

*Mixed-anion mixed-cation perovskite
(FAPbI₃)_{0.875}(MAPbBr₃)_{0.125}: an ab
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Mixed-anion mixed-cation perovskite (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125}: an *ab-initio* molecular dynamics study

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Electronic Supplementary Information (ESI) available: atomic coordinates and additional figures.

Abstract. Mixed-anion mixed-cation perovskites with (FAPbI₃)_{1-x}(MAPbBr₃)_x composition have allowed record efficiencies in photovoltaic solar cells, but their atomic-scale behaviour is not well understood yet, in part because their theoretical modelling requires consideration of complex and interrelated dynamic and disordering effects. We present here an *ab initio* molecular dynamics investigation of the structural, thermodynamic, and electronic properties of the (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125} perovskite. A special quasi-random structure is proposed to mimic the disorder of both the molecular cations and the halide anions, in a stoichiometry that is close to that of one of today's most efficient perovskite solar cells. We show that the rotation of the organic cations is more strongly hindered in the mixed structure in comparison with the pure compounds. Our analysis suggests that this mixed perovskite is thermodynamically stable against phase separation despite the endothermic mixing enthalpy, due to the large configurational entropy. The electronic properties are investigated by hybrid density functional calculations including spin-orbit coupling in carefully selected representative configurations extracted from the molecular dynamics. Our model, that is validated here against experimental information, provides a more sophisticated understanding of the interplay between dynamic and disordering effects in this important family of photovoltaic materials.

Introduction

Hybrid organic-inorganic halide perovskites (HOIHP) have allowed to develop a promising generation of solar cells. Initial breakthroughs were achieved using perovskite MAPbI_3 (where MA is CH_3NH_3) as light absorber, reaching photo-conversion efficiencies (PCE) of 15% by 2013 [1]. In this material, the A, B, and X sites of the perovskite structure ABX_3 are occupied by the ions MA^+ , Pb^{2+} , and I^- , respectively. Other members of the HOIHP family are obtained when replacing iodide by other halide, replacing lead by another group IV cation, or replacing MA^+ by another organic cation or caesium. The full family includes random alloys of the pure compounds. It soon turned out that MAPbI_3 is barely stable against decomposition into lead iodide and methylamine iodide, causing fast device degradation. There have been significant achievements in the stability by means of interface engineering [2-4], and by alloying the cations and halides [5]. In the so-called mixed-cation HOIHP, the perovskite A-site is randomly occupied by a combination of different cations, *e.g.*, MA^+ , $\text{HC}(\text{NH}_2)_2^+$ (formamidinium, FA^+) or the inorganic cation Cs^+ . These mixed compounds show remarkable improvement in their stability and are related with the evolution of record PCE [3]. Some of the recent perovskite solar cell (PSC) record efficiencies have been obtained using light absorber perovskites with composition $(\text{FAPbI}_3)_{1-x}(\text{MAPbBr}_3)_x$ with $x \sim 0.15$ [6, 7], or with MAPbBr_3 as a trace [8]. This composition was introduced by Jeon *et al.* [9], showing that incorporation of MAPbBr_3 into FAPbI_3 stabilizes the perovskite phase of FAPbI_3 and improves the PCE, particularly for composition $(\text{FAPbI}_3)_{0.85}(\text{MAPbBr}_3)_{0.15}$.

The understanding of this material, and eventually the PSC development will benefit from atomic scale simulations of the bulk materials and the interfaces. The first obstacle is the lack of models for the randomly mixed compounds. Models of several binary alloys, with either a cation or lead substituted, have been published recently [10, 11]. In fact, some recent experimental studies of mixed-cation mixed-halide perovskites have been complemented with simulations with one element substituted [12]. In this work, an atomic scale model of the mixed-cation mixed-halide $(\text{FAPbI}_3)_{1-x}(\text{MAPbBr}_3)_x$ is presented. The mixing ratio $x = 0.125$ is considered for the model, which is computationally convenient and close to the composition present in optimized PSC. The model is based on pseudo-random substitutions of FA and I in FAPbI_3 , by MA and Br, respectively. We then study the structural and vibrational properties by means of *ab initio* molecular dynamics. The alloy properties are compared with those of the pure compounds FAPbI_3 and MAPbBr_3 . The electronic structure of the alloy is also studied by means of first principles calculations on carefully selected representative configurations.

Methods

Ab-initio molecular dynamics (MD) simulations were performed to investigate the structural, dynamical, and electronic properties of $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$, as well as the end members of the solid solution FAPbI_3 and MAPbBr_3 . Our MD simulations were conducted under NVT conditions at temperature $T = 350$ K using the CP2K package [13]. The ionic forces were calculated using first principles density functional theory (DFT). The hybrid Gaussian and plane wave method (GPW), as implemented in the QUICKSTEP module of the CP2K package [14], has been used. The forces for the molecular dynamics were calculated using the PBE functional [15] with the Grimme correction scheme DFT-D3 [16] to account for the dispersion interactions. The Kohn-Sham orbitals of valence electrons are expanded in a Gaussian basis set (DZVP-MOLOPT for Pb, I, Br, C, N, H) [17]. The effect of core electrons was included by means of dual-space GTH pseudopotentials [18-20]. The functional minimizations were performed using the orbital transformation method [21, 22]. The timestep was set to 1 fs. A Nosé-Hoover chain thermostat of length 3 was used, with a time constant of 10 fs during the initial 2000 steps, and 100 fs for the rest of equilibration and sampling stages. During the initial 2000 steps, each atom had one individual thermostat applied to; this is called a massive thermostat and facilitates a fast thermalization of systems with too different atomic masses, such as H and Pb. The simulations were extended up to 28, 26, and 23 ps for FAPbI_3 , MAPbBr_3 , and $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$, respectively. These systems were considered equilibrated after the initial 8, 6, and 5 ps, respectively, while sampling took place for the subsequent time ranges. The full set of atomic coordinates along the MD simulations are available in a public repository [23]. The atomic coordinates of the special configurations representing the average structures (see below) of each compound, are provided in the ESI.

The electronic structure of selected configurations was calculated using the Vienna Ab Initio Simulation Package (VASP) [24], with the PBE functional with spin-orbit coupling (SOC), as well as with the hybrid functional PBE0 (with fraction of exact exchange modified to 0.188 and SOC as discussed in Ref [25]). Allowing for SOC is mandatory to compute accurate conduction band energies in lead halide perovskites [26], while the hybrid functional is needed to obtain correct band gaps and band edge energies. Projected augmented wave (PAW) [27, 28] potentials of soft type were used for C, N and H, with 4, 5, and 1 valence electrons respectively. Standard PAW potentials have been used for Pb, Br, and I, which include 4, 7, and 7 electrons in the valence, respectively. A kinetic energy cutoff of 295 eV defines the plane waves basis set employed.

Results and discussion

Model generation

For FAPbI₃, we start from the structure of Ref. [10]. The 384-atom supercell was transformed into a 768-atom 4x4x4 cubic supercell by means of the lattice transformation $\mathbf{A}' = \mathbf{A} + \mathbf{B}$, $\mathbf{B}' = \mathbf{B} - \mathbf{A}$, where \mathbf{A}, \mathbf{B} (\mathbf{A}', \mathbf{B}') are the initial (final) supercell lattice vectors. The conventional cubic lattice parameter was set at the experimental value $a=6.3620$ Å [29]. For MAPbBr₃, we started from the structure of Ref. [30] with lattice parameter $a=5.9328$ Å. For our 768-atom supercell, the vector lengths are $A' = B' = 4a$. The initial orientation of the MA cations was taken from the MAPbI₃ polymorphic model of Ref. [31].

The solid solution (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125} was modelled by means of a special quasi-random structure (SQS) [32], which was generated as follows. First, the set of all symmetrically different configurations within a 2x2x2 perovskite supercell with composition FA₇MAPb₈Br₃I₂₁, was obtained using the site occupation disorder method (SOD) [33]. For this purpose, cubic crystal symmetry (space group 221) of the parent lattice was assumed, considering FA and MA as point atoms. For each of the 62 inequivalent configurations, the number of Br atoms (out of eight halides) in the first coordination sphere around MA, is 0, 1, 2 or 3. Eight of these 2x2x2 supercells were then combined to form a 4x4x4 supercell configuration that satisfies two conditions: (i) The halide-halide pair correlation function is as close as possible to the expected one for the random distribution, i. e. $\langle S_i S_j \rangle = (2x - 1)^2 = 0.5625$ [32], considering the fraction of halide sites occupied by Br, $x = 3/24$. For the best SQS configuration, the obtained pair correlation functions are 0.5625, 0.5070, and 0.3958 for the first, second and third coordination spheres, respectively. (ii) The distribution of MA-Br pairs is as close as possible to the binomial distribution expected for the random solution. The probability of finding n Br ions as nearest neighbours to the MA (out of $N=12$ halides) is $P(n) = C(N, n)x^n(1 - x)^{N-n}$. These numbers must be approximated to fractions $m/8$, as we combine eight 2x2x2 supercells to form the 4x4x4 supercell. This condition translates in the requirement of including two 2x2x2 configurations with $n=0$, three with $n=1$, two with $n=2$, and one with $n=3$, in the composition of the 4x4x4 supercell, as shown in Table S1 of ESI. The supercell generated in this way is shown in **Figure 1a**.

Finally, the point-like MA and FA cations were replaced in the obtained 4x4x4 supercell by the full molecular cations, giving them random initial orientation, and the structure was then thermalized by MD. **Figure 1b** shows the full structure, drawn with the same perspective as **Figure 1a**. The supercell size was set as $A = 4a$, with $a=6.3115$ Å, that results from linear interpolation of the experimental densities of the end compounds FAPbI₃ and MAPbBr₃. A theoretical (equilibrium)

lattice parameter could have been determined, but this would have needed expensive variable cell MD. Instead, some degree of validation was pursued by means of static variable cell optimization, enforcing the cubic shape of the supercell, and taking the initial atom coordinates from some random configuration of the MD. With this procedure, the optimized lattice parameter was found as 6.3125 Å, which is very close to the interpolated value used in the subsequent MD simulations with the NVT ensemble. Applying the same procedure to the end compounds, values 6.37253 Å, and 5.9312 Å, were obtained for FAPbI₃ and MAPbBr₃, respectively, which are also close to the experimental values above mentioned, used in our subsequent simulations.

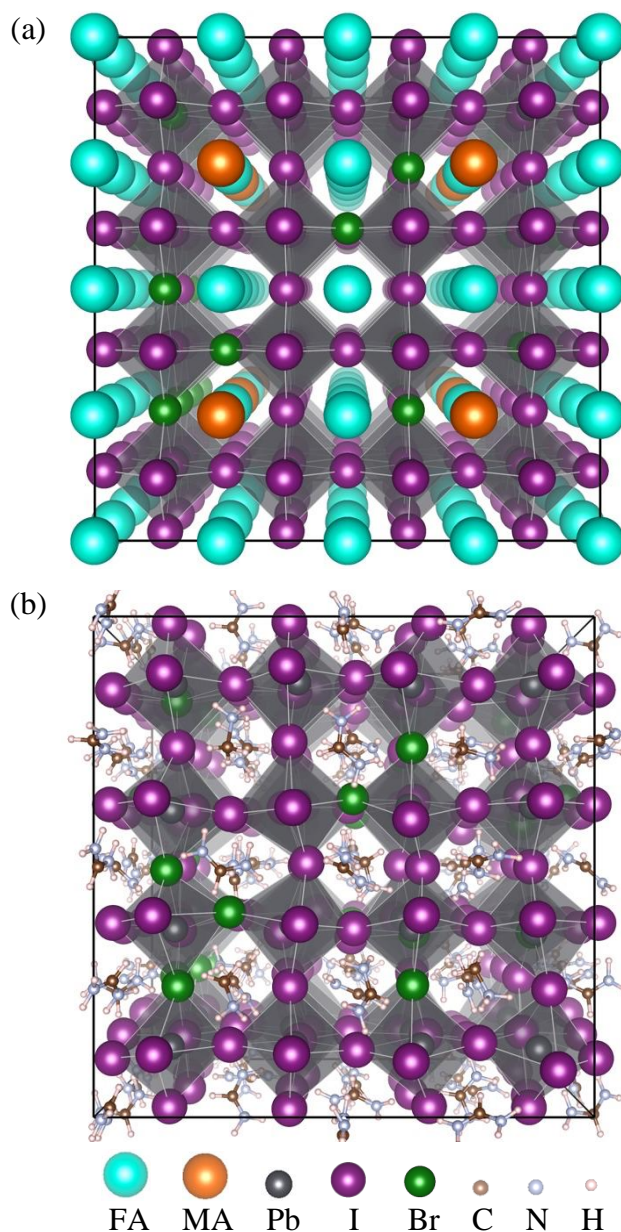


Figure 1. a) Model supercell of $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$ with MA and FA cations represented as point pseudo-atoms, and Br and I anions distributed following the quasi-random approach described in the text (all atoms at cubic perovskite symmetric positions). b) Snapshot of MD simulation at 350 K, with explicit atoms of MA and FA. Images generated with VESTA [34].

Structural analysis

We now discuss the structural information derived from the MD simulations. The descriptors of the local structure include pair distribution functions, angle distribution functions, and cation orientation, with especial attention given to variation induced by the cation and halide substitutions.

Figure 2 shows the partial pair distribution functions (PDFs) for the solid solution and the end members. Figure S1 in the ESI shows the same functions separately for the three compounds. The partial PDFs [35] are defined as:

$$g_{ij}(r) = \frac{V}{N_i N_j} \sum_k^{N_i} \sum_l^{N_j} \langle \delta(r - r_{kl}) \rangle, \quad (1)$$

where N_i and N_j are the number of atoms of the species i and j per volume V , containing N atoms of all species. The brackets $\langle \dots \rangle$ indicate the statistical average over the MD configurations. The total PDF is given as:

$$g(r) = \sum_{i,j} c_i c_j g_{ij}(r), \quad (2)$$

where the species fractional concentrations are $c_i = N_i/N$.

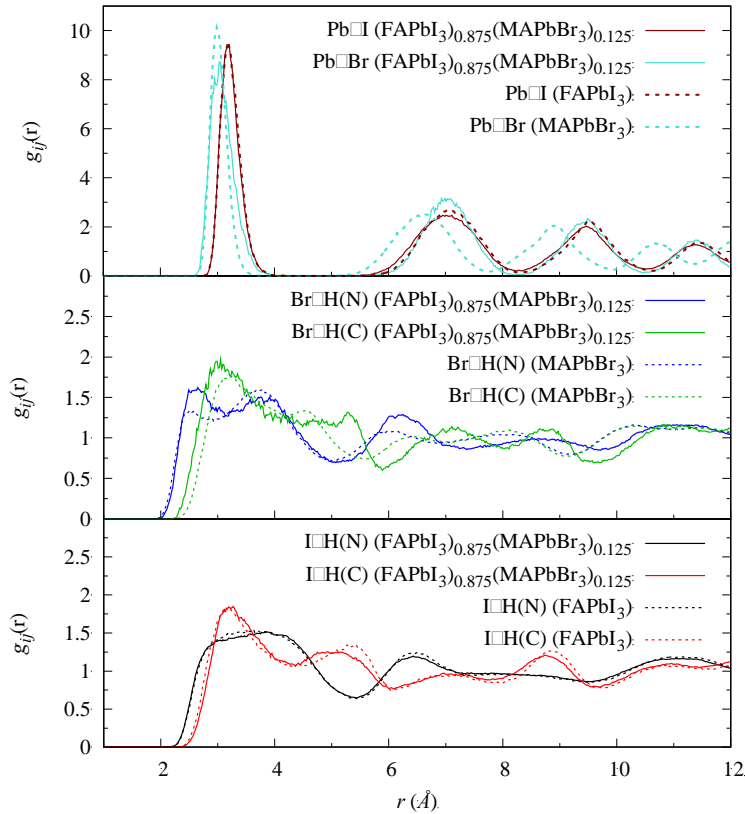


Figure 2. Partial pair distribution functions in $(FAPbI_3)_{0.875}(MAPbBr_3)_{0.125}$ and the pure compounds, for species Pb-I, Pb-Br and halide-H, differentiating the cases where H is bound to N or C.

All the simulation supercells considered in this work contain 64 A sites (occupied by MA or FA), 64 B sites (occupied by Pb), and 192 X sites (occupied by I or Br). In the simulation cell of $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$ there are 24 Br anions and 8 MA cations. As seen in **Figure 2**, the Pb-Br PDF at the range of the first coordination shell in the solid solution has the maximum at a similar distance (3.06 Å bond length) to the corresponding in MAPbBr_3 (3.01 Å), whereas the Pb-I bond length is the same (3.20 Å) in FAPbI_3 and in the solid solution. The shorter Pb-Br bond distance compared with Pb-I implies that Pb-Br-Pb trios are stretched, and the Br moves less freely in the solid solution than in pure MAPbBr_3 . **Figure 3** supports this statement, showing that the Pb-Br-Pb angles are closer to 180° in the mixture than in pure MAPbBr_3 , while the Pb-I-Pb angles in the mixture tend to be lower than in FAPbI_3 . **Figure S2** in the ESI shows the same data in separate plots for both Br and I angles, whereas **Figure S3** shows the distribution of dihedral angles X-Pb-X-Pb for all compounds. The three distributions are centred at 0°, indicating that the dynamic structure is consistent with cubic perovskites. For a tetragonal phase HOIHP displaying the typical octahedra tilting, the dihedral angle distribution would be bimodal, with two maxima centred around a positive and a negative angle [36]. The heterogeneous distribution of the Pb-X-Pb angles of the solid solution (unlike that of pure compounds) must generate deformations in the halogen cages that surround the organic cations, together with disparate Pb-Br and Pb-I bond lengths within each octahedra. Since the generated SQS supercell has a relatively homogeneous distribution of Br atoms, it is expected that these deformations should be present throughout the solid solution. These deformations are expected to disturb in some way the dynamics of the rotations of the organic cations in the mixture, because the well-known coupling between rotations and the vibrations of the inorganic framework. Also, the rotation of organic cations is guided by their hydrogen bonds interactions with their environment.

In **Figure 2**, the X-H (X=Br, I) PDF marks the difference between the H bonded to N or C. First, there is the double peak structure of the Br-H(N) PDF (Br with the H of the NH_3 group in MA) in pure MAPbBr_3 . The maximum at 2.53 Å signals hydrogen bonds, while the maximum at 3.79 Å indicate non-bonding distances. For FAPbI_3 , the PDF of I-H(N) (with the H of NH_2 end groups in FA) presents a single broad peak. This difference between Br-H(N) and I-H(N) is kept in the solid solution, regardless of the cation which the N-H species belongs to. The X-H(C) PDFs presents one single maximum at ~3Å. The maximum of the I-H(C) PDF occurs at the same distance in FAPbI_3 and the solution. In contrast, the maximum of the Br-H(C) PDF occurs at a slightly higher distance (compared with Br-H(C) PDF) in MAPbBr_3 , but at a smaller distance in the solution.

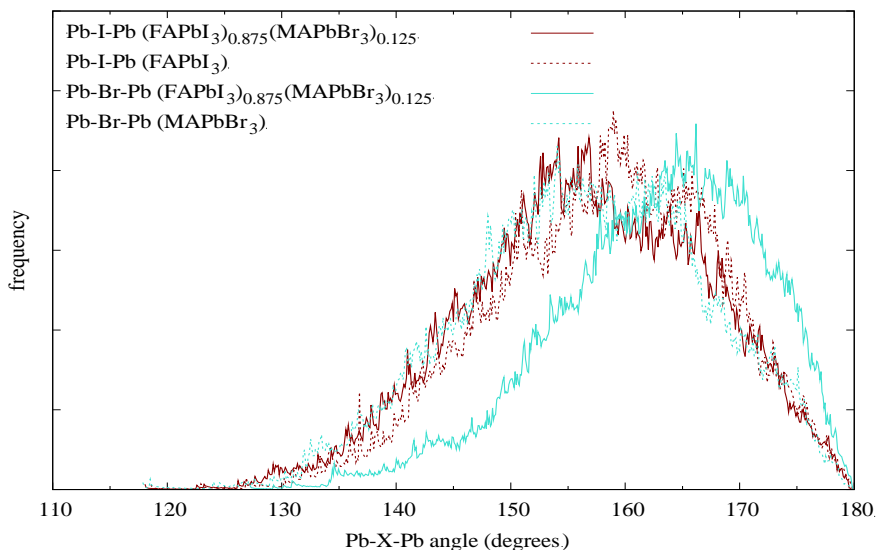


Figure 3. Distribution of Pb-X-Pb (X=Br, I) angles in the three compounds. Solid lines correspond to $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$, while dashed lines correspond to FAPbI_3 and MAPbBr_3 .

The Pb-Br PDF first peak in the solid solution is broader than in pure MAPbBr_3 . For higher coordination shells, the Pb-X PDF attain maxima at the same distances for both X=Br, I, although there are differences in the broadening and height of the PDFs. The Pb-halide distances for the second and higher coordination shells are determined by the lattice parameter. The decreased broadening of the Pb-Br PDF compared with Pb-I and with Pb-Br in MAPbBr_3 is difficult to interpret, but it may be related with the Pb-Br-Pb angles being closer to 180° , as shown in **Figure 3**.

The molecular dynamics shows that MA makes precession and rotations around its axis, with the NH_3 always pointing to the central Br (for 8 ps), although at the same time the CH_3 group points to other Br atoms. This can be seen in the video Br-1MA.mpg, provided in the dataset [23], which shows a local environment with 3 Br close to one MA. The Br atom at the centre is surrounded by 3 FA and 1 MA. The geometrical parameters are 4.0 \AA in distance cutoff, and 30° in angle cutoff. The hydrogen bonds are not permanent but form and break dynamically at this temperature.

When looking at the density maps of the C and N atoms of the solid solution (**Figure 4**), it is evident that the MA cations have an almost unique orientation during the trajectory, which is apparent in the video. This fact seems independent of the number of Br atoms (0-3 atoms) close to the MA cation. Furthermore, the density maps show that the orientation of the NH_3 group in the MA is not always towards the Br atom of the cage, see the extreme bottom-right in **Figure 4b**. All the evidence shows that the MA cations in the solid solution have the rotation affected by two causes: the deformations of the halogen cage that surrounds them, and the favourable hydrogen bond interactions towards the Br atoms. These causes should also affect the rotation of the FA cations, but the N density maps of these cations appear almost spherical. For comparison, Ghosh et

al [37] have shown a pronounced asymmetry in the N atom density map, together with stable cage deformation, in $\text{FA}_{0.9}\text{Cs}_{0.1}\text{PbI}_3$. In the next section some similarities with the case of $\text{FA}_{0.9}\text{Cs}_{0.1}\text{PbI}_3$ are exposed.

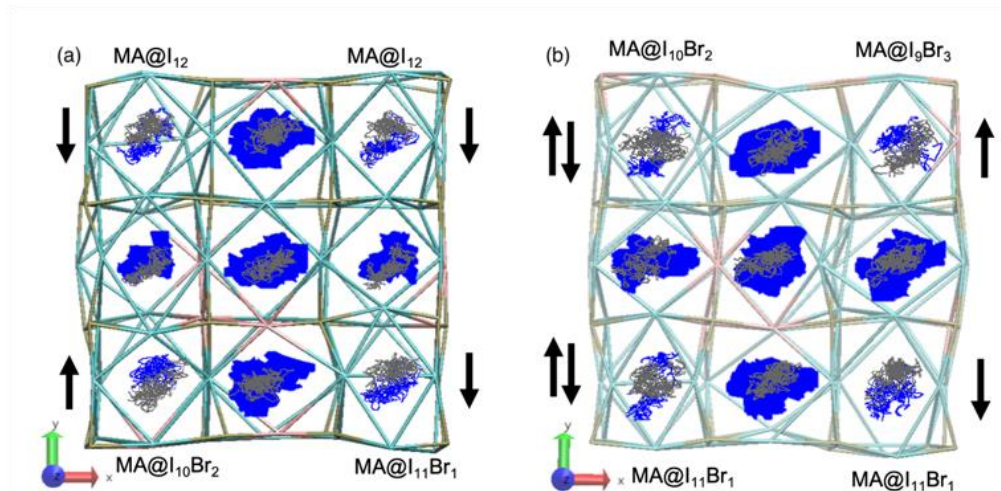


Figure 4. Density plots for N (blue) and C (grey) in a snapshot of the inorganic framework (Pb (ochre), I (cyan), Br (pink)) of the solid solution. Two different layers of the supercell are represented (a and b). Only the region that contains the MA cations is represented, corresponding to three lattice constants in each direction. The figure shows labels for the densities of the MA cations and the composition of the surrounding halogen atoms. The black arrows indicate the orientation of the MA dipoles within the cuboctahedra. The densities corresponding to the FA cations are not labelled.

Dynamic properties

The orientation dynamics of organic cations is one of the fingerprints of HOIHP, modifying the dielectric response, carrier conductivity, and thermodynamic properties, among others. In MD, this information can be obtained from the vector autocorrelation function [38], defined as:

$$c(\tau) = \frac{1}{N} \sum_{n=1}^N \langle \hat{n}(t_n) \cdot \hat{n}(t_n + \tau) \rangle, \quad (3)$$

where N is the number of different time origins averaged, the unit vector $\hat{n} = \mathbf{u}/|\mathbf{u}|$, and \mathbf{u} is the relative position vector of pairs of atoms that define molecular orientation. **Figure 5** shows the $c(\tau)$ functions for three characteristic vectors: (i) vector C-N in MA^+ parallel to molecule dipole, (ii) vector C-H in FA^+ , also parallel to molecule dipole and to the short molecule axis, and vector N-N in FA^+ , associated to the so-called tumbling motion that rotates the long molecule axis [37]. In the three cases, the curves decay more slowly in the solid solution (solid lines) than in the pure compounds (dashed lines), indicating that mixing slows down the cation reorientation dynamics of both the MA and the FA cations (although the effect seems stronger for the former than for the

latter). The slowing down of FA orientation dynamics after cation mixing has previously been observed in MD simulations of $\text{FA}_{0.9}\text{Cs}_{0.1}\text{PbI}_3$ in Ref. [37].

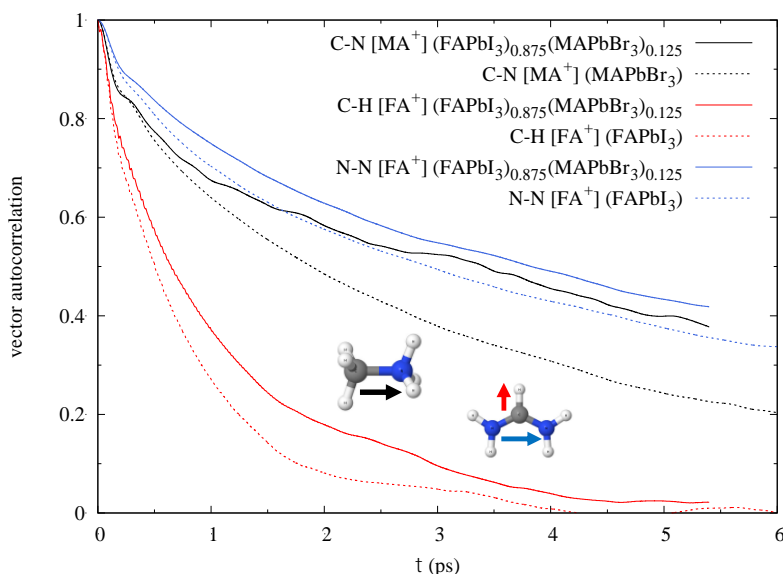


Figure 5. Vector autocorrelation of organic cations (rotation). The insets indicate the vectors in MA^+ (C-N), and FA^+ (C-H and N-N), using the same colours as in the corresponding curves.

Additional insight can be obtained from the evolution of the polar angle of vector C-N (MA^+) with respect to each Cartesian axis, displayed in **Figure S4** in the ESI. These cations are surrounded by 1, 2 or 3 Br atoms. It can be observed that proximity to 1 or 2 Br tend to fix the orientation of MA^+ , and the events of orientation reversal occur rather abruptly. When MA^+ is surrounded by 0 or 3 Br, orientation reversals occur more frequently, and are not abrupt. **Figure S5** in the ESI shows that in pure MAPbBr_3 , MA^+ cations continuously change their orientation. The restriction of MA^+ motion in $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$ is contrary to the expectation that MA^+ could rotate more freely in a wider cuboctahedral cavity, given the larger lattice parameter, compared to MAPbBr_3 .

These results on the reduced mobility of organic cations in the mixture are consistent with several experimental observations. Grüninger *et al.* [12] have performed an NMR study of the $^1\text{H} - ^1\text{H}$ correlations in $(\text{FA}_x\text{MA}_{1-x}\text{PbI}_3)$ and $(\text{FAPbI}_3)_{0.85}(\text{MAPbBr}_3)_{0.15}$, their results suggesting a restriction of the mobility of the organic cations in $(\text{FAPbI}_3)_{0.85}(\text{MAPbBr}_3)_{0.15}$. Johnston *et al.* [39] have arrived at a similar conclusion based on quasi-elastic neutron scattering measurements of triple-cation mixed halide perovskites in a low temperature hexagonal (non-perovskite) phase. They have found a correlation between cation rotation inhibition (particularly FA) and carrier lifetime, which is maximized when the Br content is 15%. They attributed the optimality of 15% Br content to that being the ratio at which approximately one every six halides are bromine. By means of Monte

Carlo simulation, they showed that for 15% Br content, the frequency distribution of Br is, from highest to smallest, 1, 0, 2, and 3 Br per unit cell.

Our observation that cation rotation is inhibited in proximity to one or two Br anions, even at this high temperature of 350 K, is qualitatively consistent with that frequency distribution. Simenas *et al.* [40] have applied dielectric spectroscopy to mixed-cation $\text{FA}_x\text{MA}_{1-x}\text{PbBr}_3$ and have obtained several activation barriers, concluding that FA presence raises the MA rotation barriers. They have also found several dielectric relaxation modes that are present only in pure FAPbBr_3 , suggesting that MA presence also hampers FA movements.

Vibrational properties

Figure 6 shows the partial vibrational densities of states (VDOS) of $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$, FAPbI_3 , and MAPbBr_3 . The vibrations of the inorganic backbone are in a band in the range 0–200 cm^{-1} . This band also contains important contributions from FA and MA. The band in the range 500–800 cm^{-1} is due to FA vibrations only, while the band in the range 1000–1800 cm^{-1} is due to both MA and FA vibrations. The band for frequencies larger than 3000 cm^{-1} is due to the stretching of C–H and N–H bonds in the organic cations [41]. As can be appreciated from **Figures 6a** and **6b**, the VDOS and the partial VDOS of the solid solution is almost identical to the weighted sum of the DOS of the pure compounds. This observation suggests a possible method for quantification of the composition x in the solution. In particular, the amount of FA^+ can be determined from isolated modes in the range 1675–1800 cm^{-1} , which are associated to the stretching of the double resonant C=N bond of FA^+ . The out-of-plane N–H bending modes of FA^+ , in the range 400–800 cm^{-1} could also be used. The band of stretching modes should be more effective in practice, because there are no more modes at this high frequency. MA^+ modes display isolated bands or peaks in the ranges 900–980 cm^{-1} , 1235 cm^{-1} , and 1400–1500 cm^{-1} . The intensity ratios of some of these bands in IR spectra may allow a quantification of the MA/FA content. On the other hand, Br content cannot be easily determined because the Br and I partial VDOS overlap in the same spectral region.

The fact that the VDOS of the solid solution is well approximated by the weighted VDOS of the compounds, suggests that the contribution of vibrations to the free energy of mixing is relatively small and can be neglected in a first approximation. This is important because it allows us to analyse the stability of the solid solution considering only energies and configurational entropic effects, as we do in the next section.

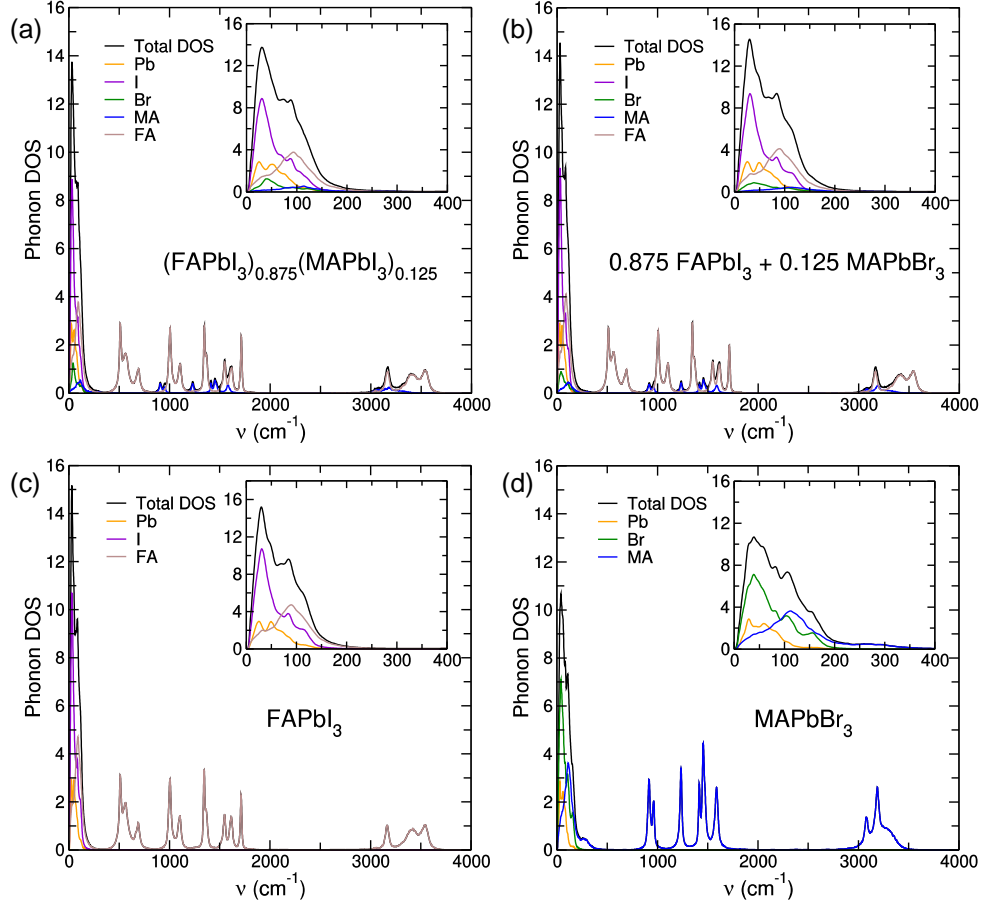


Figure 6. Vibrational density of states (VDOS) and contribution of each crystal site to the total VDOS for a) the solid solution $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$, b) the linear combination of $0.875 \text{ FAPbI}_3 + 0.125 \text{ MAPbBr}_3$, c) FAPbI_3 , and d) MAPbBr_3 .

Thermodynamics of mixing

We have calculated the enthalpy of mixing per formula unit of $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$ with respect to the pure compounds FAPbI_3 and MAPbBr_3 using the equation:

$$\Delta H_{\text{mix}} = \frac{1}{64} \{E[(\text{FAPbI}_3)_{1-x}(\text{MAPbBr}_3)_x] - (1-x)E[\text{FAPbI}_3] - xE[\text{MAPbBr}_3]\}, \quad (4)$$

where the E values are the average energies for the corresponding supercells from the ab initio MD, and $x=0.125$ is the MAPbBr_3 molar fraction. We obtain $\Delta H_{\text{mix}} = 1.39 \text{ kJ/mol}$, which means that the mixing is endothermic. However, the configurational entropy

$$S_{\text{conf}} = -4k_B(x \ln x + (1-x) \ln(1-x)) \quad (5)$$

is large (12.5 J/mol K for $x=0.125$) due to the factor of 4, which appears because there are four mixed sites (1 MA/FA and 3 Br/I) per formula unit. Assuming that the enthalpy of mixing and the configurational entropy contribution are the dominant effects on the stability, the free energy of mixing is predicted to be negative ($\Delta G_{\text{mix}} = -3.00 \text{ kJ/mol}$).

To assess whether the mixed perovskite can be expected to be stable with respect to phase separation into MAPbBr₃-rich and FAPbI₃-rich compounds, it is not enough to obtain the mixing free energy at the given composition (which quantifies the stability with respect to the pure phases). We also need to calculate the free energy at the whole range of compositions to assess if the given composition lies within a miscibility gap. Ab initio molecular dynamics are too computationally expensive to perform for the whole range of compositions, but we can extrapolate our one-point result using the widely used regular solid solution model [42-45], where the enthalpy of mixing is given by:

$$\Delta H_{\text{mix}} = W_0 x(1 - x), \quad (6)$$

for which we obtain $W_0=12.7$ kJ/mol. With this enthalpy parameter, the mixing free energy in the regular solution model is convex for the full range of compositions at 350 K, implying that there is no miscibility gap: with 4 mixed sites per formula unit, the enthalpy parameter W_0 would need to be greater than the critical value of $8k_B T$, or ~ 25 kJ/mol at 350 K, for a miscibility gap to exist.

The above analysis suggests that the mixed perovskite is indeed thermodynamically stable against phase separation. Although we have ignored other possible contributions to the thermodynamics of mixing (including vibrational and rotational contributions to the entropy of mixing), the low enthalpy of mixing in the regular model, well below the critical value for miscibility gaps, suggests that our prediction is not likely to change by including such contributions. Still, this is a point that deserves further investigation. A precise evaluation of vibrational and rotational contributions to the thermodynamics of mixing from MD simulations might become more affordable soon, thanks to progress in accurate machine-learned potentials, including on-the-fly learning schemes for MD [46, 47].

The stability of this solid solution results from the simultaneous mixing in the cation and halide sites. Both substitutions impact the thermodynamic stability (free energy of mixing) through enthalpic and entropic contributions. In terms of the entropy (eq. 5), clearly the halide mixing has the strongest effect, because it contributes 3 mixed sites per formula unit, whereas the cation mixing only contributes one mixed site per formula unit. But the thermodynamic stability of mixed-cation mixed-halide perovskites is not only due to entropy effects, but also to enthalpy contributions. There are known instabilities in the mixed-halide perovskites MAPb(I_xBr_{1-x})₃ and FAPb(I_xBr_{1-x})₃, especially segregation into Br-rich and I-rich phases upon exposure to light [5]. In fact, the strategy of two-cation and three-cation mixing was devised as an alternative to improve the stability [9, 48]. Furthermore, cation substitution (*e.g.* of cesium or lighter alkaline dopants) enhances perovskite nucleation and growth, crystal quality, and suppresses ion migration. These

parameters are relevant for solar cell durability, although they are not directly linked with thermodynamical stability [49].

Electronic structure

To compare the energy spectra of the two pure compounds and the solid solution, the energy scales must be aligned with a well-defined procedure. The electron energy zero in VASP calculations is the average electrostatic potential, which includes the local part of the PAW potentials. As the three compounds have different compositions, the energy scales have different references. To put the electronic structures in the same reference, we have applied constant shifts to the electron energies of $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$ and MAPbBr_3 so that the Pb core levels are aligned.

Table 1 shows the average electrostatic potential (times the electron charge) computed in small spheres around the Pb nuclei. The fluctuations of this potential mimic the variations of core-level shifts with the atomic environment [50]. **Table 1** shows the mean values and the standard deviation of the sphere-averaged potentials. For the mixture $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$ these parameters were calculated separately as a function of the number of Br atoms in the corners of the $\text{PbI}_{6-n}\text{Br}_n$ octahedra. The variation between octahedra with 0 and 3 Br, is 0.20 eV, while the standard deviation of the full set of Pb is similar to the one in the pure compounds. This suggests that core-level measurements (say, using X-ray photoemission spectroscopy) would not show increased broadening of Pb core levels compared to the pure compounds, and therefore that the Pb core levels can be regarded as a common energy reference for the alloy and the pure compounds. For the Pb core levels to be aligned in the three compounds, the energy scales must be shifted by 0.12 eV and 1.00 eV for $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$ and MAPbBr_3 , respectively. The same shifts modify all single-electron energies and have been applied in the DOS plots.

Table 1. Average electrostatic potential in spheres around Pb atoms in the studied compounds. The correction energy is the shift required to align the Pb core levels in the three compounds.

Average electrostatic potential	Pb	Mean (eV)	Std. dev. (eV)	Correction (eV)
$(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$	PbI_6	-45.97	0.15	
	PbI_5Br	-46.05	0.14	
	PbI_4Br_2	-46.09	0.16	
	PbI_3Br_3	-46.17	0.20	
	Pb_{all}	-46.04	0.16	0.12
FAPbI_3	Pb_{all}	-45.92	0.16	0
MAPbBr_3	Pb_{all}	-46.92	0.18	1.00

The valence band maximum (VBM) of each compound has been determined as the average energy of the higher occupied crystal orbital (HOCO), taken from a subset of 70 configurations of the MD ensembles, separated by 250 fs. **Figure 7** shows the distribution of the HOCO energies for the three compounds. The energy dispersion has been computed at PBE-SOC level. The same procedure has been applied to obtain the conduction band minimum (CBM) as the average of the lowest unoccupied crystal orbitals (LUCO). Moreover, for each compound we have identified one configuration that have the HOCO and LUCO energies very close to the average VBM and CBM. For these special (selected) configurations (see coordinates in ESI) we have calculated the electronic structure using the hybrid functional PBE0(0.188)-SOC, as well as with PBE-SOC. From these calculations with the representative configurations, the differences between PBE0(0.188)-SOC and PBE-SOC have been computed for the VBM and the CBM and have been applied as corrections to the set of HOCO and LUCO energies in **Figure 7**. Also **Figure S6** in the ESI shows the DOS for the mixed perovskite and the pure compounds, computed with the PBE functional. Each plot includes the DOS of the special configuration. All energies are referred to the VBM of FAPbI₃, which is defined as the average HOCO, as explained above. The energy scales of (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125} and MAPbBr₃ are shifted to align the average Pb core level energies with that in FAPbI₃. As the PBE functional is well known to underestimate the bandgap, the electronic structure of the selected representative configuration of each compound was recalculated with the hybrid functional PBE0(0.188)-SOC. The DOS and partial DOS calculated with this functional are shown in **Figure 8**, and in **Figure S7** of the ESI.

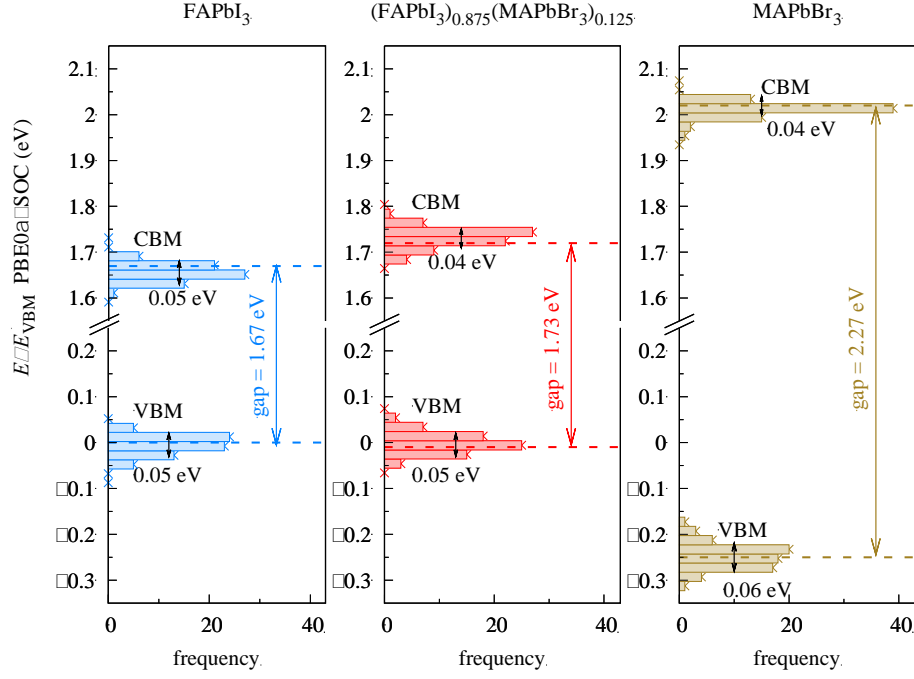


Figure 7. Distribution of energy levels of the mixture and the pure compounds at hybrid PBE0($\alpha = 0.188$)-SOC. E_{VBM}^* is the VBM state energy of the FAPbI₃ selected configuration. The dashed lines represent the energies of the VBM and CBM states for each selected configuration, and the corresponding gap is included. The black double arrows indicate FWHM, the values are added for each distribution.

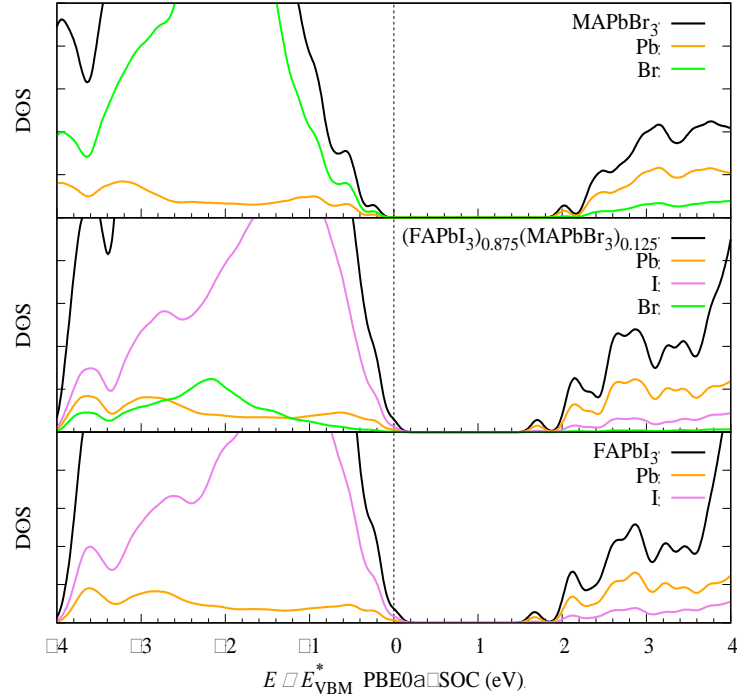


Figure 8. DOS and partial DOS of the solid solution and the pure compounds computed at hybrid PBE0($\alpha = 0.188$)-SOC. E_{VBM}^* is the VBM state energy of the FAPbI₃ selected configuration. The energy scales of (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125} and MAPbBr₃ are shifted to align the average Pb core level energies with those in FAPbI₃.

With the same approach, the imaginary part of the dielectric function was computed, which is shown in **Figure S8**. The dielectric function was computed within the random phase approximation (RPA), with the longitudinal gauge, and using only the gamma point wavefunctions. One shortcoming of the RPA is that it cannot account for exciton effects. Moreover, the rough k-point sampling that we can afford in the calculation of the dielectric function does not allow comparing the theoretical and experimental dielectric functions. However, the theoretical calculation allows us to confirm that the VBM to CBM transitions are dipole allowed. Therefore, one can conclude that the optical gaps almost coincide with the bandgaps so long as exciton binding energies are negligible.

Table 2 shows the theoretical bandgaps, computed with both hybrid functionals, as well as the experimental optical gaps. The experimental optical gaps of FAPbI_3 and $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$ were obtained by means of the Tauc's plots, shown in **Figure S9**, as well as from the literature. It is apparent that the PBE0(0.188)-SOC method provides a band gap in better agreement with the experimental optical gaps than HSE06-SOC. Let us recall that the mixing fraction 0.188 was obtained for MAPbI_3 [25], therefore it is not expected to work so well for different compositions, but it is still more accurate than the standard HSE06-SOC for these HOIHP perovskites. Moreover, both functionals reproduce well the trend that the gap of the mixture is 0.06 eV larger than the gap of FAPbI_3 .

The theoretical bandgaps of $(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$ shown in **Table 2** are close to the values predicted by the Vegard law, 1.75 eV or 1.43 eV with PBE0(0.188)-SOC or HSE06-SOC, respectively. This is consistent with experimental data summarized by the equation:

$$E_g(x, y)/\text{eV} = 1.58 + 0.436x - 0.058y + 0.294x^2 + 0.0199xy, \quad (7)$$

where the non-linear term for $x = 1 - y = 0.125$ contributes only 4 meV. Eq. (7) was obtained by Jacobsson *et al.* [51], by fitting the data of 49 synthesized mixtures spanning the compositional space of $\text{FA}_y\text{MA}_{1-y}\text{Pb}(\text{I}_{1-x}\text{Br}_x)_3$.

Table 2. Comparison of experimental and theoretical gaps.

Compound	Gap energy (eV)		
	Experimental (optical)	Theoretical (PBE0(0.188)-SOC)	Theoretical (HSE06-SOC)
FAPbI_3	1.53 ^a 1.52 ^b	1.67	1.35
$(\text{FAPbI}_3)_{0.875}(\text{MAPbBr}_3)_{0.125}$	1.59 ^b	1.73	1.41

(FAPbI ₃) _{0.85} (MAPbBr ₃) _{0.15}	1.58 ^a		
	1.61 ^b		
MAPbBr ₃	2.31 ^b	2.27	1.96

^a From Tauc's plots, **Figure S9**. ^b From Ono *et al.* [5, 51].

There is no significant difference in the imaginary part of the dielectric functions of FAPbI₃ and (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125}, as shown in **Figure S8** of the ESI. This is interesting because Brauer *et al.* [52] have recently reported a large difference in the measured attenuation coefficients of MAPbI₃ and (FAPbI₃)_{0.8}(MAPbBr₃)_{0.2}, the latter being much higher in the range 2.5-3.1 eV. They have correlated this feature with the increased carrier lifetime in the mixed perovskite. Based on our calculations, it seems that FAPbI₃ and (FAPbI₃)_{0.8}(MAPbBr₃)_{0.2} are similar in this respect.

It is known that the tilting of octahedra, as measured by the Pb-X-Pb angle deviation from 180°, and the variations of Pb-X bond lengths modify the overlap of metal s- and halide p-orbitals, and have an effect on the bandgap [53]. This has been experimentally verified by means of changing the organic cations [54]. Hence, it is interesting to investigate if this effect manifests in the dynamics of the mixed compound. From the MD simulation of (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125}, we have obtained the electronic structure, under the PBE-SOC approximation, for 70 instantaneous configurations. Each configuration has one bandgap that corresponds to a distribution of angles and a distribution of bond lengths. We can characterize these bond length and angle distributions by average values and standard deviations. We have added this information in **Figure S13** of ESI, observing that the instantaneous bandgaps correlate directly with the average Pb-X-Pb angle and inversely with the average Pb-X distance. The correlations are weak but the trend is clear and in line with the arguments made in previous work [54].

Conclusions

An atomic scale model of the random solution (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125} has been proposed. Several computed properties have been shown to reproduce available experimental measurements, such as bandgaps, lattice constant, cation orientation dynamics, and thermodynamic stability. Other physical properties are reported, including distance and angle distribution functions, vibrational and other dynamical properties, as well as the electronic structure. All these properties of the solid solution (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125} are compared with those of the end compounds MAPbBr₃ and FAPbI₃. Our MD simulations of (FAPbI₃)_{0.875}(MAPbBr₃)_{0.125} at 350 K, show a certain locking effect on the organic cations, leading to slower cation orientation dynamics in this solid solution compared with the pure compounds. Thermodynamic calculations suggest there is no miscibility gap for the

random alloying of MAPbBr₃ and FAPbI₃. Our model is therefore useful for the detailed understanding of the physical behaviour of this important material, accounting for both disorder and dynamic effects, and will allow future investigation of other bulk properties as well as of the behaviour of its surfaces and interfaces.

Author Contributions

This work was conceived by EMP, KTB and RGC. The SQS model was designed by RGC and EMP. MD simulations were made by SDM, SG and EMP. Analysis of the MD was done by SG, ALMA, and EMP. The electronic structure calculations were done by ALMA. The thermodynamic analysis was done by SG and RGC. Most of the pictures were composed by SG and ALMA. All authors contributed to the interpretation and discussion of the results. The first draft was written by EMP and RGC. All authors contributed to the final manuscript.

Conflicts of interest

There are no conflicts to declare.

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