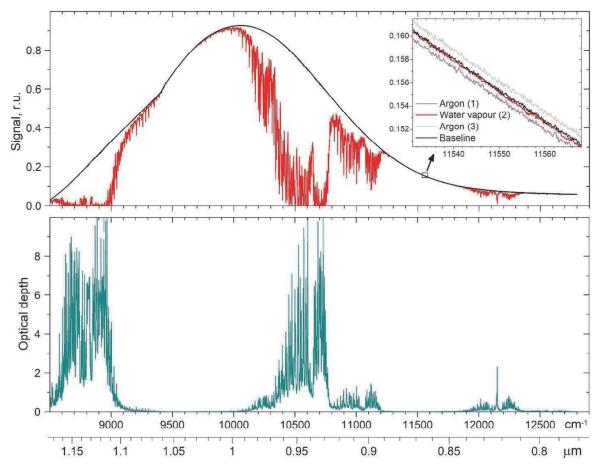




Fig. 1. FTS signals from measurements in the cell with argon (blackcurve) and water vapour (red curve) at a pressure of 3145 mbar and temperature of 431K (upper panel); the resulting spectrum of pure water vapour optical depth (dark cyan curve, bottom panel). To demonstrate the small baseline uncertainty, the insetin the upper panel shows the water vapour signal (red curve) and the baseline signal (blackcurve)obtained as an average of the signals from the cell with argon measured before (steps 1, light grey curve) and after (steps 3, dark grey curve) the sample measurements in a "window" spectral region where the continuum absorption is very weak compared to the in-band region. The kink in the baseline at about 9400 cm<sup>-1</sup> is due to the detector's sensitivity function.

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180 Deriving the water vapour continuum absorption from high-resolution absorption spectra first 181 requires the calculation and subtraction of the local contribution from water monomer lines. These calculations were made using the LBL<sub>IAO</sub> line-by-line program [34]. The local line contributions were 182 calculated within 25 cm<sup>-1</sup> from the centre of each Lorentzian line without the CKD "plinth". Water 183 vapour line parameters were taken from HITRAN-2016 [35]. The continuum data beyond 11150 cm<sup>-1</sup> 184 demonstrate weak values compared to the noise level; therefore, only the 8800 and 10600 cm<sup>-1</sup> 185 absorption bands are investigated. The retrieval of the watervapour continuum at higher 186 187 wavenumbers requires more sensitive measurements, for example, using the CRDS technique [36].

**3. Error analysis** 

*3.1 Error types* 

Discussion of the main sources of uncertainties for FTS measurements of the weak continuum absorption can be found, for example, in [37]. Here, four main error sources of error were identified and taken into account.

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#### 3.1.1 Random measurement error caused by the FTS system.

This error was evaluated by comparison of the noise within formation content at an optical depth of 1. To minimize this noise each measurement was averaged over hundreds of individual spectrometer scans. As a result, the information-to-noise ratio was not less than 500:1.

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## 3.1.2 A quasi-random error due to uncertainties in spectral line parameters used for the water vapour spectra calculations.

Although these errors do not depend on time, they are often not correlated with each other and have a random character over the spectrum. Error codes given in the HITRAN database for the line centres, intensities, temperature coefficients, and pressure broadening coefficients were used to estimatethe upper limit of the absolute error of this type (see details in [38]).

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## 3.1.3 Systematic errors caused by uncertainty in the spectral baseline (the FTS signal recorded when the cell contained argon).

208 The baseline was derived as an average of the signals obtained in measurements with argon before and after the water vapour absorption measurements. The inset in Figure 1 shows an example 209 in a window spectral region around 11550 cm<sup>-1</sup> where the continuum absorption should be negligible 210 under the experimental conditions. These errors may be caused by slow temporal drifts in the 211 spectrometer system or gas cell, and for individual measurements were partially mitigated by equal 212 213 separation in time of background spectra acquisitions in relation to that of the water sample. However, this type of error is usually negligible for the measurements of in-band continuum 214 absorption and does not exceed 1% in our case (see upper panel in Fig. 1). 215

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## 3.1.4 Systematic errors caused by the inaccuracy in measured water vapour pressure and temperature.

The main uncertainty here was from the pressure measurements. A description of how these errors were reduced using a spectroscopic technique is given in Section 3.2.

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#### 3.2 Adjustment of the water vapour pressure

The measured intensities of water vapour absorption lines are proportional to the water vapour pressure, while the intensity of the continuum absorption is proportional to the square of the vapour pressure. Therefore, the precise value of the water vapour pressure plays an important role in retrieval of the water vapour continuum. To reduce the respective systematic error in this work, we performed a spectroscopic assessment of the measured water vapour pressures by comparing measured and calculated line intensities using the HITRAN database.

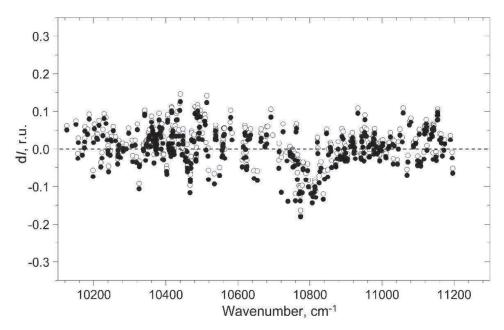
To exclude lines which are very weak or saturated, and lines with uncertain spectral parameters, we selected only spectral lines that have measured optical depths in the range 0.2 to 5 at line centre and an error-index for the line intensity and self-broadening of not less than 5 in HITRAN-2016. Then the measured intensities of the selected spectral lines were compared with those calculated line-by-line using the HITRAN-2016 parameters within a distance of a few halfwidths from the line centre. Figure 2 shows an example of a distribution of relative deviation for each selected i-th line ( $\delta I(v_i)$ ) in the investigated spectral region calculated using the equation:

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$$\delta I(v_{i}) = \frac{I_{RAL}(v_{i}) - I_{HIT16}(v_{i})}{I_{RAL}(v_{i})}.$$
 (1)

In Eq. (1),  $I_{\text{RAL}}(v_i)$  and  $I_{\text{HIT16}}(v_i)$  are line intensities obtained from the experiment and simulation, 236 respectively. The average relative deviation between measured and calculated intensities of all 237 selected lines was used as a criterion for the water vapour pressure adjustment factor. Systematic 238 239 divergence of the  $\delta I(v_i)$  distribution from zero indicates inaccuracy in the measured water vapour pressure. At the same time, strong deviations of  $\delta I(v_i)$  were also observed for individual lines, which 240 241 may be caused by errors in the parameters of relatively weak water vapour lines in the spectral database. Generally, the discrepancy was 4% on average in our measurements and we adjusted the 242 pressures to agree with the spectroscopically-derived values (see Table 1). 243

Measurements at T=471 K were also performed in this work. However, at some pressures these measurements had poor agreement between the measured and spectroscopically-derived pressure, as well as poor agreement with the pressure-squared dependence expected for the self-continuum absorption. Therefore, we excluded these measurements from analysis in this paper.





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Fig. 2. Relative deviation of line intensities in the spectral region under investigation for measurements at 431K and 2070
 mbar: empty circles – before pressure adjustment (2039 mbar), black points – after pressure adjustment (increased by 1.5%).

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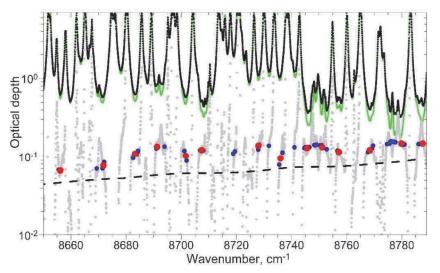
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#### 4. Retrieval of the water vapour continuum absorption

At the first stage of the analysis, the water vapour continuum optical depth  $\tau_c(v)$  was derived as a difference between the experimental optical depth spectrum  $\tau(v)$  (see Section 2) and the cumulative local contribution of water monomer lines  $\tau_{mon}(v)$  calculated with the line-by-line technique [34]. An example of the preliminary retrieval of the continuum absorption is given in Fig.3 (grey points). Fluctuations of the continuum at frequencies corresponding to water monomer line centres are caused by uncertainties in spectral line parameters. Generally, the retrieval of the continuum is not possible at line centres within absorption bands, because the continuum component is much less (2 orders of

magnitude) than the line contribution. Even small relative errors in line parameters lead to large 262 errors in the retrieved continuum. Therefore, the continuum absorption can only be derived in the 263 microwindows between absorption lines (blue points in Fig. 3), where the impact of uncertainties in 264 line parameters on the retrieved continuum is often relatively small (less than 10-20%). The 265 exclusion of line centres from the continuum retrieval does not lead to significant information loss 266 267 since the continuum possesses a rather smooth spectral character within several halfwidths of a spectral line. Moreover, spectral smoothing was applied to select the most reliable continuum 268 information within these microwindows - the continuum data points were obtained by averaging over 269 ten data points, corresponding to a derived continuum at a spectral resolution of between 1 to 4 cm<sup>-1</sup> 270 depending on the measurement pressure. This procedure helps to exclude false minima in the 271 experimental spectrum within microwindows. An example of the retrieved continuum spectrum 272 273 including smoothing is shown by the red points in Fig. 3. In the remainder of this paper, this smoothed continuum is used throughout. The semi-empirical MT CKD-3.2 continuum model [33] is 274 also shown (dashed line in Fig.3) for the measurement conditions. 275

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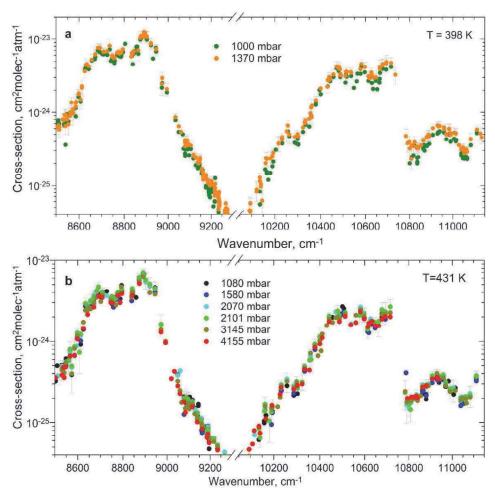
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**Fig. 3.** Example of the continuum absorption spectrum retrieved from the experimental data (431K, 1080 mbar): measured absorption spectrum of pure water vapour( $\tau(v)$ , black points), MT\_CKD-3.2 model (dashed line), calculated spectrum of the local line absorption  $\tau_{mon}(v)$  without the "CKD plinth" (green line), difference between the measured water vapour absorption and calculated local lines monomer absorption ( $\tau(v) - \tau_{mon}(v)$ , grey points), the differential spectrum  $\tau(v) - \tau_{mon}(v)$  after filtering (blue points), smoothed continuum spectrum  $\tau_c(v)$  (red points).

The self-continuum cross-section  $C_s(v,T)$  in units of cm<sup>2</sup>molec<sup>-1</sup>atm<sup>-1</sup> was derived using the equation

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$$C_{s}(\nu,T) = \frac{\tau_{c}(\nu)}{\rho_{s}P_{s}L} = \tau_{c}(\nu)\frac{kT}{P_{s}^{2}L} = \alpha(\nu)\frac{kT}{P_{s}^{2}}$$
(2)

where  $\rho_s$  and  $P_s$  are water vapour number density and pressure, respectively, *k* is the Boltzmann constant, *T* is temperature and *L* is the optical path length,  $\alpha(v)$  is the absorption coefficient. Figures 4 (a,b) illustrate the close agreement of cross-sections obtained from a range of pressures at both temperatures (398 and 431 K).



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Fig. 4. Cross-section spectra of the water vapour continuum absorption obtained using eq. (2) for two pressure sets:1000
and 1370 mbar at 398 K (a) and six pressures from 1080 to 4155 mbar at 431 (b) K. The error bars are given for the continuum cross-section spectra corresponding to 1370 mbar, 398 K (a), and 2101 mbar, 431 K (b).

A linear fitting was performed to confirm the pressure-squared dependence of the measured water vapour continuum absorption. The continuum absorption coefficients  $\alpha(v)$  versus  $P^2$  are presented in Fig.5 for some microwindows. There is good agreement between the experimental points and the fitted linear function (y=kx+b) and the intercept b is always close to zero. This helps confirm the quality of the observations. The slope of the straight line determines the cross-section value (Fig.6). Figure 6 demonstrates the expected inverse temperature dependence of the retrieved continuum absorption.

The retrieved self-continua within the 8800 and 10600 cm<sup>-1</sup> absorption bands demonstrates the 305 presence of several spectral peaks that are absent in the MT CKD-3.2 continuum model (dashed 306 lines in Fig.6), although the MT CKD-3.2 represents the overall shape of the continuum absorption 307 quite satisfactorily. Similar peaks were previously reported within more intense near-IR water vapour 308 absorption bands [9]. It is also apparent that the MT CKD-3.2 model underestimates the observed 309 continuum by about 1.5-2 times on average at the investigated temperatures in the centre of the 310 bands (see lower panel of Fig. 6). The data at 11084 and 11113 cm<sup>-1</sup> wavenumbers demonstrate the 311 greatest deviation from MT CKD-3.2 and may reflect the beginning of the q-dimer subband in the 312 continuum spectrum (see Fig. 9 and further discussion in Section 6). However, it was not possible to 313 retrieve this spectral feature completely since the difference between the experimental data and the 314 calculated contribution of water monomers turned out to be too noisy. 315

We acknowledge that MT\_CKD was not designed for application at such high temperatures, as it was intended for use in atmospheric conditions, although as noted in Section 1, the temperature dependence was defined using measurements at elevated temperatures at lower wavenumbers.

As a consequence of the above arguments, our measurements clearly indicate limitations in the MT\_CKD model in this spectral region and at these temperatures. A more physically-based model of the water vapour continuum is now required to address the limitations highlighted here. Such a model should include significant advances in experimental and theoretical capabilities, and to have a quite wide range of applicability beyond the conditions (both spectral and temperature) for which it was derived.

The cross-sections of the water vapour self-continuum absorption,\_obtained here for the first time from laboratory measurements at elevated temperatures, are given in Appendix 1.

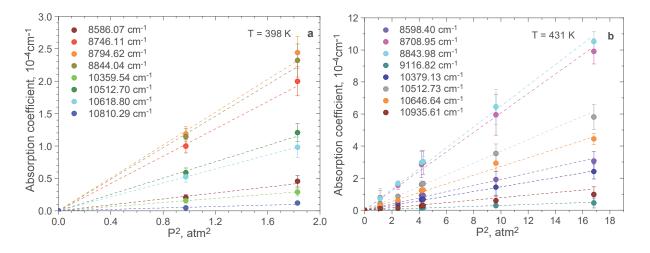


Fig. 5. Examples of P<sup>2</sup> dependence of the retrieved self-continuum absorption coefficients in some microwindows at 398
(a) and 431 (b) K.

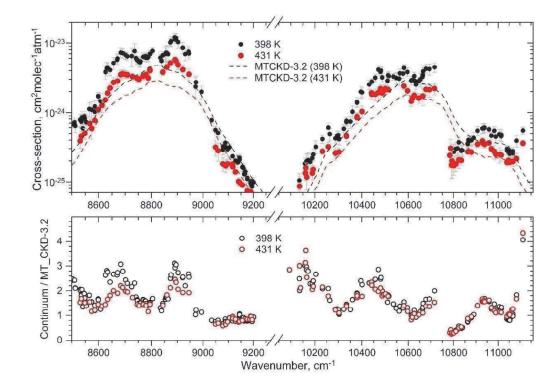


Fig. 6. Cross-section spectra of the water vapour self-continuum absorption retrieved from the experiment (upper panel)
 at 398 K (blue) and 431 K (red). The dashed lines show the corresponding MT\_CKD-3.2 model spectra. Respective ratios
 of the derived continuum to the MT\_CKD-3.2 model are shown in the bottom panel.

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#### 5. Simulation of water dimer absorption spectra

It has been shown in [7–9,20] that the spectral features of the water vapour self-continuum absorption within near-IR spectral bands are likely caused by a significant contribution from water dimers. In our study, the parameterization of the dimer model proposed in [9] was used for the 8800 and 10600 cm<sup>-1</sup> absorption bands. The total water dimer absorption cross-section (b-dimers + qdimers)  $C_s$  (in [cm<sup>2</sup>/atm/molec], where 'atm' and 'molec' applies to the pressure and number of water monomers, respectively) was simulated using the following equation:

$$C_s(\nu) = K_{eq}^b \sum_i S_i^b f_i^b (\Delta \nu_i, \gamma^b) + K_{eq}^q \sum_j S_j^q f_j^q (\Delta \nu_j, \gamma^q), \quad (3)$$

where  $K^{b}_{eq}$  and  $K^{q}_{eq}$  are the equilibrium constants of b- and q-dimers (in  $[atm^{-1}] \equiv [n_{dimers}/n_{monomers}]$  per 343 1 atm of water monomers]);  $S_{i}^{b}$  is the intensity of i-th subband of b-dimers [cm/dimer];  $S_{i}^{q}$  is the 344 intensity of i-th line of q-dimers [cm/dimer];  $f_{i}^{b}(\Delta v_{i}, \gamma^{b})$  and  $f_{i}^{q}(\Delta v_{i}, \gamma^{q})$  are Voigt profiles [cm] with 345 halfwidths at half-maximum intensity  $\gamma^{b}$  and  $\gamma^{q}$  [cm<sup>-1</sup>] of b- and q-dimers, respectively;  $\Delta v_{i}$  is the 346 distance from the centres of b-dimer subbands;  $\Delta v_i [cm^{-1}]$  is a distance from q-dimer line centre. The 347 calculation was carried out using the LBL<sub>IAO</sub> line-by-line program [34]. It is important to note that all 348 parameters in Eq.(3) have a clear physical meaning as opposed to the semi-empirical parameters that 349 are often used in continuum models. The physical background of the model parameters - and so, the 350 possibility to verify them from other sources – will allow us (similar to that in [24,39]) to estimate the 351 contribution of water dimers to the continuum absorption in the investigated bands (see Section 6). In 352 Section 7 (devoted to the atmospheric calculations), we will use this relatively simple dimer model to 353 extrapolate the self-continuum from 400-430 K to the 260-296 K temperature range. 354

Some data on the frequencies and strengths of several main bending and stretching oscillations 355 in b-dimers can be obtained from theoretical calculations and low-temperature measurements [28,40– 356 42]. In this work, the b-dimer spectrum was simulated on the basis of quantum-chemical calculations 357 358 of the O-H stretching vibrational overtone spectrum of the water dimer presented as two individually vibrating monomer units [29]. The used data for the intensities of b-dimer transitions is presented in 359 Table 2. The Voigt profile with 20 cm<sup>-1</sup> halfwidth was used to simulate the subbands shape of b-360 dimers, as it fits best the respective experimental features. However, this parameter has a minor effect 361 on the total water dimer spectrum (absorption by b- and q-dimers), since b-dimers contribute weakly 362 to the water vapour self-continuum at high temperatures within the bands investigated here (see 363 details below). Recently interpreted measurements [43] of the self-continuum in the 3600 cm<sup>-1</sup> band 364 at 296 K used a more sophisticated, although still speculative, approach to modelling the b-dimer 365 band shape. This is based on estimates of the b-dimer rotational constants and distinguishing between 366 parallel and perpendicular bands; at this lower temperature, the contribution of b- and q-dimers is 367 expected to be more equal, so that assumptions on the b-dimer shape are more important than is the 368 case here. 369

Table 2. Positions and intensities of transitions in bound dimer [29] used for the water dimer model.

Local mode assignments*	Wavenumber, cm <sup>-1</sup>	Intensity, cm/molec
0> <sub>f</sub>  2> <sub>b</sub>  1>	8530.5	2.35E-21
$ 20\rangle_{+} 1\rangle(70\%)+ 11\rangle_{+} 1\rangle(16\%)$	8754.9	6E-22
$ 2 \ge_{f}  0 \ge_{b}  1 \ge (63\%) +  1 \ge_{f}  1 \ge_{b}  1 \ge (22\%)$	8804.8	7E-21

$\begin{split}  20\rangle_{-} 1\rangle \\  1\rangle_{f} 1\rangle_{b} 1\rangle(66\%)+ 2\rangle_{f} 0\rangle_{b} 1\rangle(25\%) \\  11\rangle_{+} 1\rangle(74\%)+ 20\rangle_{+} 1\rangle(18\%) \\  0\rangle_{f} 2\rangle_{b} 2\rangle(69\%)+ 0\rangle_{f} 3\rangle_{b} 0\rangle(13\%) \\  0\rangle_{f} 3\rangle_{b} 0\rangle(80\%)+ 0\rangle_{f} 2\rangle_{b} 2\rangle(12\%) \\  30\rangle_{+} 0\rangle(77\%)+ 21\rangle_{+} 0\rangle(9\%) \\  30\rangle_{+} 0\rangle(67\%)+ 2\rangle_{f} 1\rangle_{b} 0\rangle(12\%) \\  30\rangle_{-} 0\rangle \\  1\rangle_{f} 2\rangle_{b} 0\rangle(68\%)+ 3\rangle_{f} 0\rangle_{b} 0\rangle(15\%) \\  21\rangle_{+} 0\rangle(80\%)+ 30\rangle_{+} 0\rangle(10\%) \\  2\rangle_{f} 1\rangle_{b} 0\rangle(74\%)+ 1\rangle_{f} 2\rangle_{b} 0\rangle(15\%) \\  2\rangle_{1} 1\rangle_{b} 0\rangle(74\%)+ 1\rangle_{f} 2\rangle_{b} 0\rangle(15\%) \\  2\rangle_{1} 1\rangle_{0} 0\rangle(74\%)+ 1\rangle_{f} 2\rangle_{b} 0\rangle(15\%) \\  2\rangle_{1} 1\rangle_{0} 0\rangle(74\%)+ 1\rangle_{1} 2\rangle_{b} 0\rangle(15\%) \\  2\rangle_{1} 1\rangle_{0} 0\rangle(10\%) \\  2\rangle_{1} 1\rangle_{1} 0\rangle(10\%) \\  1\rangle_{1} 1\rangle_{1$	8806.9 8930.1 9006.9 10057.5 10161.1 10601 10611 10615.3 10673.7 10869.7 10889.1	5.5E-20 1.9E-21 4.85E-24 2.65E-22 1.95E-21 1.85E-21 6.5E-21 1.8E-20 9.5E-21 8E-22 3.5E-21
$ 2>_{f_1} 1>_{b_1} 0>(74\%)+ 1>_{f_1} 2>_{b_1} 0>(15\%)$	10889.1	3.5E-21
$ 21>_{b_2} 0>$	11042	2.25E-21

377

\* According to the notation [28],  $|x>_{f}|y>_{b}|z>$  and  $|xy>_{\pm}|z>$ label the vibrational modes in the donor and acceptor water unit respectively. Here, x and y denote number of the vibrational quanta respectively in the free ('f') and bound ('b') OH-stretching mode in the donor unit, z is the quanta in the H<sub>1</sub>OH<sub>b</sub> bending mode, while "±" refers to the symmetry of the stretching vibrations in the acceptor unit.

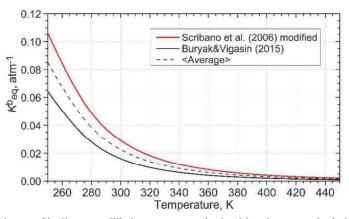
Quasibound dimers, which can be considered as a transitional state between free-pairs and b-378 379 dimers, have not been studied as much as the bound states. Therefore, a very simple approximate model of q-dimer lines was used here. In a similar way to [9], the q-dimer absorption spectrum was 380 simulated as a sum of strongly broadened water monomer lines with doubled intensity S<sub>i</sub> (i.e. 381  $S^{q}_{i} = 2S_{i}$ ). Strong broadening occurs because the lifetime of q-dimers is rather short (~10<sup>-12</sup> s). The 382 halfwidth of q-dimer lines was set to 10 cm<sup>-1</sup>, which corresponds to estimates of their average 383 lifetime (see [9]). Intensities of q-dimer lines were assumed to be equal to double the intensities of 384 the corresponding water monomer lines, as an approximation for two slightly interacting water 385 monomers in a short-lived metastable state. For simulation of the q-dimer spectrum, intensities and 386 centres of monomer lines were taken from the HITRAN-2016 database [35]. It was shown that the 387 total dimer spectrum agrees well with the measured continuum within 1600 and 3600 cm<sup>-1</sup> absorption 388 bands [9] despite using this quite simple model for the description of the q-dimer spectrum. 389

390 The main challenge in parameterization of the dimer model (Eq. (3)) is to determine the equilibrium constant of q-dimers. Direct quantum-chemical calculations of this value, especially for 391 the high temperatures observed here, are not available at present. In this work, an attempt was made 392 to derive both  $K^{b}_{eq}$  and  $K^{q}_{eq}$  values by fitting the model (Eq. (3)) to the retrieved continuum within 393 8800 and 10600 cm<sup>-1</sup>absorption bands. As a result, a satisfactory spectral agreement between the 394 395 dimer model and the continuum absorption spectrum was established. A significant difference in the 396 expected contribution of b- and q-dimers at the measurement temperatures was also observed, with a strong prevalence of q-dimers. This result supports the conclusion made on the basis of the statistical 397 approach [19,21] for the temperature dependence of  $K^{b}_{eq}$  and  $K^{q}_{eq}$ . However,  $K^{b}_{eq}$  values derived from 398 this fitting were characterized by significant estimated errors that exceed 100% in some cases. This is 399 due to the very small relative contribution of b-dimers to the total absorption at the investigated 400 temperatures, so that a simultaneous fitting of b- and q-dimer spectra to the continuum leads to large 401 estimated errors in the derived  $K^{b}_{eq}$  values and in the fitting itself. 402

Currently two relatively recent independent estimates of  $K^{b}_{eq}$  temperature dependence are 403 available [40,41]. The first [40] requires recalculation adjusted for a more accurate value of the 404 dissociation energy obtained from measurements [44] ( $D_0^{\text{new}} = 1105 \text{ cm}^{-1}$  instead of  $D_0=1234 \text{ cm}^{-1}$ 405 used in [40]). In our work, the adjusting factor  $e^{(D_0^{new}-D_0)/kT}$  was applied to  $K^{b}_{eq}$  from [40]. The 406 available calculated temperature dependences of  $K^{b}_{eq}$  (Fig.7, red [40] (modified) and black [41] (with 407  $D_0 = 1105 \text{ cm}^{-1}$ ) solid curves) noticeably differ from each other at low temperatures. Moreover, both 408 estimates are partially confirmed by different experimental data at temperature up to 350 K (see, for 409 example, Fig.6 (left panel) in [24]). Therefore, in the next step, the average value of these two 410

411 estimates (further denoted as  $K^{b(aver)}_{eq}$ ) was taken for simulation of b-dimer absorption spectra. 412 Table 3a contains the model parameters for b-dimer spectra calculation. Thus, the main fitting 413 parameter of the dimer model was the q-dimer equilibrium constant. Table 3b (column 5) presents 414 the obtained  $K^{q}_{eq}$  values as a result of fitting the dimer model (Eq. (3)) to the retrieved continuum 415 spectra with  $K^{b(aver)}_{eq}$  values from theoretical calculations (Table 3a, column 5) using the least square 416 method. The rms deviation of  $K^{q}_{eq}$  is 29% on average.

417



418

**Fig. 7.** Temperature dependence of b-dimer equilibrium constant obtained in *ab initio* calculations [40] and modified for  $D_0$  (see the text above) (red curve), and in [41] (black solid curve). The average values between [40] modified and [41] are shown by dashed black curve.

422

**423 Table 3.** Result of the dimer model parameterization:

424 **a** – Parameters for simulating b-dimer absorption spectra using theoretical calculations for equilibrium constant 425  $K^{b}_{eq}$  (see details above).

Temperature, K	Absorption band, cm <sup>-1</sup>	Intensities and centre positions	Subband HWHM, $\gamma$ , cm <sup>-1</sup>	$K^{\mathrm{b(aver)}}_{\mathrm{eq}},$ atm <sup>-1</sup>
398 431	8800, 10600 8800, 10600	Quantum-chemical calculations [29]	20	0.0031 0.0019

429

**b**– Parameters for simulating q-dimer absorption spectra using fitted values (5th column) and theoretical calculations for equilibrium constant  $K^{q}_{eq}$  (column 6, see Section 6).

Temperature, K	Absorption band, cm <sup>-1</sup>	Intensities and centre positions	Line HWHM, $\gamma$ , cm <sup>-1</sup>	$K^{q(fit)}{}_{eq},$ atm <sup>-1</sup>	$K^{ m q(calc)}{ m eq},$ atm <sup>-1</sup>
398 431	8800 10600 8800 10600	Strongly broadened monomer lines from HITRAN-2016 [35] with doubled monomer intensities	10	0.0306 0.0284 0.0170 0.0168	0.0090 0.0069

430

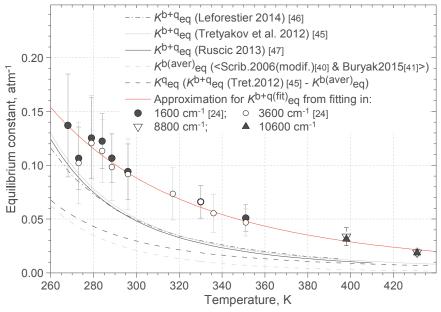
435

#### 431 **6. Discussion**

As mentioned earlier, there is no direct information about the q-dimer equilibrium constant at present, but it can be roughly estimated using information about the b-dimer and the total equilibrium constants as defined by Eq. (4)

$$K_{eq}^{b+q} = K_{eq}^b + K_{eq}^q.$$
(4)

436 Currently, three estimates of the total equilibrium constant  $K^{b+q}_{eq}$  are known from different 437 approaches to determine the second virial coefficient [45,46] and from the thermodynamic properties 438 of water dimers [47]. These data can be considered reliable as they are in good agreement with each other (see Fig.8, solid grey, solid black, and dash-dot black curves). In this work, we apply the temperature dependence of  $K^{b+q}_{eq}$  derived from the virial equation of state for real gases, using highly accurate measurements of water vapour thermodynamic properties [45]. The difference between  $K^{b+q}_{eq}$  [45] and  $K^{b(aver)}_{eq}$  was taken to get approximate temperature dependence of  $K^{q(calc)}_{eq}$  (see black dashed curve in Fig.8 and values in column 6 of Tab.3b). Column 5 in Tab.3b contains the values of  $K^{q(fit)}_{eq}$  obtained as a result of the dimer model fitting to the retrieved water vapour self-continuum spectra.



#### 446

Fig. 8. Temperature dependences of equilibrium constants obtained from different approaches: total equilibrium constant 447  $K^{b+q}_{eq}$  obtained from quantum-chemical calculation [46] (dash-dot curve), from the second virial coefficient [45] (solid 448 grey curve), and thermodynamic properties of water dimers [47] (solid black curve); average values of b-dimer 449 450 equilibrium constant  $K^{\text{b(aver)}}_{\text{eq}}$  [40] (modified) and [41] (grey dashed curve); q-dimer equilibrium constant  $K^{q(\text{calc.})}_{\text{eq}}$ obtained in this work as a difference between  $K^{b+q}_{eq}$  [45] and  $K^{b(aver)}_{eq}$  (black dashed curve); total equilibrium constant 451 452  $K^{b+q}_{eq}$  obtained from the fitting of the dimer model to experimental water vapour continuum spectra within 1600 and 3600 453 cm<sup>-1</sup> bands (black and white circles) [24];  $K^{b+q}_{eq}$  obtained from the fitting within 8800 and 10600 cm<sup>-1</sup> bands (white and 454 black triangles) in the current work; approximation function of all experimental points for the total equilibrium constant 455 derived using the water dimer continuum model [9] within the near-IR absorption bands (solid red curve).

456

The values of  $K^{q(fit)}_{eq}$  obtained from fitting the dimer model (Eq. (3)) to the experimental 457 continuum in two different absorption bands at each temperature are close to each other (see triangle 458 symbols in Fig. 8). This seems a reliable result as the concentration of water dimers (characterized by 459 an equilibrium constant) in water vapour should not depend on the spectral region. The examples of 460 fitting the dimer model (3) to the experimental data are presented in Fig.9 (a,b,g,h). Given the very 461 approximate character of the q-dimer absorption model (the second term in Eq. (3)) and the dominant 462 contribution of q-dimers at the investigated temperatures, the dimer model provides a fairly detailed 463 spectral description of the retrieved self-continuum spectra. 464

465 Comparison of values in columns 5 and 6 in Tab. 3b shows evidence that the fitted values 466  $K^{q(fit)}_{eq}$  are significantly greater than  $K^{q(calc)}_{eq}$  derived from Eq. (4) using reliable values, by about a 467 factor of 3 on average. A more complete picture of the dimer model parameterisation can be seen in 468 Fig.8. The total equilibrium constant  $K^{b+q}_{eq}$  data obtained at relatively low temperatures within 1600 469 and 3600 cm<sup>-1</sup> bands [24] and at elevated temperatures within 8800 and 10600 cm<sup>-1</sup> absorption bands 470 was interpolated in this work using the empirical fit

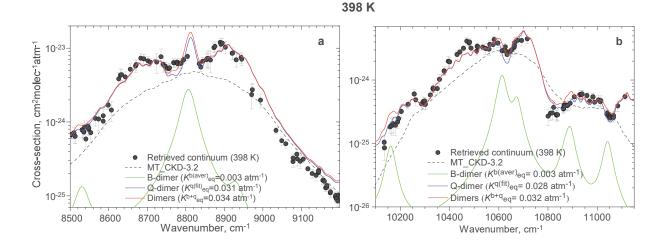
471 
$$K_{ea}^{b+q}(T) = 3.717 \cdot 10^8 \cdot T^{-3.886}.$$
 (5)

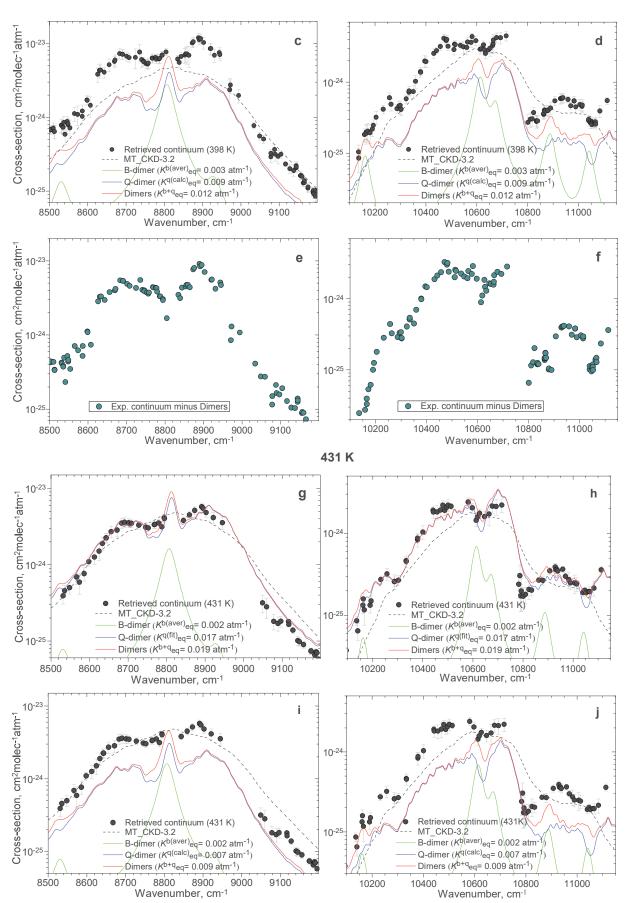
This can be considered as the temperature dependence of some *effective* total dimerization constant (solid red curve in Fig. 8); i.e. it is the constant that gives a satisfactory description of spectral behaviour and strength of the water vapour self-continuum in the investigated spectral regions, irrespective of the physical origin of the continuum (see upper panels at each temperature (a,b,g,h) in Fig.9) if the intensities of the b- and q-dimer used here are assumed to be correct and no other mechanisms were responsible for the continuum. We refer to the dimer model using this empirical fit as the "dimer-based model".

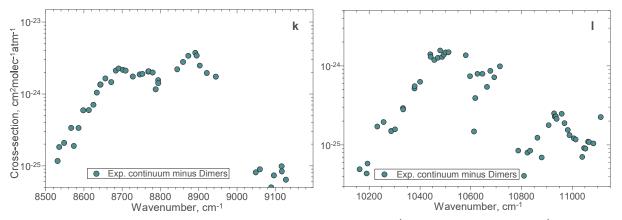
The effective equilibrium constant  $K^{b+q(fit)}_{eq}$  obtained in this work is a factor of 1.5-2.5 greater 479 than values of  $K^{b+q}_{eq}$  from prior estimates [45–47] across the entire temperature range. This means 480 the best fitting of the dimer model (Eq. (3)) requires a larger quantity of water dimers than can be 481 482 objectively explained at the considered thermodynamic conditions (according to the independent estimates), and it is K<sup>q</sup><sub>eq</sub> that is strongly overestimated in our model. One possible explanation of this 483 result can be a contribution from additional mechanisms for the water vapour self-continuum which 484 is not accounted for in our model. For example, it could be absorption by intermediate line wings as 485 suggested in [39]. The recent analysis [43] of measurements in the 3600 cm<sup>-1</sup> band at 296 K reached 486 a broadly similar conclusion, finding a factor of about 1.35 greater  $K^{b+q(fit)}_{eq}$  (which is within the 487 uncertainty at 296 K shown in Fig. 8) than expected from the prior estimates; they also suggested that 488 enhanced absorption in the intermediate wings [39] may explain the difference. Another explanation 489 could be overestimation of the intensities of fundamental transitions of the b-dimers in [29] caused by 490 the neglect of intermolecular vibrations in the dimer model. Inclusion of the intermolecular modes 491 into quantum-chemical calculations may potentially decrease the intensity of fundamental transition 492 (the main spectral peaks) up to 30% [48,49], but strongly increase the calculated underlying part of b-493 dimer absorption which is currently mostly attributed to the q-dimers by the fitting procedure. It 494 should be stressed that it is more likely that an overestimation of  $K^{q(fit)}_{eq}$  in our current fitting that 495 leads to the overestimation of the total  $K^{b+q(fit)}_{eq}$ . 496

Fig. 9 (c,d,i,j) contains the simulated water dimer absorption spectra using the values of  $K^{b(aver)}_{eq}$  (Table 3a, 5 column) and  $K^{q(calc)}_{eq}$  (Table 3b, column 6) obtained from Eq. (4). The integrated spectral contribution of the b-dimer and q-dimer absorption to the continuum is 36% at 398 K and 45% at 431 K in this case. The part of the retrieved continuum that is unexplained by water dimers using the currently-available theory, and total equilibrium constant, is presented in Fig. 9 (e,f,k,l).

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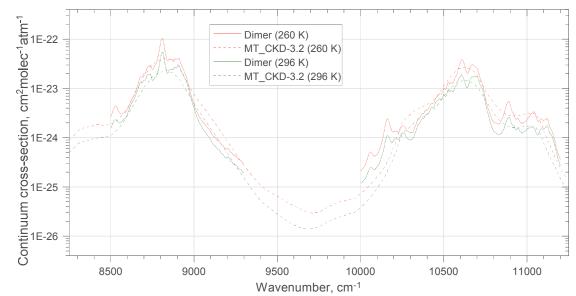
504 Fig. 9. Result of the water dimer model (Eq. (3)) fitting within the 8800 cm<sup>-1</sup> (left panels) and 10600 cm<sup>-1</sup> (right panels) absorption bands at 398 K (a-d) and 431 K (g-j). Upper panels at each temperature: the result of the water dimer model 505 fitting to the retrieved water vapour self-continuum cross-section spectra using the fitting parameter  $K^{q(fit)}_{eq}$ . Middle 506 panels at each temperature: the result of the water dimer model simulation using theoretically-derived estimated values 507  $K^{b(aver)}_{eq}$  and  $K^{q(calc)}_{eq}$ . Lower panels (e,f at 398 K and k,l at 431 K): the unexplained part of the continuum absorption 508 obtained as a difference of the retrieved continuum and the dimer model from middle panels (c,d at 398 K and i,j at 509 431 K). The water vapour self-continuum spectrum derived from measurements (black circles), model spectra of b- and 510 511 q-dimers (green and blue curves, respectively), total model spectrum of water dimers (red curve), MT CKD-3.2 model (dashed curve), the unexplained absorption spectrum (dark green circles). The parameter values of the water dimer model 512 513 are given in Tab. 3 a,b.

515

#### 7. Radiative impact of the new self-continuum

This section aims to determine how much of an effect the retrieved water vapour self-516 continuum absorption has from the perspective of atmospheric radiative transfer. Within the 517 investigated 8800 and 10600 cm<sup>-1</sup> absorption bands, water vapour lines and the self-continuum are 518 weaker than in the bands at lower wavenumbers. The near-visible absorption bands, unlike the 519 stronger near-IR bands, do not completely attenuate solar radiation between the top-of-atmosphere 520 and the surface layer (i.e. their absorption is not saturated); therefore, uncertainty in absorption within 521 these bands has more impact on the calculated shortwave surface fluxes than near-IR bands at lower 522 wavenumbers. 523

Despite the fact that our observations are limited by the elevated temperatures (398 and 431 K), 524 the good agreement between the experimentally-retrieved water vapour continuum and the dimer-525 based model (see Fig. 9, a,b,g,h) allows us to simulate H<sub>2</sub>O self-continuum spectra at atmospheric 526 temperatures by extrapolating the dimer-based model. Here, for the temperatures of interest, we 527 calculated the water dimer cross-sections (Eq. (3)) with the effective values of  $K^{b+q}_{eq}$  obtained from 528 the best fit to the experimental data at different temperatures and approximated using the temperature 529 dependence from Eq. (5). Figure 10 shows the extrapolated coefficients from the dimer-based model 530 at 296 and 260 K (see Supplementary materials 3), compared to those from MT CKD-3.2 at the 531 same temperatures. Despite MT CKD-3.2 being a factor of  $\sim 1.5$ -2 weaker on average than the 532 observed continuum at elevated temperatures, at atmospheric temperatures there is reasonable 533 agreement between the dimer-based model (using the effective value of  $K^{b+q}_{eq}$ ) and MT CKD-3.2. 534 However, this agreement must be treated with caution, as the true temperature dependence in these 535 bands, strictly speaking, may be different to that obtained from the combination of these and near-IR 536 bands at different temperatures (Fig. 8 and Eq. (5)) - we do not have direct observational evidence 537 that this is the case. Also, the dimer model and MT CKD-3.2 demonstrate different spectral 538 539 behaviour; the dimer-based model has various peaks and troughs corresponding mainly to the



transitions of the q-dimer, and there are also some larger differences at the edges of each of the two

541 bands.

542

543 Fig. 10 MT\_CKD-3.2 (dashed lines) and dimer-based model coefficients (solid lines) at 260 K (red) and 296 K (green).

We derived the dimer-based model spectrum at 296 and 260 K, which are the temperatures at which the MT\_CKD continuum coefficients are specified. For ease of incorporation into our radiative transfer model, we then use the MT\_CKD temperature dependence to interpolate the dimer absorption between these temperatures. The MT\_CKD temperature dependence is of the form

548 
$$C_{s}(\nu,T) = Cs(\nu,T_{0}) \left(\frac{C_{s}(\nu,T_{1})}{C_{s}(\nu,T_{0})}\right)^{(T-T_{0})/(T_{1}-T_{0})}, (6)$$

where  $T_0$  is 296 K and  $T_1$  is 260 K. Since this temperature dependence interpolates absorption crosssections between 296 and 260 K, and the dimer-based model shows a reason able agreement with MT\_CKD at these two temperatures (Fig. 10), one can expect that the temperature dependences of these two models do not deviate significantly in this temperature region. The highest tropospheric temperature used in our model atmospheres is 300 K, meaning that the MT\_CKD temperature dependence is suitable for modelling the range of temperatures we explore here (260-300 K); at 280 K the difference is no more than 3% at any wavenumber, and averages out to 0.15%.

To estimate irradiances, we use an updated version of the RFMDISORT radiative transfer tool 556 557 (used, for example, in [50]). This is a combination of two established radiative transfer codes; the Reference Forward Model [51] (a line-by-line code used to determine gas absorption) and DISORT 558 [52] (a multiple scattering code used to compute irradiances). A spectral resolution of  $0.1 \text{ cm}^{-1}$  is 559 used here. We use an offline version of MT CKD-3.2 to calculate continuum absorption, with 560 561 modifications using user-provided continuum absorption cross-sections. For this work, we used tropical (TRO), mid-latitude summer (MLS) and sub-arctic winter (SAW) standard atmospheres, 562 with specified profiles of H<sub>2</sub>O, CO<sub>2</sub> (at 380 ppmv), CH<sub>4</sub> (1.7 ppmv), O<sub>2</sub>, N<sub>2</sub> and O<sub>3</sub>. Spectral data is 563 obtained from the HITRAN2016 database. We used the Kurucz solar spectral irradiance [53]. These 564 calculations are for clear-sky conditions, and include the effects of Rayleigh scattering, with a 565 spectrally constant surface albedo of 0.3. For an overhead Sun, the original MT CKD-3.2 self-566 continuum reduces the downwelling surface irradiance by  $\sim 0.26$  W m<sup>-2</sup> in MLS conditions compared 567 to the no-continuum case across the 8500-9250 cm<sup>-1</sup> and 10000-112000 cm<sup>-1</sup> bands (see Fig.11 (c, 568 d)). This value is strongly dependent on the humidity; for SAW the absorbed irradiance is as low as 569

 $\sim 0.014 \text{ W m}^{-2}$ , but as high as  $\sim 0.46 \text{ W m}^{-2}$  for TRO. This makes up  $\sim 15\%$  of the total (self + foreign) continuum absorption and 0.5% of the total water vapour absorption in this spectral region in the MLS case; this contribution will be greater for more humid atmospheres, and lesser for less humid ones. In most radiation models, the continuum at these wavelengths is parameterised using versions of MT\_CKD. The results in many studies were obtained on the basis of MT\_CKD-2.5 in the shortwave (e.g. [54]). Here, we use MT\_CKD-3.2 as a benchmark, as this is the most recent version in which the water vapour continuum was updated.

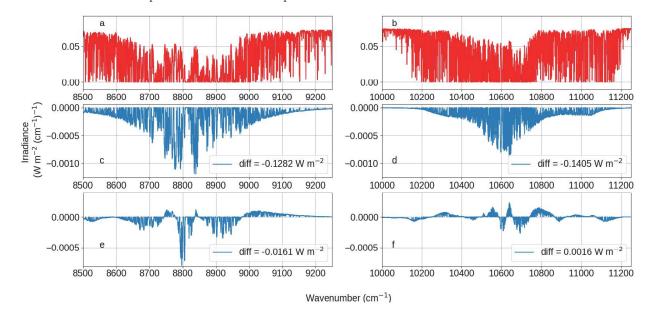


Fig. 11 Downwelling surface irradiance in the 8000-9250 cm<sup>-1</sup> (panels a, c and e) and 10000-11200 cm<sup>-1</sup> (panels b, d and
f) bands for a mid-latitude summer atmosphere with overhead Sun (panels (a) and (b), the modelled impact of the
MT\_CKD-3.2 self-continuum in these spectral regions (panels (c) and (d)), and the change in surface irradiance from
using the dimer-based model as opposed to MT\_CKD-3.2 (panels (e) and (f)). A negative value in panels (c), (d), (e) and
(f) indicates that the surface irradiance is being reduced, i.e. that additional absorption is occurring.

583

577

Figure 11 shows the calculated irradiances I at the surface for the model setup described above, 584 with the MT CKD-3.2 continuum shown in panels (a) and (b), the effect of the MT CKD-3.2 self-585 continuum in this region (panels (c) and (d)), derived as  $I_{MT CKD} - I_{no self-continuum}$  (where  $I_{MT CKD}$  and 586 Ino self-continuum are the irradiances including the MT CKD self-continuum and without it, respectively), 587 and the effect of the change between the continuum obtained by extrapolating the dimer-based model 588 in temperature and MT CKD-3.2 in panels (e) and (f), derived as Idimer model-IMT CKD. The data in 589 Fig. 11 was generated using MLS with an overhead Sun. The integrated difference (across the 8000-590 12000 cm<sup>-1</sup> region) between the two in this case is relatively small (roughly 0.021 W m<sup>-2</sup>), due to the 591 broad similarity between the MT CKD-3.2 and the effective water dimer spectra at the relevant 592 temperatures. For the MLS case described in Fig. 11, the reduction in the surface irradiance across 593 the two bands due to the self-continuum is 7% greater using the dimer-based model rather than 594 MT CKD-3.2; however, this is dominated by a decrease in irradiance of ~12.5% in the 8500-9250 595  $cm^{-1}$  region, with a much smaller decrease (~1%) in irradiance in the 10000-11200 cm<sup>-1</sup> region. A 596 more detailed breakdown of the effect of the dimer-based model relative to MT CKD-3.2 is 597 presented in Table 4, for a range of atmospheric profiles and solar zenith angles. It is interesting to 598 note that the increase in atmospheric absorption for the 60-degree solar zenith angle case in Table 4a 599 using the dimer-based model is greater for the MLS atmosphere than the more humid TRO 600 atmosphere in the 8500-9250 cm<sup>-1</sup> band. This is an indication that the saturation of absorption lines in 601 the tropical atmosphere reduces the effect of the enhanced continuum absorption at these higher 602

contribution changes in the solar zenith angle increases in some cases.  $10000-11200 \text{ cm}^{-1}$  band as the solar zenith angle increases in some cases.

The differences between MT CKD-3.2 and the dimer-based model from this work are largest 605 at the q-dimer band centres (according to blue curves in Fig. 9). These bands are included explicitly 606 within our model, whereas in MT CKD 3.2 they could be interpreted as being included indirectly in the "weak 607 interaction term", which would spread their effect over a wider spectral range (see e.g. Fig. 10). It is clear 608 from Fig. 11(e) that the narrow q-dimer peaks at ~8800 cm<sup>-1</sup> have a significant impact on the total 609 self-continuum absorption. There is better agreement with MT CKD when integrating across the 610 band, due in part due to the peaks and troughs in the dimer-based model cancelling each other out. 611 The sign of the change relative to MT CKD is dependent on the atmospheric conditions and solar 612 zenith angle; it is likely that some of the spectral features are causing some bands to saturate sooner 613 than others, within certain monomer band centres (which correspond to the q-dimer peaks which give 614 the dimer-based model its more detailed spectral structure). Despite this, the presence of these peaks 615 means that there may therefore be some useful spectral information that could be used to validate the 616 dimer model. An atmospheric measurement with a high enough precision (e.g. those used as part of 617 the Total Carbon Column Observing Network [55]) could potentially observe the sharply-peaked 618 features especially noticeable, for example, at ~ 8530 and 10160 cm<sup>-1</sup> (see Fig. 11). 619

While a change in the continuum may have an effect on water vapour retrievals (e.g. MODIS retrievals in the 915-965 nm band [56]), the significant cancellation of the peaks in this band (see e.g. Fig.11 c) results in a minimal change in the optical depth averaged over this spectral region going from MT\_CKD-3.2 to the dimer-based model.

Table 4 Differences between the spectrally integrated surface irradiances (dimer-based model – MT\_CKD-3.2) for
 different solar zenith angles and atmospheres, separated by spectral band.

626	<b>a)</b> 8500-9250 cm <sup>-1</sup>			
	Solar zenith angle	TRO	MLS	SAW
	0	-0.0218 (-11.7%)	-0.0161 (-12.5%)	-0.001 (-13.9%)
	30	-0.0168 (-10.11%)	-0.0165 (-14.3%)	-0.0009 (-12.8%)
	60	-0.0035 (-3.49%)	-0.0057 (-3.95%)	-0.0007 (-11.9%)
627				
628	<b>b)</b> 10000-11200 cm <sup>-1</sup>			
	Solar zenith angle	TRO	MLS	SAW
	0	-0.0003 (-0.14%)	0.0016 (1.14%)	0.0002 (3.1%)
	30	0.0002 (0.1%)	-0.0016 (-1.23%)	0.0002 (3.2%)
	60	0.0011 (0.8%)	-0.0002 (-0.11%)	0.0002 (3.3%)

629

\* Values are in W m<sup>-2</sup> integrated over each band. Values in brackets indicate the percentage change in the surface
irradiance due to self-continuum absorption within each band using the dimer-based model rather than MT\_CKD-3.2. A
negative number indicates that the surface irradiance has decreased (i.e. absorption has increased) when making this
change from MT\_CKD3.2 to the dimer-based model, and vice versa.

634

#### 635 8 Conclusions

Measurements of IR radiation absorption in pure water vapour using Fourier transform spectroscopy were used to retrieve the water vapour self-continuum absorption in the 8800 and 10600 cm<sup>-1</sup> water vapour bands at 398 and 431 K, and at pressures between 1000 and 4155 mbar. To our knowledge these are the first experimental derivations of the self-continuum in these bands. The dimer-based model of the water vapour self-continuum absorption, proposed for other infrared absorption bands in the earlier work [24], was parameterized and extended to higher wavenumbers

and higher temperatures by fitting the model to the experimental continuum spectra. A good 642 quantitative description of the continuum absorption by this model was established, but required 643 more water q-dimers than can be objectively explained by independent thermodynamic estimates. 644 The MT CKD-3.2 model demonstrates an underestimation of the observed continuum by about a 645 factor of 1.5-2 on average in the measured absorption bands at elevated temperatures. Moreover, the 646 647 characteristic spectral peaks observed in the measured self-continuum spectra are absent in MT CKD-3.2. The temperature dependence of the total *effective* dimerization constant was derived 648 in a broad temperature region from 268 to 430 K based on fitting of the dimer model to the measured 649 continuum spectra with one fitted parameter (the equilibrium constant of quasibound dimers) in this 650 work and the results of the lower temperature data in near-IR bands [24]. Using this temperature 651 dependence, the dimer-based model for 8800 and 10600 cm<sup>-1</sup> water vapour bands was then 652 extrapolated from 400-430 K to the temperatures 260-296 K, and was found to be in reasonable 653 agreement with the MT CKD-3.2 continuum model at these temperatures (see Section 7), but with 654 less agreement toward the band edges, and with some significant differences in narrow spectral 655 regions (corresponding to absorption features of the quasibound dimer). The dimer-based model 656 provides some support for the values produced by the MT CKD model at atmospheric temperatures 657 but not for the physical assumptions underlying that model. We suggest that the dimer-based model 658 could now be considered as a replacement to MT CKD for the in-band self-continuum as it is has 659 now been shown to simulate, with reasonable accuracy, the observed self-continuum in several near-660 IR bands. 661

It is shown that without our empirical adjustment to the equilibrium constant of quasibound 662 dimers, water dimers could account for not more than 50% of the detected water vapour self-663 continuum absorption within the 8800 and 10600 cm<sup>-1</sup> absorption bands at the investigated 664 temperatures. Possible reasons for the difference between this and the observed absorption could be 665 the presence of additional mechanisms that contribute to the in-band continuum (such as intermediate 666 line wings) or so-far neglected contributions in theoretical models of the bound dimer spectrum. In 667 addition, to minimize the uncertainty of the water dimer model, the spectrum of quasibound dimers 668 also needs to be studied in more detail. Hence, to advance understanding, improvements in 669 theoretical calculations are needed. Measurements of the continuum strength over a wider range of 670 experimental conditions would also be very beneficial in constraining theoretical models. The 671 extension of such work to include the foreign continuum would also be beneficial. 672

673

#### 674 Acknowledgments

Experimental part of the work was performed under financial support from the NERC-EPSRC (UK) 675 funded consortium CAVIAR (Continuum Absorption at Visible and Infrared wavelengths and its 676 Atmospheric Relevance (NE/D012082/1)). Processing of the experimental data and analysis was 677 supported by the Russian Foundation for Basic Research (project number 19-32-90157\19) and the 678 Ministry of Science and Higher Education of the Russian Federation (Program of the Basic Scientific 679 Investigations, budget funds for V.E. Zuev Institute of Atmospheric Optics of Siberian Branch of the 680 Russian Academy of Sciences). JE and KPS acknowledge support from the NERC "Advanced 681 Spectroscopy for improved characterisation of the near-Infrared water vapour Continuum (ASPIC)" 682 683 research grant (NE/R009848/1) during the writing phase of this paper. We thank the reviewers for many important suggestions. 684

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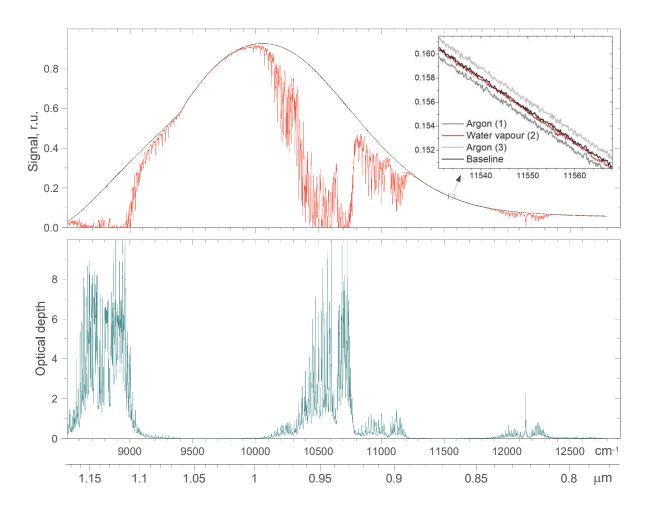
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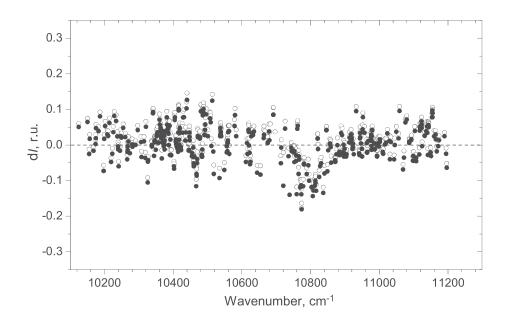
**Table 1.** Cross-section absorption,  $C_s(v)$  [cm<sup>2</sup>molec<sup>-1</sup>atm<sup>-1</sup>], of water vapour self-continuum experimentally retrieved in this work at 398 and 431 K within 8800 and 10600 cm<sup>-1</sup> absorption bands.

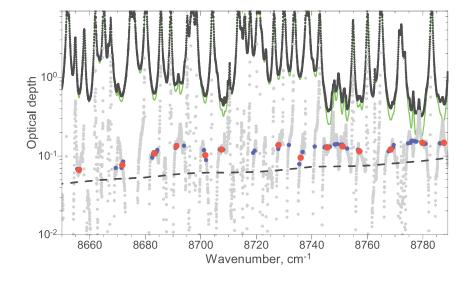
398 K					431 K						
v, cm <sup>-1</sup>	$C_s(v)$	$C^{err}_{s}(v)$	v, cm <sup>-1</sup>	$C_{s}(v)$	$C^{err}_{s}(v)$	ν, cm <sup>-1</sup>	$C_s(v)$	$C^{err}_{s}(v)$	v, cm <sup>-1</sup>	$C_s(\nu)$	C <sup>err</sup> s(v)
8502.76	6.85E-25	8.23E-26	10135.45	1.04E-25	2.62E-26	8531.26	3.9E-25	8.61E-26	10052.73	2.41E-26	3.01E-27
8503.12	6.73E-25	8.19E-26	10136.23	8.55E-26	3.19E-26	8535.51	4.57E-25	7.71E-26	10094.07	3.74E-26	7.38E-27
8503.18	6.84E-25	8.23E-26	10158.86	1.83E-25	3.70E-26	8548.44	5.00E-25	8.92E-26	10136.20	8.61E-26	1.06E-26
8510.23	7.16E-25	1.25E-25	10165.49	1.97E-25	5.53E-26	8566.64	6.90E-25	1.42E-25	10140.36	6.48E-26	1.51E-26
8512.94	6.43E-25	1.30E-25	10165.88	1.91E-25	5.63E-26	8573.81	5.89E-25	1.80E-25	10160.61	1.33E-25	2.81E-26
8513.09	6.40E-25	1.30E-25	10171.94	2.05E-25	5.72E-26	8586.10	7.64E-25	1.52E-25	10162.35	1.59E-25	2.86E-26
8531.32	7.85E-25	1.66E-25	10180.58	1.94E-25	5.81E-26	8598.40	1.09E-24	1.36E-25	10166.23	1.17E-25	4.08E-26
8531.69	7.75E-25	1.65E-25	10189.74	2.19E-25	4.83E-26	8612.80	1.26E-24	2.58E-25	10189.83	1.33E-25	2.64E-26
8535.36	7.42E-25	1.44E-25	10193.60	2.47E-25	4.69E-26	8624.98	1.51E-24	3.64E-25	10193.45	1.50E-25	2.28E-26
8535.51	7.36E-25	1.44E-25	10195.00	3.20E-25	6.90E-26	8633.68	1.90E-24	3.70E-25	10193.45	2.74E-25	2.80E-26
8535.60	7.32E-25	1.45E-25	10232.14	4.15E-25	5.68E-26	8643.08	2.24E-24	3.17E-25	10256.85	3.21E-25	5.20E-26
8537.83	8.53E-25	1.80E-25	10256.82	6.04E-25	1.00E-25	8643.17	2.24E-24	3.17E-25	10286.62	2.59E-25	3.37E-26
8541.11	5.89E-25	1.64E-25	10263.09	4.88E-25	9.67E-26	8643.30	2.25E-24	3.16E-25	10286.77	2.58E-25	5.29E-26
8546.57	8.81E-25	1.52E-25	10286.65	4.23E-25	5.84E-26	8656.13	2.71E-24	4.71E-25	10302.29	2.68E-25	3.62E-26
8548.44	7.99E-25	1.45E-25	10294.42	4.62E-25	8.09E-26	8671.47	2.84E-24	5.23E-25	10333.50	4.63E-25	4.14E-26
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8553.83	7.20E-25	2.01E-25	10302.29	4.13E-25	7.27E-26	8690.75	3.61E-24	5.18E-25	10378.85	8.37E-25	1.54E-25
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8585.92	1.03E-24	2.26E-25	10333.78	7.29E-25	7.12E-26	8708.95	3.48E-24	3.86E-25	10441.20	1.91E-24	1.69E-25
8586.07	1.22E-24	2.48E-25	10333.93	7.22E-25	7.52E-26	8727.97	3.29E-24	3.67E-25	10442.34	1.82E-24	2.92E-25
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8607.14	1.45E-24	4.44E-25	10359.54	1.03E-24	2.10E-25	8768.43	3.35E-24	3.71E-25	10480.01	2.20E-24	2.84E-25
8626.03	3.83E-24	8.44E-25	10378.92	1.40E-24	2.27E-25	8769.37	3.37E-24	3.71E-25	10487.24	1.90E-24	2.43E-25
8630.64	4.31E-24	9.40E-25	10379.28	1.38E-24	1.49E-25	8779.55	3.52E-24	3.57E-25	10494.26	2.06E-24	3.72E-25
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8656.13	5.16E-24	1.01E-24	10431.01	2.53E-24	4.05E-25	8794.59	4.04E-24	4.06E-25	10581.00	2.40E-24	2.92E-25
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9190.44	9.25E-26	1.20E-26									
9190.59	9.18E-26	1.21E-26									
9194.50	8.53E-26	1.34E-26									
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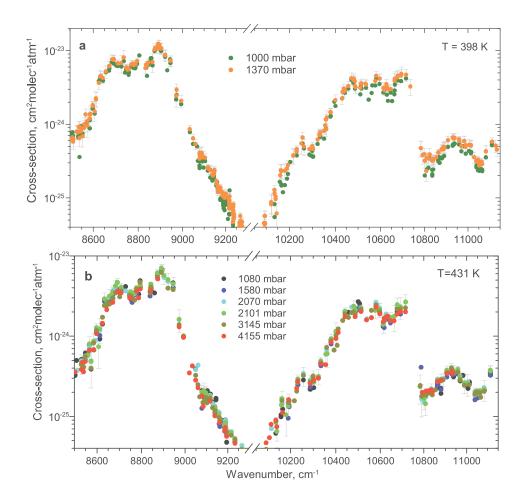


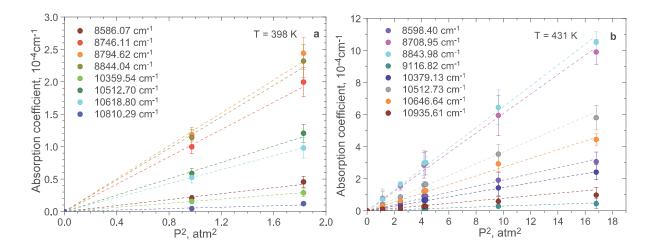


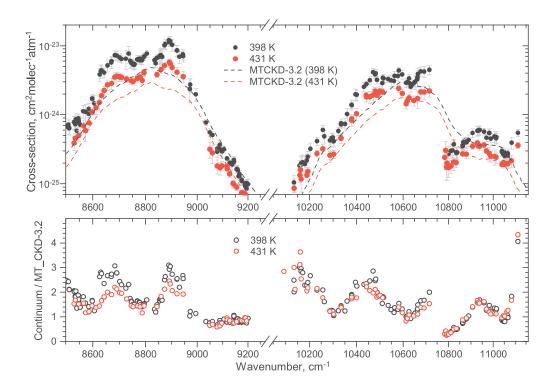


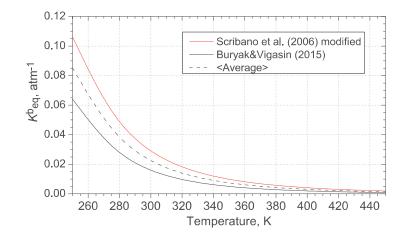


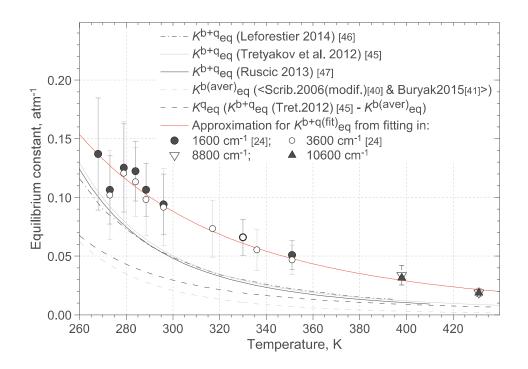


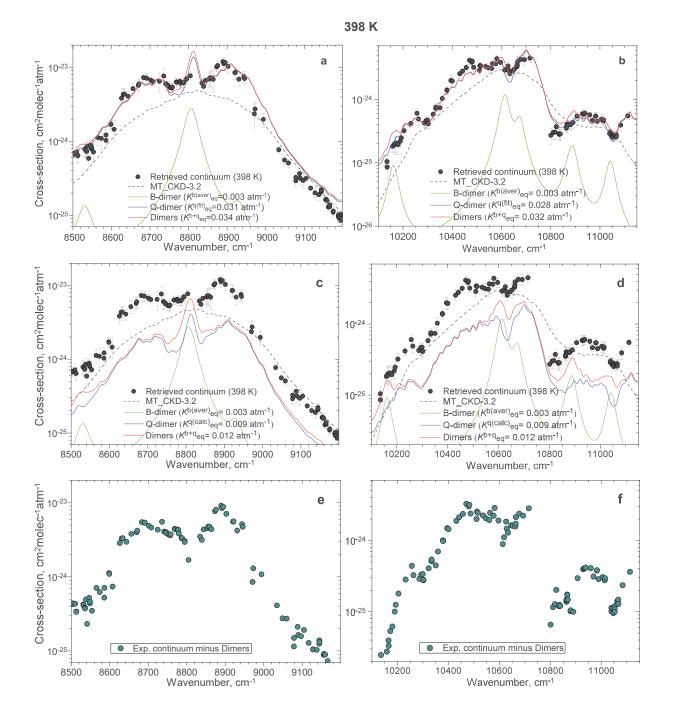


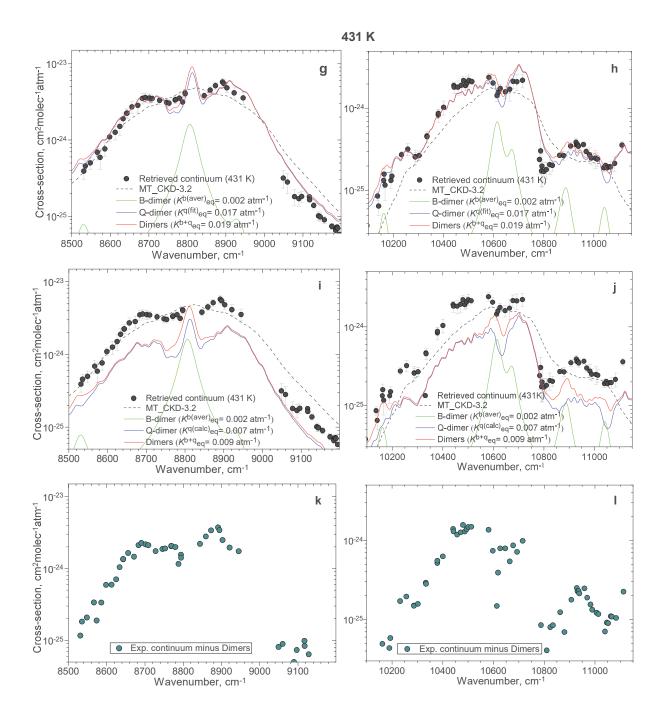


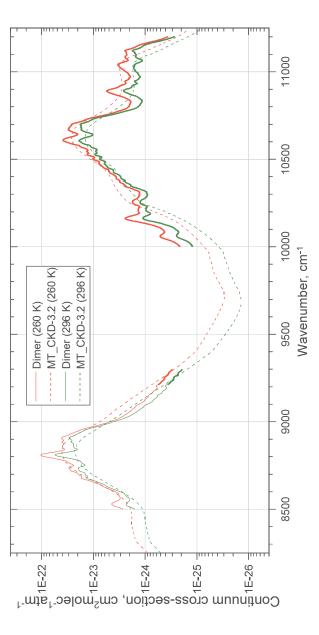


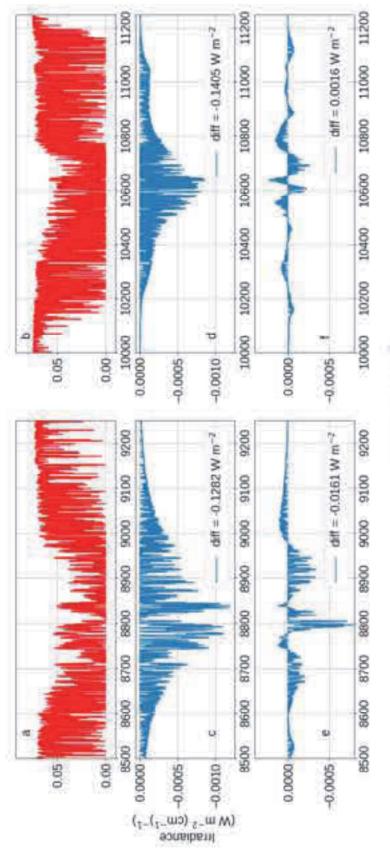












# Wavenumber (cm<sup>-1</sup>)