Analysis of the influence of the wind speed profile on wind power production


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Analysis of the influence of the wind speed profile on wind power production

C.A. Lopez-Villalobos, O. Martínez-Alvarado, O. Rodríguez-Hernandez, R. Romero-Centeno

1. Introduction

The economic viability of wind power projects depends on the site's wind conditions since the wind farm's energy production has to compensate for the installation and maintenance cost. A reliable assessment of the wind resource is crucial to manage existing wind farms and evaluate the viability of future ones (Serban et al., 2020; Gormo et al., 2021). Therefore, modelling the vertical structure of the surface layer flow is required, especially the vertical wind speed profile, e.g., to extrapolate wind speed measurements performed at lower altitudes to the wind turbine's hub height. The wind shear magnitude is site-specific and depends on wind direction, wind speed, atmospheric stability, surface roughness, complexity of the terrain, and other atmospheric phenomena. Complex land areas are characterized for high shear and turbulence levels in the wind flow, although this could increase the wind turbine power and load fluctuations (Schulz et al., 2014). Complex terrains are usually avoided because of the more severe wind conditions but are becoming more appealing for the wind industry (Alfredsson and Segalini, 2017).

Vertical variation of wind speed is an important parameter for wind turbine design, especially for those with large diameter rotors. Several theoretical and empirical models have been developed to describe wind speed vertical distribution across the atmospheric boundary layer (Gualtieri, 2019a). Here, we use a logarithmic model and a power-law method. The wind speed profile is commonly described by a logarithmic profile valid close to the surface (diabatic surface layer wind profiles), modified by the Monin–Obukhov similarity theory (MOST) for thermal stability. In an ideal horizontally homogeneous terrain where the atmosphere is in a steady state, the surface layer turbulence properties are sufficiently approximated by the MOST (Obukhov, 1971; Monin and Obukhov, 1959). The similarity theory assumes that normalized variances and covariances of various atmospheric surface layer parameters are universal functions of a stability parameter governed by the Obukhov length. MOST agrees with measured data at least up to 100 m (Holtslag, 1984). According to the MOST, the profiles of wind and air temperature in the turbulent surface layer could be described by a set of equations.
that depends only on a few parameters, including the surface roughness length $z_0$ (Kalnay, 2003). The surface roughness and the different atmospheric stability conditions greatly influence the vertical profile of winds. They must be taken into account in the estimation of the vertical wind profile (Radińcz et al., 2020; Zhan et al., 2020; Chanprasert et al., 2020; Du et al., 2021). Wind speed and air temperature measurements at different heights can be used to derive the Monin–Obukhov length $L$ via the Richardson number (Holtslag et al., 2014; Donnou et al., 2019; Holtslag et al., 2020). The Monin–Obukhov length $L$ has to be derived from measurements at the site. The power-law method is one of the most used tools for extrapolating wind speed in the vertical direction. The power law is empirical and commonly used in wind engineering to define vertical wind profiles because it is simple and ready to use (Lopez-Villalobos et al., 2018; IEC61400-1, 2005; IEC61400-2, 2013). It describes the degree of atmospheric stability by means of the wind shear exponent, which indicates the amount of stratified flow, but it is not a direct measure of stability.

Surface layer turbulence properties over complex terrain are not satisfactorily understood despite several relevant studies (Martins et al., 2009; Rotach and Zardi, 2007; Moraes et al., 2005; Rotach et al., 2004; Nadeau et al., 2013; Tampieri, 2017; Serafin et al., 2018). Thus, there is still no consensus regarding the functional forms of MOST relationships or the limitations of this theory (Lee and Buban, 2020). Applications over flat sites are more frequent than elsewhere and implementation over complex terrains sites is generally more challenging because they can significantly affect the shear profile (Gualtieri, 2019b). As the air flows over complex terrains, changes occur to the mean and turbulent components of the flow which may result in a decrease or increase in wind shear, or even occurrences of negative wind shear (Wharton et al., 2015). Flow in the roughness sublayer (e.g. flow over vegetative canopies) resembled a turbulent mixing layer (Raupach et al., 1996), formed around the inflectional mean velocity profile, which develops between two coflowing streams of different velocities, differs in several ways from turbulence in a surface layer.

In addition to the aforementioned, wind speed profiling is useful for the development of wind resource atlases (Ouammi et al., 2010; Elliott et al., 1987; Archer and Jacobson, 2003), estimation of shear impacts on wind turbine loading and failures (Smith et al., 2002; Lopez-Villalobos et al., 2018), and wind farm layout optimization (Vasel-Be-HaghandArcher, 2017; Roque et al., 2020; Gualtieri, 2017).

Given that wind speed profiles depend on atmospheric stability, this should not be assumed as constant throughout the day and year because this profile is used to assess the wind power production and wind turbine rotor loads (Lopez-Villalobos et al., 2018; Han et al., 2018). Some studies have been carried out to assess the impact of the atmospheric stability on resource assessment and wind turbine aerodynamic performance, and fatigue loads, e.g. Holtslag et al. (2014), Sathe and Bierbooms (2007), Rehman et al. (2018) and Sathe et al. (2013) showed the significance of atmospheric stability on wind turbine power production as well as on wind turbine loads, where it is directly caused by the influence of the underlying atmospheric stability on both wind shear and turbulence properties. Moreover, there are studies that indicate that blade loads were hardly affected by atmospheric stability (Kretschmer et al., 2018).

In this work, the characteristics of the vertical variation of wind speed are analysed within the limit of the surface boundary layer, where some of the most important variables are: friction velocity, momentum and energy fluxes, and surface roughness. Therefore, we can neglect the Coriolis parameter, baroclinity, wind shear, and entrainment processes near the top of the boundary layer. The effect of the wind speed vertical profile in the wind resource assessment at La Ventosa, Oaxaca, Mexico. This region is of special interest. It concentrates the greatest wind potential in Oaxaca due to the strong mountain gap wind travelling through the Chivela Pass into the eastern Pacific coast in southern Mexico, most commonly between October and February (Hong et al., 2018). We explore if the Monin–Obukhov similarity theory is suitable to describe the vertical wind speed within the surface boundary layer at the test site. Moreover, it is analysed the default International Electrotechnical Commission (IEC) (IEC61400-1, 2005; IEC61400-2, 2013) standard value and variable power-law method.

Furthermore, we study how the vertical wind profile influences wind power production in the rotor swept area using the rotor equivalent wind speed definition (Wagner et al., 2011; Commission et al., 2005), which it takes into account that the wind speed at hub height does not represent the wind speed at the lowest and upper part of a large-scale wind turbine rotor (European Wind Energy Association and others, 2012; Wharton and Lundquist, 2012).
2. Data and methods

2.1. Measurement site

Mexico has a large and diverse renewable energy resource such as solar, wind, biomass, hydropower and geothermal. Among these, wind power is one of the most efficient and developed energy sources (Thakur et al., 2016). Mexico is the second-largest wind power producer in Latin America after Brazil, with a total installed capacity of 6789 MW at the end of 2020 (GWEC, Global Wind Energy Council, 2020).

Figs. 1(a) and 1(b) show the measurement site at La Ventosa, Oaxaca in the Tehuantepec Isthmus region, Mexico. La Ventosa concentrates 33% of the country’s total installed capacity of the country (GWEC, Global Wind Energy Council, 2020). The windy Isthmus region is relatively flat, and the maximum resource generally occurs from late morning to afternoon. However, during the windiest months (November through February), the wind resource is sometimes slightly greater at night than during the day (Lopez-Villalobos et al., 2021; Elliott et al., 2003). This suggests that effects related to the boundary layer stability are at play during these months.

Near the test site, to the north, is La Ventosa city, and there are some wind farms surrounding the area. La Ventosa region has been the subject of several studies to determine the region’s wind characteristics (Cadenas and Rivera, 2007; Jaramillo and Borja, 2004; Lopez-Villalobos et al., 2018, 2021). It is known that the frequency distribution of wind speed is bimodal, a feature that is closely related to the wind direction, with northerly winter winds being stronger (Romero-Centeno et al., 2003; Jaramillo and Borja, 2004). Furthermore, the reliability of the IEC61400’s Normal Turbulence Model (NTM) for fatigue load design parameter (IEC61400-1, 2005; IEC61400-2, 2013) is proven to be unsuitable for the location due to present greater wind dispersion than the standard NTM reported (Lopez-Villalobos et al., 2018). A power spectrum analysis has been conducted in the region and found a spectral gap and a microscale region with similar variance, allowing the use of mean-times from 6 h to 1 min with no significant difference in the wind resource assessment results (Lopez-Villalobos et al., 2021).

2.2. Data processing

Measurements from an 80 m high anemometric mast located at the Centro Regional de Tecnología Eólica (CERTE, shown in Fig. 1(b)) in La Ventosa, Oaxaca (16°32′49.8″ N, 94°57′20.83″ W) were used. These data were provided by the Mexican Wind Atlas (AEM, by its acronym in Spanish), funded by the United Nations Development Programme Global Environmental Finance (UNDP-GEF) unit and implemented by Mexico’s Instituto Nacional de Electricidad y Energías Limpias (INEEL). The horizontal wind speed and direction were measured at four heights: 80, 60, 40, and 20 m. In addition, measurements of air temperature at 15 and 40 m and pressure at 15 m were used. The data were averaged and saved every 10 min from December 1st of 2017 to December 1st of 2018.

Virtual and potential air temperature need to be estimated to carry out the atmospheric stability analysis from the AEM measurements. Therefore, the potential air temperature was estimated as \( \theta_v = \theta \left( \frac{P_0}{P} \right)^{0.286} \), where \( P_0 = 1000 \text{ hPa} \) is the atmospheric reference pressure, and \( P \) is the air pressure. The virtual potential air temperature was calculated as \( \theta_v = \theta (1 + 0.6r) \), where \( r \) is the mixing ratio for unsaturated air. We calculated \( r \) using the relative humidity measured at the site, following the methodology described in Bolton (1980).
To extrapolate the wind speed vertically, we need to estimate the Richardson stability parameter, which is proportional to the height above the surface at which buoyant factors dominate over mechanical production of turbulence (Stull, 1988). Virtual potential air temperature is analogous to potential air temperature in the sense that they both remove the air temperature variation caused by pressure changes of an air parcel. Thus, we can compare air parcels at different elevations to determine which one is warmer or cooler when brought to the same height. It is also a helpful quantity because it takes moisture and air temperature into account when considering buoyancy and stability. So, we can analyse virtual air temperature variations instead of variations in density.

2.3. Vertical velocity profile and atmospheric stability

The variation of wind speed with height in the surface boundary layer is typically well described by a logarithmic relationship between surface stress (represented by the friction velocity, \( u_f \)) and surface roughness (represented by the aerodynamic roughness length, \( z_0 \)). In the present work, the wind profile in non-neutral conditions, which integrates the Businger–Dyer relationships (Dyer, 1974; Businger et al., 1971), is estimated by

\[
u = \left(\frac{u_f}{k}\right) \ln \left(\frac{(z-d)}{z_0}\right) - \psi_m(\zeta_m).
\]

(1)

where \( k \) is the Von Karman constant (0.4), \( z \) is the vertical height, \( d \) is the zero plane displacement (\( d = 0 \) for bare soil surfaces (Garratt and Hicks, 1973) which is the case in the present study), \( z_0 \) is the surface roughness, \( u_f \) is the friction velocity, and \( \psi_m \) is a stability correction function which depends on the ratio \( \zeta_m = (z-d)/L \) where \( L \) is the Obukhov length. The friction velocity is defined as \( u_f = k\Delta U/\phi_m \ln(z_2/z_1) \), where \( \phi_m \) is a Monin–Obukhov stability correction function also known as the dimensionless wind shear, \( z_2 \) and \( z_1 \) correspond to the heights of available measurements (in our case 40 and 15 m, respectively), and \( \Delta U \) is the change in horizontal wind speed at these heights.

The Richardson number, \( R_i = \frac{g \Delta \theta}{\beta (\Delta U)^2} \ln \left(\frac{z_2}{z_1}\right) \), serves as an indicator of forced and free convection instability mechanisms (Arya, 2001), where \( \Delta \theta \) is the virtual potential air temperature difference at two different heights, \( T_0 \) corresponds to the absolute air temperature at height \( z_1 \), \( g \) is the acceleration due to gravity, \( z_m = (z_2z_1)^{1/2} \) is the geometric mean height. Richardson number is useful to classify the atmosphere in the surface layer as unstable, neutral, and stable. Negative \( R_i \) values indicate that convection predominates, winds are weak, and a strong vertical motion is characteristic of an unstable atmosphere, while for positive values lower than 0.2, the atmosphere is stable (Arya, 2001; Stull, 1988).

The \( \phi_m \) and \( \psi_m(\zeta_m) \) stability functions have been empirically determined in various studies (Businger et al., 1971; Deardorff, 1972; Nickerson and Smiley, 1975). The corresponding value of the stability parameter \( \zeta_m = z_m/L \) can be determined from (Zilitinkevich and Calanca, 2000; Newman and Klein, 2014)

\[
\zeta_m = \begin{cases} 
\frac{R_i}{1 - \beta R_i}, & 0 \leq R_i < 0.2, \\
1 - \beta R_i, & R_i \geq 0.
\end{cases} 
\]

(2)

Knowing \( \zeta_m \), \( \phi_m \) is determined as

\[
\phi_m = \begin{cases} 
(1 - \gamma \zeta_m)^{-1/4}, & \zeta_m < 0, \\
1 + \beta \zeta_m, & \zeta_m \geq 0.
\end{cases} 
\]

(3)

and \( \psi_m(\zeta_m) \) is determined as

\[
\psi_m(\zeta_m) = \begin{cases} 
-\beta \zeta_m, & \zeta_m > 0, \\
\ln \left(\frac{1 + x^2}{2} \right) - \ln \left(\frac{1 + (1 + x)^2}{2} \right) - 2 \tan^{-1}(x), & \zeta_m < 0.
\end{cases} 
\]

(4)

where \( x = (1 - \gamma \zeta_m)^{1/4} \). In the Eqs. (2) to (4), \( \gamma \) and \( \beta \) are coefficients determined using nonlinear least-squares best fits applied to observations (Dyer and Hicks, 1970; Dyer, 1974; Högström, 1996; Maronga and Reuder, 2017). The values of these coefficients have been extensively debated in the past literature. Although 4.7 is commonly accepted for \( \beta \) (Irwin, 1979; Businger et al., 1971; Deardorff, 1972; Zoumakis and Keleissis, 1991), a value of 5 is also frequently used (Zannetti, 2013; Garratt and Hicks, 1990). For \( \gamma \), a value of 16 was proposed (Garratt and Hicks, 1990; Holtslag, 1984), although 15 is also recommended (Businger et al., 1971; Deardorff, 1972; Nickerson and Smiley, 1975). However, we note that those equations are not the only possible formulations, and we refer the reader to Optis et al. (2016) and Foken (2006) to discuss alternative forms of these relationships. In the current work, the values of \( \beta = 5 \) and \( \gamma = 15 \) were set.

Despite the limitations of the logarithmic wind speed profile in stable conditions, it is still frequently used under these conditions for wind power resource assessment and forecasting at altitudes within a few hundred metres of the surface. Over the last two decades, it has been used extensively in wind power meteorology (Petersen et al., 1998; Burton et al., 2011; Lange and Focken, 2006; Motta et al., 2005; Van den Berg, 2008; Emeis, 2010, 2018; Giebel et al., 2011; Brechsl et al., 2012). For wind power forecasting, in particular, the logarithmic wind speed profile has been used to interpolate wind speeds between two numerical weather prediction model levels to hub height, extrapolate observed wind speeds to hub height, or extrapolate the geostrophic winds to hub height using the friction velocity computed from the geostrophic drag law (Tennekes, 1973).

An alternative approach is given by the power-law method. This is a well-known engineering method commonly used to vertically extrapolate wind speed. The equation is written as \( u(z) = u_r (z/z_r)^{\alpha} \) where \( \alpha \) is the wind shear exponent, commonly assumed to be \( \alpha = 1/7 \approx 0.143 \) for neutral atmospheric stability as recommended by the IEC61400 standard (IEC61400-2, 2013), \( u_r \) and \( z_r \) are the reference wind speed and height, respectively, and \( z \) is the height to which wind speed is to be extrapolated. A fixed wind shear coefficient may, in some cases, result in under or overestimation of wind speeds and wind power production (Firtin et al., 2011; Rehman et al., 2013; Schwartz and Elliott, 2006). There are efforts to modify the standard power-law methodology to improve the prediction of wind speeds at higher heights; however, in many cases, a fixed wind shear coefficient is used based on long-term average time series wind data (Corscadden et al., 2016; Gualtieri, 2016). A constant wind shear coefficient is a factor that contributes to increasing uncertainty in wind speed extrapolation whilst using a variable wind shear coefficient provides a more accurate estimate of wind speed at hub height (Gualtieri, 2016; Đurišić and Mikušić, 2012).

2.4. Wind power resource assessment

In wind power projects, it is essential to determine the wind energy potential of a specific site. Then, the wind power production is estimated using a ten-minute wind speed time series and a wind turbine power curve. In this study, the Vestas V90-2MW wind turbine power curve was used (Fig. 2), corresponding to a
three-bladed upwind horizontal axis wind turbine. The V90-2MW has a rotor diameter of 90 m, with rotor blades of 44 m long, and a hub height of 80 m above surface level (Vestas, 2015). It starts producing electric power at a wind speed of 3 m/s, which is the power production cutoff windspeed for nominal power output of 2 MW at 13.5 m/s, and the survival wind speed is 25 m/s, which is the power production cutoff wind speed (pitch power control).

The mean energy production of a wind turbine, $P_T$, for a given time series with $N$ data points, is defined as (Manwell et al., 2010):

$$P_T = \frac{1}{N} \sum_{j=1}^{N} P_j(V_{eq}(t_j)),$$

where $P_j$ is the wind turbine power production as a function of the rotor equivalent wind speed, $V_{eq}(t) > 0$. The rotor equivalent wind speed is the wind speed corresponding to the kinetic energy flux through the swept rotor area, when accounting for the vertical shear (Wagner et al., 2014). The simplest model for $V_{eq}$ accounts for only the windspeed shear and does so by dividing the turbine’s rotor disk into discrete vertical layers, as follows:

$$V_{eq}(t) = \left( \sum_i u_i^2(t) \frac{A_i}{A} \right)^{1/3},$$

where $A$ represents the area swept out by the rotor disk, $A_i$ the area of a discretized section of the rotor disk (as shown in Fig. 3), and $u_i$ is the wind speed measured in the given section. The section area ratios are defined as follows: $A_1/A = 0.125$, $A_2/A = 0.25$, $A_3/A = 0.25$, and $A_4/A = 0.125$. From Fig. 3, the hub height is 80 m above ground level, and the wind turbine rotor radius is 45 m.

3. Results

3.1. Atmospheric stability

The vertical variation of the hourly mean virtual potential air temperature and its spread (25 and 75th percentile values) throughout the year is shown in Fig. 4. It is important to mention that the local time (LT) corresponds to GMT-6 and we will use LT instead. Throughout the year, the mean virtual air temperature starts increasing around 07:00 h, reaching a maximum value around 14:00–15:00 h, and then it starts to decrease slowly, showing a net radiative loss of energy from the surface during night time. The seasonal behaviour of the hourly virtual potential air temperature shows higher values during spring and summer (Figs. 4(a), 4(b)). It is interesting to note the variation of the spread throughout the year, with higher spread during autumn and winter than during summer. Moreover, Fig. 4 shows, consistently for all seasons, a slight increase of temperature with height occurring mainly between 20:00 h to 06:00 h, called inversion. The most common inversion is radiational inversion, which happens due to the radiational cooling of the earth’s surface. Because of the longwave radiation to space, the earth is cooled at night. The inversion is maximized on clear nights with light wind and dry air, but it generally erodes rapidly once daytime heating warms the lower planetary boundary layer.

Fig. 5 shows the seasonal differences of the hourly mean virtual potential air temperature at both heights, which we define as $\partial \theta / \partial z \approx \Delta \theta / \Delta z = (\theta(z_2) - \theta(z_1))/(z_2 - z_1)$, where $z_2 > z_1$. The criteria for static stability is then based on the sign of this gradient (Arya, 2001). If $\partial \theta / \partial z > 0$ corresponds to a stable stratification, otherwise is unstable. The greater differences are found in spring from 00:00 to 06:00 h during stable condition and in summer from 19:00 to 23:00 h.

Fig. 6 shows the hourly mean friction velocity values, which represent the intensity of the turbulent movement of the air masses on the surface due to the roughness present at the site. The general behaviour of the friction velocity shows a diurnal variability, similar to the potential air temperature, which is expected due to the forcing occurring in the atmospheric boundary layer by solar heating. $u_*$ typically varies daily with low $u_*$ during calm nights (calm winds) ($u_* = 0$) and high $u_*$ during daytime (strong winds) ($u_* = 1$ m/s). Moderate wind values are often near $u_* = 0.5$ m/s, which might be related to moderate mean friction velocity values during the spring and summer (from 0.35 to 0.5 m/s). High mean friction velocity values (from 0.5 to 0.75 m/s) for the winter and autumn are related to high wind speed mean values. The maximum values are found during the winter season, reaching a maximum mean value of 0.75 m/s at 16:00 h, which coincides with an unstable thermal static atmosphere. We found a lower mean value during spring and summer, where the lowest wind speed values of the year are found, around 0.33 m/s. Furthermore, the highest dispersion (Vertical lines) is observed.
Fig. 4. Seasonal variation of the hourly mean virtual potential air temperature: (a) spring (March–May 2018); (b) summer (June–August 2018); (c) autumn (September–November 2018), and (d) winter (December 2017, January–February 2018), for 15 m and 40 m height. The vertical lines go from the 25th to 75th percentile.

Fig. 5. Seasonal differences of the hourly mean virtual potential air temperatures between 40 and 15 m heights. The vertical lines go from the 25th to the 75th percentile.
in the winter and autumn seasons, which are the seasons with the highest wind speed shear. During the day, $u_*$ varies from 0.63 to 0.97 m/s throughout the seasons, where the maximum value occurs in winter and the minimum in spring. During the night, it varies from 0.51 to 0.79 m/s, where the maximum occurs in winter and the minimum in spring.

Fig. 7 shows the hourly mean seasonal behaviour throughout the day of the $\xi_m$ time series. The figure shows that there is a mixture of stable and unstable conditions; however, while the sun is heating the region’s surface (08:00 h to 17:00 h), unstable conditions dominate. The atmosphere is mostly unstable in all seasons, around 70% of the time.

### 3.2. Wind profile adjustment

The seasonal behaviour of $\psi_m(\xi_m)$ is displayed in Fig. 8. In general, it exhibits a diurnal pattern similar to $\xi_m$ but with the opposite sign, so that under unstable conditions $\psi_m(\xi_m)$ is positive while under stable conditions it is negative. Consequently, the velocity profiles in the surface layer are expected to become increasingly curvilinear as instability increases.

The wind shear exponent $\alpha = 1/7$ is recommended by the IEC61400 standard \cite{IEC61400-2} for neutral atmospheric conditions with values higher (lower) than 1/7 indicating stable (unstable) conditions \cite{Newman2014}. We used the power-law equation, $U_z = U_0 (Z/Z_r)^\alpha$, to estimate variable wind shear exponent as $\alpha = \ln(U_z/U_r) / \ln(Z/Z_r)$. Here, $U_0$ and $U_r$ are equal to the wind speed time series measured at $Z_z = 80$ m and $Z_r = 20$ m, respectively. Fig. 9 shows the seasonal variability of the hourly mean wind shear exponent. During the day, the mean $\alpha$ values range between 0.12 and 0.20 indicating almost neutral atmospheric conditions. During the night, the $\alpha$ values range between 0.20 to 0.25, which indicates stable atmospheric conditions.

Until now, we do not have information about the roughness length $z_0$, but we can estimate it using the known variables. We can estimate the variability of $z_0$ from data by obtaining seasonal roughness values. To estimate $z_0$, we use a least-square fitting to the AEM measurements. Table 1 shows the variability of $z_0$ ranging from 0.20 to 1.15 m, which is reported in the literature as farmland terrain that matches the type of terrain of the site.

Table 1 summarizes the seasonal and diurnal mean values of $u_*$, $\psi_m(\xi_m)$, $z_0$ and $\alpha$. The latter, during day, is close to the IEC neutral atmospheric stability recommendation, but during night, is larger than recommendation, mostly during stable atmospheric conditions. These variables are used as input to vertically extrapolate the wind speed.

The seasonal wind speed profiles during the day and night are shown in Figs. 10 and 11, respectively. During the day, in
Fig. 7. Frequency distribution of hourly stability data by season: (7a) spring, (7b) summer, (7c) autumn, (7d) winter, based on the Obukhov length time series at $z_0 = (z_2 - z_1)^{1/2} = 24.5$ m above the surface. $z_1$ and $z_2$ correspond to 15 and 40 m, respectively.

Table 1
Summary of the vertical profile variables used in the log-law and power law equations, according to the season of the year and daytime conditions.

<table>
<thead>
<tr>
<th>Season</th>
<th>Variables</th>
<th>$u_*$</th>
<th>$\psi_m (z_0)$</th>
<th>$z_0$</th>
<th>$\alpha$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spring</td>
<td>Daylight</td>
<td>0.63</td>
<td>0.78</td>
<td>0.20</td>
<td>0.14</td>
</tr>
<tr>
<td></td>
<td>Night</td>
<td>0.51</td>
<td>-0.98</td>
<td>1.05</td>
<td>0.22</td>
</tr>
<tr>
<td>Summer</td>
<td>Daylight</td>
<td>0.68</td>
<td>0.43</td>
<td>0.30</td>
<td>0.15</td>
</tr>
<tr>
<td></td>
<td>Night</td>
<td>0.52</td>
<td>-1.06</td>
<td>0.87</td>
<td>0.22</td>
</tr>
<tr>
<td>Autumn</td>
<td>Daylight</td>
<td>0.87</td>
<td>0.21</td>
<td>0.38</td>
<td>0.17</td>
</tr>
<tr>
<td></td>
<td>Night</td>
<td>0.68</td>
<td>-1.45</td>
<td>1.15</td>
<td>0.22</td>
</tr>
<tr>
<td>Winter</td>
<td>Daylight</td>
<td>0.97</td>
<td>0.50</td>
<td>0.22</td>
<td>0.16</td>
</tr>
<tr>
<td></td>
<td>Night</td>
<td>0.79</td>
<td>-0.45</td>
<td>0.38</td>
<td>0.21</td>
</tr>
</tbody>
</table>

Fig. 10, the mean values generally show a good fit, although, for autumn and winter seasons, the estimation using the default value ($\alpha = 1/7$) tends to deviate more from the mean values above 20 m height. In Fig. 11, the estimations obtained using the default wind shear exponent deviates from mean values during the stable atmospheric condition at night. Moreover, for the log-law model, the estimations deviate from the mean values at 20 and 80 m height. Additionally, the variable wind shear method predicts the tendency of the AEM mean values. Now, we will compare the wind speed profiling methods against the AEM measurements. We will use the index of agreement defined as $\text{IOA} = 1 - \frac{\sum_{i=1}^{n} (P_i - O_i)^2}{\sum_{i=1}^{n} (|P_i - O_i| + |O_i - \bar{O}|)^2}$, which is a standardized measure of the degree of model prediction error and varies between 0 and 1. A value of 1 indicates a perfect match, and 0 indicates no agreement at all (Willmott, 1981). The IOA is shown in Table 2 of the power-law and log-law methods compared against AEM dataset. In the columns are shown, diurnally, the seasonal mean variable wind shear exponent and using a default value of 1/7. In general, there is a good general agreement with the AEM dataset. The log-law and the variable wind shear exponent power-law method has a IOA values closely 1.0. Moreover, the power-law adjustment using $\alpha = 1/7$ has a good agreement, but throughout the year shows the lowest IOA values amongst all adjustment. The latter is because, during the night, the wind speed is greater than predicted by the model. We can say that stable atmospheric conditions is expected to present higher wind speed than neutral atmospheric conditions.

3.3. Effects of vertical wind shear in wind power production

In this section, we assess the influence of using the different wind speed extrapolation methods in the wind resource assessment for a whole year. Seasonal mean $\psi_m$ value and seasonal $u_*$
time series were used to calculate the wind power production (Eq. (5)). The reference value of 20 m of the AEM measurement was used as an input of the power-law (IEC standard and seasonal variable wind shear value) and log-law method to extrapolate to 42.5, 60, 80, 100 and 117.5 m.

Fig. 8. Seasonal variation of the hourly mean stability function correction: (a) spring (March–May 2018); (b) summer (June–August 2018); (c) autumn (September–November 2018), and (d) winter (December 2017, January–February 2018) at 24.5 m above the surface. $z_1$ and $z_2$ correspond to 15 and 40 m, respectively. The vertical lines go from the 25th to 75th percentile.

Fig. 9. Seasonal variation of the hourly mean wind shear exponent ($\alpha$) between 80 and 20 m heights. The vertical lines go from the 25th to 75th percentile.

Fig. 12 shows the mean power output $P_T(V_{eq})$ using the equivalent wind speed determined from the log-law and power-law ($\alpha = 1/7$ and variable $\alpha$) method. We will use the variable wind shear exponent method as a reference value because it has demonstrated good agreement against AEM measurements.
Fig. 10. Vertical wind speed profiles from different adjustments to the AEM measurements during daylight for (a) spring, (b) summer, (c) autumn, and (d) winter seasons. The blue dashed line (---) represents the profile estimated from the variable wind shear exponent of the power-law equation. The green dashed line (-----) corresponds the profile estimated from the power-law considering $\alpha = 1/7$, which is the IEC61400 standard recommendation. The red dashed line (----) represents the profile obtained using the log-law equation. The black solid markers (■■■) represent the mean values from the AEM measurements, and error bars (horizontal lines) go from the 25th to the 75th percentile. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Table 2

<table>
<thead>
<tr>
<th>Season</th>
<th>Index of agreement of wind speed profiling adjustment methods: Power law (P.l), Log-law (L-l).</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>P.l (variable)</td>
</tr>
<tr>
<td>Spring day</td>
<td>0.99</td>
</tr>
<tr>
<td>Spring night</td>
<td>0.99</td>
</tr>
<tr>
<td>Summer day</td>
<td>0.98</td>
</tr>
<tr>
<td>Summer night</td>
<td>0.99</td>
</tr>
<tr>
<td>Autumn day</td>
<td>0.99</td>
</tr>
<tr>
<td>Autumn night</td>
<td>0.99</td>
</tr>
<tr>
<td>Winter day</td>
<td>0.99</td>
</tr>
<tr>
<td>Winter night</td>
<td>0.99</td>
</tr>
</tbody>
</table>

In general, $P_T(V_{eq})$ has a seasonal and diurnal dependency, reaching a maximum during daylight in winter. The $\alpha = 1/7$ underpredicts a maximum of 13% less mean power output during the night, although during winter and spring, where the $\alpha$ value is nearly 1/7, there is an over-prediction of 0.6% more mean power output. These results suggest that the IEC standard might be suitable for estimating wind resources if the only data available is wind speed at one height. However, the wind resource should be expected to be underestimated by about 12%.

Table 3 shows the mean power production using the AEM measurements at hub height (80 m) and using variable $\alpha$ and log-law method of extrapolation to the same height. The percentage error is greater for the log-law method, with an over-prediction of 9% for the extrapolated hub height wind speed. The method that best approached against AEM mean power prediction at hub height (80 m) was the variable wind shear exponent method, with a percentage error difference close to zero. Therefore, we recommend using the variable power-law method to estimate wind energy production based on the present results.

The power production difference between equivalent wind speed and hub height wind speed is assessed between AEM measurement at hub height (80 m) and the variable wind shear method. The latter is because the variable wind shear method has shown good agreement against AEM measurements. From Fig. 12 and Table 3 a maximum percentage error at night is shown during spring and summer seasons (1.6 and 1.3%, respectively) and a minimum error at daylight during winter season (0.2%). Although, there is, on average, 0.9% more power production if the wind shear is considered employing equivalent wind speed.
Fig. 11. Vertical wind speed profiles from different adjustments to the AEM measurements at night for: (a) spring, (b) summer, (c) autumn, and (d) winter seasons. The blue dashed line (---) represents the profile estimated from the variable wind shear exponent of the power-law equation. The green dashed line (---) corresponds the profile estimated from the power-law considering $\alpha = 1/7$, which is the IEC61400 standard recommendation. The red dashed line (----) represents the profile obtained using the log-law equation. The black solid markers (•••) represent the mean values from the AEM measurements, and error bars (horizontal lines) go from the 25th to the 75th percentile. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Table 3
Seasonal mean power output ($P_T$) at hub-height (80 m) of the AEM measurement, power-law(IEC & variable) and Log-law wind speed extrapolation method.

<table>
<thead>
<tr>
<th>Season</th>
<th>Day ($P_T$ (MW))</th>
<th>Night ($P_T$ (MW))</th>
<th>Dynamic $\alpha$</th>
<th>Log-law AEM</th>
<th>Dynamic $\alpha$</th>
<th>Log-law AEM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spring</td>
<td>0.898</td>
<td>0.960</td>
<td>0.898</td>
<td>0.698</td>
<td>0.693</td>
<td>0.698</td>
</tr>
<tr>
<td>Summer</td>
<td>1.049</td>
<td>1.070</td>
<td>1.049</td>
<td>0.833</td>
<td>0.811</td>
<td>0.833</td>
</tr>
<tr>
<td>Autumn</td>
<td>1.343</td>
<td>1.336</td>
<td>1.343</td>
<td>1.203</td>
<td>1.135</td>
<td>1.203</td>
</tr>
<tr>
<td>Winter</td>
<td>1.467</td>
<td>1.497</td>
<td>1.467</td>
<td>1.379</td>
<td>1.339</td>
<td>1.379</td>
</tr>
</tbody>
</table>

The latter indicates no influence of the vertical wind speed variation within and on top (up to 117.5 m) the surface boundary layer on the mean power production. The ratio of the rotor diameter and the hub height is almost 1.12. The wind shear exponent mean values are 0.14 and 0.22, which confirms the conclusions reported in Van Sark et al. (2019), although the influence is dependent on the rotor size and hub height; therefore, it is necessary to analyse with other wind turbine power curves, and wind turbine measured power output.

If wind speed data is available at more than one height, the variable $\alpha$ method is recommended for wind resource assessment. However, if there is the air temperature and relative humidity data, the log-law model would give more information about the vertical wind profile within the surface boundary layer, which is useful for estimating wind turbine aerodynamic performance.

4. Summary and conclusion

This paper analyzes the effect of the vertical wind speed profile in the surface boundary layer on the mean power production of a horizontal axis wind turbine for La Ventosa, Oaxaca, in Mexico. Two of the most widely used vertical wind speed extrapolation methods for wind resource assessment, the power-law and log-law methods, were compared against wind speed data available in the AEM. For the power-law method, a constant value of the shear exponent, $\alpha = 1/7$, and a variable $\alpha$ were used. The log-law model and the power-law method using a variable $\alpha$ yielded IOA values close to 1.0, while good agreement was obtained for $\alpha = 1/7$. However, with $\alpha = 1/7$, the lowest IOA values were obtained among all the adjustments throughout the year-nights.
A comparison was made between the mean power production using the AEM measurements at 80 m, which corresponds to the Vestas90 wind turbine hub height, against that obtained by extrapolating the wind speed at the same hub height using the power-law method with variable $\alpha$ and the log-law model. The percentage error is greater when using the log-law model, with an overestimation of 9%. The method that best approximated the estimation of the mean power from the AEM data at 80 m was the power-law method using a variable $\alpha$, with a percentage error close to zero.

Mean power output was estimated by the equivalent wind speed equation using available AEM measurements. The 20 m reference value of the AEM measurements was used for the power-law method ($\alpha = 1/7$ and variable $\alpha$) and the log-law model to extrapolate to 42.5, 60, 80, 100, and 117.5 m. Variable $\alpha$ was used as reference value because it was in better agreement with the AEM measurements. With $\alpha = 1/7$, the average maximum power during the night is underestimated by 13%. However, during winter and spring, when the value of $\alpha$ is almost 1/7, there is an overprediction of 0.6% in mean power output.

We evaluated the effect of the vertical wind speed profile on the wind resource assessment by calculating the difference in mean power production using the equivalent wind speed and the wind speed at 80 m height. We found a minimum difference of 1.3%, indicating that the vertical variation of wind speed within and above (up to 117.5 m) the surface boundary layer does not influence the average power output for a wind turbine with a diameter of 90 m and a hub height of 80 m.

As a final comment, if wind speed data is available at more than one height, the $\alpha$ variable method is recommended for wind resource assessment. However, if complementary data, including air temperature and relative humidity, are available, the log-law method, specifically the similarity method, could provide more information about the state of the atmosphere, which is useful for aerodynamic performance of wind turbines.

**CRediT authorship contribution statement**

C.A. Lopez-Villalobos: Conceptualization, Methodology, Formal analysis, Investigation, Data curation, Visualization, Writing – original draft. O. Martínez-Alvarado: Writing – review & editing. O. Rodriguez-Hernandez: Writing – review & editing. R. Romero-Centeno: Conceptualization, Methodology, Writing – review & editing.

**Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.
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