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Simulating satellite urban land surface temperatures: sensitivity to sensor view angle and assumed landscape complexity

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A R T I C L E   I N F O
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Urban
DART
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A B S T R A C T
Urban land surface temperature (LST) from satellite earth observation (EO) varies with sensor view angle. Where these variations are not accounted for, urban LST products are inconsistent through time, limiting their use in urban weather and climate model evaluations and process studies (e.g. urban heat island, building energy balance, human thermal comfort). Obstacle-resolving numerical models (ORM) of urban form and radiation exchange are being used to: (a) understand relations between EO view angle, the 3-dimensional urban surface, and urban spatially continuous, global product that has been used to map surface temperature viewing directly downward (i.e. nadir) is biased towards the observation is limited to a two-dimensional view of the surface-leaving radiance to determine LST (Jiang et al., 2018). Urban three-dimensional (3D) morphology and complex surface materials create directionally variable (i.e. anisotropic) surface-leaving radiance (Krayenhoff and Voogt, 2016). Surface-leaving radiance sampled by a remote sensor can therefore change depending on the view angle. For example, an observation viewing directly downward (i.e. nadir) is biased towards the surface-leaving radiance from horizontal surfaces (Roth et al., 1989; Voogt and Oke, 1997; Hu and Wendel, 2019), missing the large wall area contributing to the “complete” surface temperature across all surfaces (Jiang et al., 2018; Yang J et al., 2020). Anisotropy of surface-leaving observation is limited to a two-dimensional view of the surface-leaving radiance to determine LST (Jiang et al., 2018). Urban three-dimensional (3D) morphology and complex surface materials create directionally variable (i.e. anisotropic) surface-leaving radiance (Krayenhoff and Voogt, 2016). Surface-leaving radiance sampled by a remote sensor can therefore change depending on the view angle. For example, an observation viewing directly downward (i.e. nadir) is biased towards the surface-leaving radiance from horizontal surfaces (Roth et al., 1989; Voogt and Oke, 1997; Hu and Wendel, 2019), missing the large wall area contributing to the “complete” surface temperature across all surfaces (Jiang et al., 2018; Yang J et al., 2020). Anisotropy of surface-leaving observation is limited to a two-dimensional view of the surface-leaving radiance to determine LST (Jiang et al., 2018). Urban three-dimensional (3D) morphology and complex surface materials create directionally variable (i.e. anisotropic) surface-leaving radiance (Krayenhoff and Voogt, 2016). Surface-leaving radiance sampled by a remote sensor can therefore change depending on the view angle. For example, an observation viewing directly downward (i.e. nadir) is biased towards the surface-leaving radiance from horizontal surfaces (Roth et al., 1989; Voogt and Oke, 1997; Hu and Wendel, 2019), missing the large wall area contributing to the “complete” surface temperature across all surfaces (Jiang et al., 2018; Yang J et al., 2020). Anisotropy of surface-leaving radiation is limited to a two-dimensional view of the surface-leaving radiance to determine LST (Jiang et al., 2018). Urban three-dimensional (3D) morphology and complex surface materials create directionally variable (i.e. anisotropic) surface-leaving radiance (Krayenhoff and Voogt, 2016). Surface-leaving radiance sampled by a remote sensor can therefore change depending on the view angle. For example, an observation viewing directly downward (i.e. nadir) is biased towards the surface-leaving radiance from horizontal surfaces (Roth et al., 1989; Voogt and Oke, 1997; Hu and Wendel, 2019), missing the large wall area contributing to the “complete” surface temperature across all surfaces (Jiang et al., 2018; Yang J et al., 2020). Anisotropy of surface-leaving observation is limited to a two-dimensional view of the surface-leaving radiance to determine LST (Jiang et al., 2018). Urban three-dimensional (3D) morphology and complex surface materials create directionally variable (i.e. anisotropic) surface-leaving radiance (Krayenhoff and Voogt, 2016). Surface-leaving radiance sampled by a remote sensor can therefore change depending on the view angle. For example, an observation viewing directly downward (i.e. nadir) is biased towards the surface-leaving radiance from horizontal surfaces (Roth et al., 1989; Voogt and Oke, 1997; Hu and Wendel, 2019), missing the large wall area contributing to the “complete” surface temperature across all surfaces (Jiang et al., 2018; Yang J et al., 2020). Anisotropy of surface-leaving

1. Introduction

Surface temperature is a central variable in the surface energy balance. Satellite-derived land surface temperature (LST) can provide a spatially continuous, global product that has been used to map surface urban heat islands (Yang H et al., 2020; Miles and Esau, 2020) and urban air temperature (Venter et al., 2020) for an improved understanding of the effects of cities on the climate and heat stress of populations. Urban land surface models increasingly use LST for model evaluation (Gian naros et al., 2013; Hu et al., 2014). However, any remote sensing (RS)
radiance across urban canopies is defined as an “effective” thermal anisotropy, to differentiate from the thermal anisotropy exhibited by individual surface components (Voogt and Oke, 1998a) caused by the non-Lambertian properties of real-world surfaces, including specular reflections from glass and metals. Effective thermal anisotropy in urban areas can give rise to directional variations in LST of over 10 K (Lagouarde et al., 2010) and is unaccounted for in current LST retrievals. This can confound estimates of surface urban heat island intensity (Lagouarde et al., 2010) and is unaccounted for in current LST retrievals.

Future operational LST retrievals will convert angular LST to nadir or hemispherical temperature products by including models which normalise the angular variations (Cao et al., 2019) or “complete” surface temperature weighted across the full urban envelope (Voogt and Oke, 1997; Jiang et al., 2018; Yang J et al., 2020). The proposed models are semi-empirical parametric models (PM) that are computationally efficient and do not rely on complex inputs of land surface type, structure or component temperature distribution (Cao et al., 2019). PM describe the temperature weighted across the full urban envelope (Voogt and Oke, 1997; Jiang et al., 2018; Yang J et al., 2020). The proposed models are semi-empirical parametric models (PM) that are computationally efficient and do not rely on complex inputs of land surface type, structure or component temperature distribution (Cao et al., 2019). PM describe the underlying processes of angular LST using kernels for (e.g.) emissivity, sun angle and shadow distributions. These are analytically expressed underling processes of angular LST using kernels for (e.g.) emissivity, sun angle and shadow distributions. These are analytically expressed

Using concurrent multi-angle LST for implementation of PM presents challenges. Observations from different satellites have spatial and temporal mismatches and have systematic product/instrumentation uncertainties (Ermida et al., 2014). Only ASTR and SLSTR sensors operate with two observation angles (Liu et al., 2020). Even differences in capture time for a multi-angle and multi-instrument observations (e.g. ~10 min) can have an effect as urban facets exhibit large fluctuations in surface temperature at short time scales (Christen et al., 2012). Quantifying these uncertainties requires detailed evaluation from high-resolution observations and simulations.

3D models (hereafter “3DM”) or obstacle resolving models (ORM) offer a detailed, physical basis to evaluate PMs and multi-angle LST through explicit definition of the observed surface geometry and temperature distribution. However, available ORM approaches also vary in terms of building complexity and representation of real-world surface temperature variability. For example, Jiang et al. (2018) evaluate the PM of Vinnikov et al. (2012) and simulate scenarios when multi-angular LST were unavailable using an ORM (CoMSTIR) with idealised surface temperatures and cuboid buildings. Wang et al. (2020) evaluated the GUTA PM using the DART ORM (Wang et al., 2018) configured with repeating idealised buildings. It is the overarching objective of this study to quantify the implications of assumptions during the ORM setup. This is vital so that ORM can then be used to assess uncertainties inherent in PM used to support the next generation of LST retrievals.

ORM require a 3D description of the surface of interest to determine upwelling radiance (e.g. DART – Discrete Anisotropic Radiative Transfer, Gastellu-Etchegorry et al. (2015)), surface temperature fields (e.g. TUF-3D – Temperature of Urban Facets, Krayenhoff and Voogt (2007)) or to interpret sensor view (e.g. SUM - Surface-sensor-sun Urban Model, Soux et al., 2004). The idealised geometries greatly simplify model setup and input parameters. Improving geometry and surface
Fig. 2. Variability of surface characteristics in central London between grid-cells (n = 81, each 420 m × 420 m) compared to the study area (red) with (upper) maps and (lower) histograms with nth percentiles (Pn) of P25 → P75 (dashed lines), P50 (solid line), with solid red line the study area value. (a) Land cover (4 m resolution) with extent of maps (white dashed box) in b–l and a sample MODIS M*D11A1 pixel (orange box). Surface characteristics: (b) plan area fraction of tall vegetation (> 2 m) (c) plan area fraction of grass (d) plan area fraction of buildings (i.e. plan area index), (e–h) building height, (i–l) sky view factor (Dozier and Frew, 2002) calculated in R (R Core Team, 2017) with the “horizon” package (Van Doninck, 2018), and (g, l) standard deviation of the respective parameter. Maps oriented to grid north (WGS84 UTM grid zone 31 N). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
temperature characterisation requires rarely available detailed datasets (Masson et al., 2020) or more complex model design (i.e. beyond frequently used plane-parallel building grids such as in TUF-3D; ENVI-met, Gal and Kanto (2020)).

A range of urban characteristics have not yet been addressed by previous thermal anisotropy modelling applications:

i. With cuboid buildings and flat surfaces, sub-facet scale (e.g. < 1 m) shadowing is not accounted for. Sub-facet shadows can reduce a wall’s mean surface temperature by 1–7 K (Hilland and Voogt, 2020), whereas roof shape (pitch and structure) can cause variations of over 20 K (Morrison et al., 2021). Prior ORM studies of LST anisotropy without micro-scale 3D structure hence tend to underestimate the anisotropy (Lagouarde et al., 2016; Krayenhoff and Voogt, 2016).

ii. Urban vegetation is often a large fraction of the urban surface (Small and Lu, 2006) and generally much cooler than impervious surfaces (Meier and Scherer, 2012). To our knowledge only Dyce and Voogt (2018) have used ORM with urban vegetation to simulate directional LST, but using plane-parallel building and vegetation canopies (see i.).

iii. Surface temperatures from ORM are very sensitive to model parameters that describe the surface composition (e.g. material thickness, heat capacity, albedo, emissivity). Still, to date neither these parameters nor the ORM surface temperatures are extensively evaluated as the necessary observations are both challenging to obtain and have limited spatial and temporal footprints (Pigeon et al., 2008). Ground-based observations, such as those across a residential area (Adderley et al., 2015), an idealised scale model (Morrison et al., 2018) or the New York city skyline (Ghandehari et al., 2018), do not cover the full complexity and diversity of realistic urban geometries. Although airborne observations (e.g. Sugawara and Takamura, 2006; Lagouarde and Irvine, 2008) and vehicle transects (Voogt and Oke, 1998a) have greater spatial extent, and hence represent higher complexities, they are snapshots in time.

iv. Urban materials are generally unknown at high spatial (facet scale), spectral (short and longwave) and angular (e.g. specular reflectivity) resolution. Thus, ORM are typically prescribed with bulk and Lambertian optical properties. In stark contrast, real urban areas have extremely complex material distributions and spectral responses (Kotthaus et al., 2014), with plastic signatures (Kotthaus et al., 2014), with plastic signatures around tall buildings (Agathangelidis et al., 2020) may hence be anomalies associated with LST retrieval uncertainties caused by the influence of specific materials (e.g. high glass fraction) on the anisotropy (Crawford et al., 2018).

To assess such sources uncertainty in common ORM configurations and to quantify the relative impact of simplifying the urban form and temperature, respectively, this study uses a uniquely detailed model accounting for those characteristics (i.-iv.) commonly simplified elsewhere. This allows us to model urban thermal anisotropy, with varying degrees of complexity in the underlying processes whereby the implications of various assumptions can be quantified. Realistic urban form and surface temperatures that are neither often nor easily available are combined to simulate a heterogeneous urban area. The micro-scale surface structure of 3D buildings is here resolved to individual pitched roofs, chimneys, balconies. Building facades, ground surfaces and vegetation are assigned component surface temperatures derived from high-resolution thermal infrared camera observations. Using a state-of-the-art radiative transfer model, a “realistic baseline” simulation of urban anisotropy is performed that then serves as a reference to assess simplified model setups. The complex landscape is incrementally simplified to obtain descriptions similar to previous studies to and the ability to characterize angular LST variability is compared to the “realistic

Table 1

<table>
<thead>
<tr>
<th>Study area (Fig. 1a, 420 x 420 m) land cover fractions and variability of heights (Morrison et al., 2020) and sky view factor (Gal and Unger, 2014; Dorman, 2021).</th>
<th>Trees &amp; Shrubs</th>
<th>Building</th>
<th>Grass</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plan area fraction</td>
<td>0.17</td>
<td>0.37</td>
<td>0.17</td>
</tr>
<tr>
<td>Percentiles</td>
<td>Height (m)</td>
<td>Height (m)</td>
<td>Sky view factor</td>
</tr>
<tr>
<td>P25</td>
<td>6.82</td>
<td>6.9</td>
<td>1.41</td>
</tr>
<tr>
<td>P50</td>
<td>10.01</td>
<td>13.49</td>
<td>1.57</td>
</tr>
<tr>
<td>P75</td>
<td>15.21</td>
<td>19.1</td>
<td>1.75</td>
</tr>
</tbody>
</table>

Table 2

Central London study area is represented as three-dimensional model landscapes with variations in: surface geometry level of detail (LOD), surface temperature distribution ($T_{\text{ISO}}$) and vegetation leaf area density (LAD). Landscapes are implemented in the DART radiative transfer model to simulate directional land surface temperature.

<table>
<thead>
<tr>
<th>Landscape feature</th>
<th>Code</th>
<th>Description</th>
<th>Basis</th>
</tr>
</thead>
<tbody>
<tr>
<td>Surface geometry level of detail description (summary in Fig. 3)</td>
<td>LOD2</td>
<td>Realistic buildings (e.g. pitched roofs, chimneys) and vegetation &gt;2 m tall</td>
<td>Most realistic geometry directly from Google Earth (Morrison et al., 2020), including sub-facet scale features</td>
</tr>
<tr>
<td>LOD1</td>
<td>Extruded building footprints. Same vegetation as in LOD2</td>
<td>Most widely available and easy to use format for 3D building morphology.</td>
<td></td>
</tr>
<tr>
<td>LOD0</td>
<td>Randomly oriented cuboid buildings. No trees.</td>
<td>Assumed in parametric models (e.g. GUTA) and a constraint in many common 3D models (e.g. TUF-3D’s plane-parallel cubes)</td>
<td></td>
</tr>
<tr>
<td>Surface temperature distribution ($T_{\text{ISO}}$) (details in Table 4)</td>
<td>M21</td>
<td>Ground-based observations (Morrison et al., 2021) stratified by sun-surface geometry, shadow history and high/low albedo</td>
<td>Most detailed description available from observed surface temperature variation (Morrison et al., 2021)</td>
</tr>
<tr>
<td>ILU</td>
<td>Same as M21 but no shadow history</td>
<td>A simpler scheme accounting only for sun-surface geometry; used in other models (e.g. Wang et al., 2018)</td>
<td></td>
</tr>
<tr>
<td>Leaf area density of trees/shrubs uniformly applied to all vegetation</td>
<td>LAD0</td>
<td>No vegetation (trees/shrubs)</td>
<td>Typical assumed in other models (except Dyce and Voogt (2018))</td>
</tr>
<tr>
<td>LAD0.15</td>
<td>Uniform LAD = 0.15 m$^2$ m$^{-3}$</td>
<td>Krayenhoff et al., 2020</td>
<td>upper range</td>
</tr>
<tr>
<td>LAD0.7</td>
<td>Uniform LAD = 0.7 m$^2$ m$^{-3}$</td>
<td>Lalic and Mihailovic, 2004a</td>
<td>lower range; also near (Klingberg et al., 2017) ~ 0.6 lower range</td>
</tr>
<tr>
<td>LAD1.6</td>
<td>Uniform LAD = 1.6 m$^2$ m$^{-3}$</td>
<td>Lalic and Mihailovic, 2004a</td>
<td>upper range; used in London, UK (Jenjean et al., 2017); within (Klingberg et al., 2017) upper range (1.5–2)</td>
</tr>
</tbody>
</table>
urban LST as brightness temperatures (Etchegorry et al., 2012) (Section 2.1.2) can simulate satellite-derived LST variation by view angle.

### Methods

#### Model landscape

In this study, the term “landscape” describes a 3D model of urban form and surface temperature. Here, the urban form includes the buildings, ground, and vegetation, overlaid with a 3D surface temperature field with 1 m × 1 m × 1 m resolution voxels (Appendix A). Each voxel holds a data point (here surface temperature) for a given volume. Landscapes are created (Section 2.3) and then implemented in DART (Section 2.1.2) to simulate T_{b}^{EO}.

#### DART radiative transfer model

DART (here version 5.7.5) is a computer model that simulates radiative transfer in heterogeneous 3D landscapes. Using a ray tracing approach, DART determines the emission and multiple scattering of individual longwave infrared (LWIR) rays across a landscape. The result can be a 2D image of a landscape’s surface-leaving thermal radiance \([L^{surf}(x, y, \phi, \theta, \lambda, \phi_0)]\), W m\(^{-2}\) sr\(^{-1}\) \(\mu\)m\(^{-1}\) across a horizontal plane at the top of the landscape (the bottom of atmosphere – BOA) (Yin et al., 2015; Wang and Gastellu-Etchegorry, 2020) at a given wavelength (\(\lambda\), \(\mu\)m), with (x, y) the image pixel indexed by surface component(s) i (e.g. roof and/or wall), \(\phi\) and \(\theta\) (\(^\circ\)) the zenith and azimuth propagation angles, and \(\Omega\) (sr) the solid angle. Hereafter for brevity, \(\Omega\) and \(\lambda\) are no longer stated explicitly as simulations are performed at a single selected wavelength and use uniform solid angle. For each timestep, 116 2D images are computed for directions \(\theta = 0 \rightarrow 360^\circ\). To reduce computation time, the number of image files, and the data stored, only images for \(\phi < 50^\circ\) are simulated.

To determine a landscape’s view angle variation in upwelling radiance, \(L^{surf}(x, y, \phi, \theta, i)\) is resampled to obtain a landscape mean surface-leaving radiance typical for EO resolutions:

\[
L^{surf}(\phi, \theta) = \frac{1}{n} \sum_{[x,y]} L^{surf}(x, y, \phi, \theta, i)
\]

### Table 3

<table>
<thead>
<tr>
<th>LOD0</th>
<th>Uncertainty</th>
<th>Details</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plan area index (PAI)</td>
<td>± 10%</td>
<td>&gt; 90% accuracy (EO building masks in European cities) (Esch et al., 2020)</td>
</tr>
<tr>
<td>Mean building height</td>
<td>± 3 m</td>
<td>Mean bias error (EO in Germany) – 3 m (Frantz et al., 2021)</td>
</tr>
<tr>
<td>Building spacing</td>
<td>± 25%</td>
<td>Real-world cities have irregular building spacing (Chen et al., 2017)</td>
</tr>
</tbody>
</table>

The uncertainty range used in morphometric parameters for the lowest level of detail (LOD0) geometry description of the London study area. EO indicates earth observation techniques are used.

Baseline” to understand which details are most relevant for future comparisons to PM implemented in LST retrievals.

### 2. Methods

#### 2.1. Modelling satellite LST variation by view angle

The Discrete Anisotropic Radiative Transfer (DART) model (Gastellu-Etchegorry et al., 2012) (Section 2.1.2) can simulate satellite-derived urban LST as brightness temperatures (T_{b}^{EO}) for different “landscapes” (Section 2.1.1). As DART can model T_{b}^{EO} for any zenith (\(\phi\)) and azimuth (\(\theta\)) view angles (\(^\circ\)), this allows variations across different landscapes to be assessed. Taking nadir sampled temperatures \(T_{b}^{EO}(\phi = 0)\), i.e. “straight down” EO view as reference, the difference (\(\Delta T_{b}^{EO}\)) to off nadir \(T_{b}^{EO}(\phi, 0)\) is:

\[
\Delta T_{b}^{EO} = T_{b}^{EO}(\phi, 0) - T_{b}^{EO}(\phi = 0)
\]

The overall \(T_{b}^{EO}\) range (i.e. maximum (max) to minimum (min)) for distribution of temperatures at a given view angle is (Krayenhoff and Voogt, 2016):

\[
\Lambda = \max\{T_{b}^{EO}(\phi, 0)\} - \min\{T_{b}^{EO}(\phi = 0)\}.
\]
with n the number of image pixels. \( L_{\text{surf}}(\phi, 0) \) then relates to \( T_b^{\text{EO}}(\phi, 0) \) by inversion of the Planck function \( (B_{\lambda}^{-1}) \) at the simulation wavelength \( \lambda, \mu \text{m} \):

\[
T_b^{\text{EO}}(\phi, 0) = B_\lambda^{-1} \left[ L_{\text{surf}}(\phi, 0) \right].
\]

Here \( \lambda = 11.02 \mu \text{m} \) is used, corresponding to the centre of MODIS (Moderate Resolution Imaging Spectroradiometer) band 31. A split window (Zhengming and Dozier, 1996) or other (e.g. Islam et al., 2017) LST retrieval would then use \( L_{\text{surf}} \) at different bands and consider neither the view angle or facet (i) level radiative exchange processes.

\[ T_b^{\text{EO}}(\phi, 0) = B_\lambda^{-1} \left[ L_{\text{surf}}(\phi, 0) \right]. \]

2.1.3. DART vs. previous sensor view modelling of anisotropy

Previous sensor view modelling of thermal anisotropy to derive \( T_b^{\text{EO}}(\phi, 0) \) has determined the weighted contribution from various surface types (e.g. sunlit/shaded wall, roof, ground) for different view angles (e.g. Lagouarde et al., 2010):

\[
T_b^{\text{EO}}(\phi, 0) = \sum_{i} f_i(\phi, 0) (T_{b,i})
\]

where \( f_i(\phi, 0) \) is the view fraction of surface component i within the sensor field of view determined by a sensor view model (e.g. Soux et al., 2004), \( T_{b,i} \) is the surface component brightness temperature from observations or energy balance modelling, and \( n_i \) is the total number of surface components. Surface components act independently and are typically opaque; but have included tree crowns (Dyce and Voigt, 2018).

DART surface components can instead have radiative contributions from anisotropic scattering, transmission through turbid media (e.g. vegetation) and the (cloud-free) sky and are not constrained to idealised geometry (cuboid buildings, plane-parallel surfaces, smooth facets, etc.), bulk facet-level surface temperatures, or Lambertian emission.

2.2. Study area and observation period

The central London (UK) 420 m × 420 m study area has a mix of vegetation, high- and low-rise structures (Fig. 1). The analysis uses ground-based surface temperature observations taken in the area (Morrison et al., 2020; Morrison et al., 2021) for a mainly clear-sky summer day (27th August 2017).

To assess how representative the study area is of central London and a single EO pixel (e.g. MODIS/Sentinel) at a resolution of ~1 km × 1 km, the morphometric and land cover characteristics are analysed for a ~4 km × 4 km area around the site (Fig. 2a). South and east of the site is the central business district. Both average building height and plan area index (PAI, fractional area covered with buildings) decrease northwards, while vegetation fraction increases in more residential areas. The study area PAI is similar to the surroundings (Fig. 2), but there is more vegetation (>75th percentile of the extended area, Table 1 cf. Fig. 2b, c) associated with a park (Fig. 1b, centred at grid coordinates 284,500, 5,712,850).

As earlier ground-based thermography studies were undertaken in less built-up areas, our site’s median building height (13.5 m, Table 1) is greater than both (Adderley et al., 2015) area-weighted building height of 6.23 m and (Morrison et al., 2018) 1.5 m cubes. From visual inspection, the vegetation fraction is lower than in the (Meier and Scherer, 2012) study area.

2.3. Model landscapes of the study area

The study area surface geometry, vegetation and temperature are simulated to create a series of model landscapes (Table 2, more details in Appendix A). Digital surface models (DSM) are used to represent the 3D geometry of each landscape. Their resemblance to the “real world” are indicated by their level of detail (LOD), where LOD2 (Fig. 3) has the most realistic building features (e.g. sloped roofs, chimneys, and balconies) and LOD0 the most idealised. In LOD1, the building footprints Evans et al. (2011), Fig. 1a) are vertically extruded (using “3Dfier”, Commandeur, 2020) to create 3D buildings with flat roofs and walls. As building footprints are widely available (e.g. Microsoft’s Open Street Map (IHeris et al., 2020)) LOD1 models are relatively easy to produce and hence most commonly used.

In LOD0 (Fig. 3), cuboid buildings are used with random orientations constrained so each wall angle has the same weight in an effective thermal anisotropy (Wang et al., 2018) estimate. The baseline LOD0 has regularly spaced cubes of randomly assigned heights (informed by the LOD2’s building height inter-quartile range) with both the PAI and number of buildings from the LOD1 building footprint. As LOD0 requires the least input information and preprocessing, it could potentially parameterise urban geometry globally; although coarsely and less accurately than higher LOD datasets. A range of LOD0 geometries are derived (hereafter “LOD0 ensemble”) to account for uncertainties in the

<table>
<thead>
<tr>
<th>Surface property name</th>
<th>Obtained in 3D using</th>
<th>Surface property description</th>
<th>Surface property stratification</th>
<th>Used in</th>
</tr>
</thead>
<tbody>
<tr>
<td>Orientation and material</td>
<td>Blender (Blender, 2018) 3D modelling, airborne hyperspectral data (Morrison et al., 2020)</td>
<td>Cardinal facing wall orientation. Boolean high/low albedo roof separation for LOD2 geometry (constant low albedo for LOD1 and LOD0)</td>
<td>Roof (low albedo) South facing</td>
<td>M21, ILU</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Roof (high albedo) West facing</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Ground (impervious) Down facing</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Ground (grass) North facing East facing</td>
<td></td>
</tr>
<tr>
<td>Sun-surface geometry</td>
<td>DART shortwave simulation</td>
<td>Bidirectional reflectance factor (BRF)</td>
<td>Lambertian BRF: 0 (shaded) → 2 (most sunlit) {0.05 steps} (unitless)</td>
<td>M21, ILU: boolean sun or shade</td>
</tr>
<tr>
<td>Shadow history</td>
<td>DART shortwave simulation shadow tracking through time (Morrison et al., 2021).</td>
<td>Recently shaded surfaces cool exponentially with time constant (r, min); maximum interval 2r (or until ambient temperature reached)</td>
<td>2r Roof ~ 86 min (fastest cooling)</td>
<td>M21</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2r Ground ~ 269 min</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>21 Walls ~ 347 min (slowest cooling)</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(Morrison et al., 2021)</td>
<td></td>
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Fig. 4. Study area surface-leaving radiance shown as brightness temperatures ($T_b$) simulated using three-dimensional (3D) surface temperature derived from observations and the DART model for 27th August 2017 at (left) 11:00 and (right) 14:00 for (top) nadir and (middle – bottom) off-nadir zenith (ϕ) angles. Black dashed box (top left) is the area shown in Fig. 6a-d. Images have orthographic sensor perspective projection with surface → sky view directions such that: $\theta = 0^\circ$ is grid north and $\theta = 90^\circ$ grid east (WGS84 UTM grid zone 31 N) and $\phi = 0^\circ$ ($\phi = 90^\circ$) is viewing directly upward from (parallel to) the surface. White areas are the view inside buildings at the edge of the domain and masked from subsequent analysis.
Fig. 5. Simulated thermal anisotropy for the study area with (polar plots) the difference in brightness temperature $[\Delta T_{EO}(\phi, \theta) - T_{EO}(\phi = 0^\circ)]$ from nadir temperature ($T_{EO}(\phi = 0^\circ)$) with zenith angle ($\phi$, dashed lines with intervals top left plot) $\leq 47^\circ$ simulated using observationally derived “M21” three-dimensional (3D) $T_s$ (Morrison et al., 2021) across LOD2 geometry (same as Fig. 4) (Table 4). DART is used to simulate surface-leaving radiance for discrete directions (coloured dots). $\phi = 0^\circ$ is radiation propagating upward and perpendicular to flat ground; $\phi = 90^\circ$ is propagation parallel to flat ground; $\theta = 0^\circ$ is radiation propagating true north and $\theta > 90^\circ$ is radiation propagating eastward (etc.). Absolute simulated values (inset) show (dot) nadir $T_s$ ($T_{EO}(\phi = 0^\circ)$), (black bar) the $T_{EO}$ range across any direction up to $47^\circ$ off-nadir, and (red bar) the range for near-nadir (e.g. Landsat) views ($\phi < 8.8^\circ T_{EO}(\phi, 0^\circ)$). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
Fig. 6. Detail of Fig. 4 (black dashed lines): (a) aerial RGB image with similar shadow patterns (EDINA Digimap, 2015), (b-e) simulated high-resolution nadir-view (i.e. zenith angle $\phi = 0^\circ$) images to represent earth observation (EO) products (x, y, pixels; m) of brightness temperature ($T_{b}^{EO}(x, y)$) using DART across landscapes with varied descriptions of surface geometry level of detail (LOD); LOD2 highest, LOD0 lowest and three-dimensional surface temperature ($T_{s}^{3D}$), where M21 is complex ($T_{s}^{3D}$ = M21) (Morrison et al., 2021) and ILU is simplified ($T_{s}^{3D}$=ILU). Labels ($T_{s}^{3D}$ ($\phi = 0^\circ$)) are image averages (with Planck function).

bulk parameters used (Table 3): PAI ±10% (Esch et al., 2020), building height ± 5 m (Frantz et al., 2021) and spacing of cubes randomly up to 25% from the regular spacing distance.

All DSMs are given a broadband emissivity of 0.93 based on observed mean impervious material values (Kotthaus et al., 2014). This is used by DART to simulate multiple scattering of longwave ($\lambda = 11.02 \mu m$, Section 2.1.2) radiation between surface components.

The vegetation in LOD1 and LOD2 are both the same, whereas for LOD0 there is no vegetation (Fig. 3). The vegetation is based on location of tall vegetation (i.e., non-grass) which includes trees and shrubs (> 2 m above ground level), hereafter vegetation canopy elements (VCE, Appendix A). As the leaf area density (LAD) can vary with vegetation type and volume, we consider some different densities (Table 2) but for each case all VCE voxels are assumed to have the same characteristics. The 1 m$^3$ voxels are assumed to be turbid with a spherical angular distribution of leaves, constant LAD and “deciduous leaf” optical properties at 11 μm from the DART spectral database (leaf transmissivity = 0.0145, reflectance = 0.0195).

2.4. Model surface temperature

Ground-based observations on a mostly cloud-free day at 30 min resolution are used to capture spatial and temporal variations of $T_s$ that are known to vary over short distances (Lee et al., 2018; Aguerre et al., 2019; Morrison et al., 2021). Previous ground-truth of urban $T_s$ are often limited to single-point infrared thermometers (e.g. Mathew et al., 2018; Wang et al., 2018), whereas we use thermal infrared cameras to better resolve spatial variations in surface temperature (Christen et al., 2012; Adderley et al., 2015). Observed surface temperatures (Morrison et al., 2021) are assigned to all landscape surfaces giving either a detailed distribution (“M21”, Table 2), or simply based on solar illumination (“ILU”, Table 2). The observed surface temperatures are corrected for atmospheric emission and absorption, and surface reflections, with uncertainties as determined by Morrison et al. (2020). Each voxel ($X = Y = Z = 1\, m$) is assigned one $T_s$ ($T_s^{3D}(X, Y, Z)$) in both methods (Appendix B).

However, a voxel can contain more than one surface component; for example, a building corner may have both east and south facing walls, or a balcony a south, down and roof facing surfaces. In these cases $T_s^{3D}(X, Y, Z, i)$ is set to the mean $T_s(i)$ of all surface components involved. The surface temperature voxels are saved as a pre-processing product for input into DART, with the surface temperature distribution across the DSM triangles determined by the triangle-cell intersection.

For M21, the thermal camera observations are stratified based on three surface properties $i$ ($T_s(i)$) (Table 4) that drive surface temperature variation in urban areas (Morrison et al., 2021). These include: for example, a pitched roof’s $T_s$ can vary with orientation to the sun; materials with higher albedos are associated with lower surface temperature through the lower absorption of solar radiation; and the effects of thermal inertia (Aguerre et al., 2019) are stratified by a combination of facet type and time in shade rather than using overall aggregates (e.g. Voogt and Oke, 1998b; Morrison et al., 2018). For ILU, $T_s(i)$ is stratified using sunshine status, surface orientation, and material only (i.e. no shadow history, Table 4).

Following the GUTA PM (Wang et al., 2018) evaluation using DART, a surface component $T_s$ range is calculated for direct input to the model. The range of mean temperatures is defined by shaded (“lower”) and
sunlit (“upper”) limits. The “upper” limit is prescribed in DART to any sunlit surface, and the “lower” \( T_s \) to any shaded surface. This gives 3D variations based on sun angle, DSM, and vegetation.

While M21 is the best estimate of a realistic \( T_s \), ILU is both more easily simulated as it requires fewer surface temperature components, and more representative of studies limited by observations availability (e.g. IRTs, thermocouples, Li and Li (2020)) or idealised 3DM with plane-parallel geometry. The ILU setup is already implemented in DART, meaning the landscape geometry can change without needing to manually pre-process and store the M20 landscape temperature in large 5D numerical arrays (i.e., 3D space, shadow history timestep, surface class).

As the brightness temperature observations for vegetation are unstratified by sun-surface geometry, all VCE are assigned the same \( T_s \). This is the observed air temperature measured 1 km south east of the study area (Morrison et al., 2020).

3. Results and discussion

First, the highest detail landscape simulation, informed by observations and 3D modelling, is analysed (Section 3.1). Based on this, the best estimate of 2D satellite observations are derived. The simulations are unprecedented both in terms of spatial resolution (<1 m) and temporal continuity (30 min resolution for a day post-sunrise).

Second, this benchmark is used to study a comprehensive range of idealised landscapes (Section 3.2) based on similar assumptions used in previous simplified approaches to interpret effective thermal anisotropy. These simplified models are required to verify any future operational corrections (e.g. based on GUTA, Wang et al. (2020)) for effective thermal anisotropy.

3.1. Highest detail landscape simulation

3.1.1. Spatially resolved LST variations in response to satellite view angle

To quantify variations in LST in response to the view angle across, high spatial resolution directional brightness temperature images \( T_b^{EO}(x, y, \phi, \theta) \), a combination of LOD2 geometry and M21 surface temperature observations (Table 2) is used. Depending on the view angle, different surfaces are captured in the image (Fig. 4) which creates unique brightness temperature distributions. Roof, ground, and vegetation are viewed from the nadir direction. Off-nadir view angles also have wall surfaces visible, many with complex \( T_b \) distributions.

Fig. 7. Simulated satellite brightness temperature \( (T_b^{EO}) \) using DART and daytime ground-based observations across zenith view angles \( (\phi) \) up to 47° off-nadir, shown as differences between nadir and off-nadir \( (\Delta T_b^{EO}) \) for a central London study area using a realistic (LOD2, Fig. 3) landscape geometry and dense vegetation (LAD1.6, Table 2). \( \Delta T_b^{EO} \) compared across two different three-dimensional (3D) surface temperature \( (T_s^{3D}) \) parameterisations derived from observations: \( T_s^{3D} = M21 \) varies by sun-surface geometry, facet type, shadow history, material. \( T_s^{3D} = ILU \) varies by sun/shade/facet type only. (b) \( \Delta T_b^{EO} \) for (black) day (blue) night time off-nadir view angles for 08:00 → 22:00 27th August 2017 and (a) subset of view angles for (left) M21 and (right) ILU for all azimuth angles \( (0° \leq \theta \leq 360°) \) for (rows) three zenith view angles with (star) sun angle. Angle definitions (c) shows “upward” polar coordinate system used, i.e. angles measured with a ground to sky perspective, with (crosses) the discrete view angles, (coloured lines) the three zenith samples used in (a) and (stars) the 30 min upward sun angles from early morning \( (\phi > 50°, \theta < 135°) \) → midday \( (\phi \approx 40°, \theta = 180°) \) → late afternoon \( (\phi > 50°, \theta > 230°) \). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
facets wall geometry creates contrasting temperatures around sunlit portions and cooler shaded areas (e.g. wall recesses, from balconies) or with oblique sun-surface angles. With simple planar surface geometry, wall patterns. The complex roof geometry creates similarly complex shadow histories. The near-nadir (e.g. Landsat) views (here the sun direction is consistent with prior mid-latitude observations (Hu and Wendel, 2019). The near-nadir (any of a-c have n points = 4360), shown as differences between nadir (\( \phi = 0^\circ \)) and off-nadir (\( \Delta T_{b}^{EO}(\phi) \)) compared for landscapes with different building geometry level of detail (LOD) for a central London study area. All comparisons have no vegetation. 3D surface temperatures distributed by solar illumination (\( T_{3D}^{s} \)). 

3.1.2 Temporally resolved thermal anisotropy

While airborne studies capture temporal snapshots of anisotropy, here the analysis is continuous at 30 min resolution between 2 h after sunrise (08:00) and 2 h after sunset (22:00), allowing for a time series evolution of anisotropy (Fig. 5) to be investigated. It reveals that at 08:00, when \( T_{b} \) is similar between facet types (Appendix B), \( T_{b}^{EO}(\phi, \theta) \) is near-isotropic across all view angles up to \( \theta = 47^\circ \) (eq. 2).

\( T_{b}^{EO}(\phi, \theta) \) is greater for off-nadir view angles around the sun angle (hot spots). At 10:00 \( T_{b}^{EO}(\phi, \theta) \) peaks at 3.0 K warmer than nadir (301.2 K) (\( \Lambda = 4.7 \) K). \( \Lambda \) reaches 4.9 K at 10:30. The hot spot being found near the sun direction is consistent with prior mid-latitude observations (Hu and Wendel, 2019). The near-nadir (e.g. Landsat) views (here \( \phi < 8.8^\circ \), Fig. 5, red bars) have lower \( T_{b}^{EO}(\phi, \theta) \) variation as expected (\( \Lambda \leq 1.0 \) K, \( \Lambda = 1.0 \) K at 12:30) with minimum 0.2 K at 08:00 and 20:00.

3.2 Effect of landscape simplification on thermal anisotropy

To identify key inter-landscape differences in brightness temperature from an earth observation perspective (\( T_{b}^{EO} \)) for the different landscape configurations (Fig. 3, Fig. 4) we discuss a subset (Fig. 6a) of the study area. The highest detail \( T_{b}^{EO}(\text{LOD2 geometry and M21}) \) has the greatest \( T_{b}^{EO}(\phi, \theta) \) variation (cf. Fig. 6c), particularly across roofs where sub-facet geometry (e.g. sloped roofs, chimneys) have diverse sun-surface geometries.

In Fig. 6b, M21’s sun-surface geometry classification (BRF, Table 4) prescribes a range of \( T_{b} \) For example, \( T_{b}^{EO}(x, y) \) across the sunlit pitched roof (centred \( x = 25 \), \( y = 370 \)) has around 307 K \( \sim 316 \) K \( T_{b}^{EO}(x, y) \) variation (low irradiance and BRF), the right side is almost perpendicular to the sun angle (high irradiance and BRF).

The parameterisation ILU (Fig. 6c) has Boolean “sunlit” and “shaded” temperatures across \( T_{b}^{EO} \) (Section 2.4). This results in the pitched roof being mostly homogeneous as it is prescribed “sunlit” roof \( T_{b} \). Across other roofs, \( T_{b}^{EO}(x, y) \) ILU varies only if there is self-shadowing from micro-scale roof features. ILU’s lower micro-scale variation in roof temperature results in a \( T_{b}^{EO}(\phi = 0^\circ) \) (308.0 K) that is 2.5 K higher than for the M21 (305.5 K) case. Similar micro-scale effects have been reported for walls with ~20–40% self-shading (Hilland and Voogt, 2020).

With flat roofs (LOD1) there is no micro-scale \( T_{b} \) variation (Fig. 6d). LOD1’s buildings are generally more pronounced given their flat facets with sharp right angles when roofs and walls intersect. Some buildings
are present in LOD1 but not in LOD2 (and vice versa) because of differing DSM data sources. LOD1, created around 2010, has buildings at 
\(x = 50, y = 390\) and \(x = 0, y = 420\) (Fig. 6) which are absent in LOD2 (created 2018). However, manual inspection across the study area, suggests the LOD1 footprints generally agree well with the LOD2 buildings (Fig. 1a).

For vegetation, both the geometry and temperature descriptions in the LOD1 and LOD2 simulations are the same. Hence, the VCE have homogeneous \(T_s\). However near the canopy edges, \(T_bEO(x, y)\) varies where the canopy is often thinner (e.g. Fig. 6b) allowing radiation from the warmer ground below to penetrate.

Although, the LOD0 cubes (Fig. 6e) have no micro-scale \(T_s\) variation and VCE are omitted, the \(T_s\) responds to the shadows cast on the ground creating the coolest regions. The cube roofs are warmest. The VCE are not included as the layout relative to real-world buildings (cf. cubes) is not matched. Using idealised cuboid vegetation to test the sensitivity of various vegetation and cube morphologies to thermal anisotropy (see Dyce and Voogt, 2018) is outside of this study’s aims.

### 3.2.1. Surface temperature distribution

The two different surface temperature distributions (M20, ILU, Table 2, Table 4) are compared to understand the contribution of shadow history and surface cooling through time impact on \(T_bEO(\phi, \theta)\) variations. \(T_bEO(\phi, \theta)\) is simulated using the simplified temperature across the landscape (\(T_s3D = ILU\), Table 2) and compared to results using the complex distribution (\(T_s3D = M21; Table 2, Section 3.1\)).

Across all off-nadir view angles through the day (08:00–22:00, Fig. 7b), the effective thermal anisotropy (defined here as the [off-nadir
range is greatest (larger positive values) around the sun angle (parameterisation (–)). Analysis of thermal anisotropy through time (Fig. 7 a) draws out the hot spot in relation to the sun angle. \( \Delta T^\text{bEO}(\phi, \theta, T^\text{3D} = \text{LOD1}) > 0 \) K across a wider range around the sun angle for all timesteps.

As M21 resolves the thermal inertia with surface orientation (Supplementary Material, Appendix D), \( \Delta T^\text{bEO}(T^\text{3D} = \text{LOD2}) \) can reproduce an observed asymmetrical hot spot (Lagouarde et al., 2010) caused by the “lags” of the azimuth hot spot behind the sun angle hotspot. After sunset (Fig. 7a, without *) \( \Delta T^\text{bEO}(T^\text{3D} = \text{LOD2}) \) maintains a positive bias into the night, with a thermal inertia hot spot signal of \( \Delta T^\text{bEO} > 1 \) K around \( \theta = 200° - 300° \) until 21:30. In contrast, as \( T^\text{3D} = \text{ILU} \) has no thermal inertia, \( \Delta T^\text{bEO}(T^\text{3D} = \text{ILU}) \) has no evening warm bias and has less variation (–0.5 → 0.5 K after sunset across all view angles). Across night-time intervals 18:30–22:00, the MAE is 0.19 K (Fig. 7b, blue).

3.2.2. Surface geometry
To isolate the importance of building shape complexity, the landscape DSM is simplified (LOD2 → LOD1 → LOD0) with one \( T^\text{3D} \) parameterisation (\( T^\text{3D} = \text{ILU} \)). Vegetation is excluded in LAD0 (Table 2).

Comparing across all 30 min time intervals (08:00–18:00) and \( \phi \) settings, the anisotropy for the two lower LOD landscapes (Fig. 8 a-c, y axes) generally agrees well with LOD2. The planar facet geometry (\( \Delta T^\text{bEO}(\text{LOD2}) \)) agrees better with the LOD2 anisotropy (Fig. 8a, \( y \) axis) (MAE = 0.16 K) than the cuboid geometry (\( \Delta T^\text{bEO}(\text{LOD0}) \); MAE = 0.44 K; Fig. 8b). The linear regression (Fig. 8, green) slopes are lower for LOD0 (0.55) than LOD1 (0.87). Generally, a slope < 1 would indicate the more complex geometry (LOD2) is more anisotropic. The LOD2 \( \Delta T^\text{bEO} \) range is greatest (larger positive values) around the sun angle (“hot spot”, Fig. 7) and has smaller negative values for azimuth angles 180° opposite the sun angle. Underestimation of anisotropy for LOD0 is consistent with prior low LOD modelling comparisons to observations (e.g. Krayenhoff and Voogt, 2016).

As anisotropy from surfaces’ both view fractions (\( f_i(\phi, \theta) \), Appendix C) and temperatures (\( T^\text{3D} \), Eq. 5) drives \( \Delta T^\text{bEO} \), these are explored to understand the differences in anisotropy in response to LOD (Fig. 8). LOD2 has the smallest roof view fraction (\( f^\text{roof} \), Fig. 9g) as pitched roofs and awnings (etc.) with a deviation of >45° from horizontal are classified as a wall (Appendix A), with the lower roof fractions offset by higher fractions of wall. LOD2 \( f^\text{roof} \) is the most anisotropic, decreasing from 0.31 at nadir to 0.27 for a view of south-facing surfaces (\( \phi = 47.1°, \theta = 214.1° \); Fig. 9g). At nadir the tops of any convoluted roofs are most visible, but with increasing view angles lower roof structures can be occluded by other roof features. Comparing across all azimuth angles at \( \phi = 47.1° \), LOD2 \( f^\text{roof} \) varies between 0.27 → 0.32.

LOD1 and LOD0 \( f^\text{roof} \) are near-isotropic (~0.02 range, Fig. 9h, i), consistent with assumptions made in most parametric models and idealised 3D. This makes \( f^\text{roof} \) approximately same as the plan area index for any direction (Hu and Wendel, 2019; Wang and Chen, 2019). \( f^\text{ground} \) is generally consistent across LODs (Fig. 9d–f).

\( T^\text{3D} \) varies between LODs even when using the same surface temperature distribution (\( T^\text{3D} = \text{ILU} \)), as differences in surface geometry translate into solar illumination patterns (e.g. through changes in sunlit and shaded fractions). To investigate these LOD effects, \( T^\text{bEO}(\phi, \theta) \) is separated by component directional brightness temperatures (\( T^\text{bEO}(\phi, \theta, i) \)). While \( T^\text{bEO}(\phi, \theta) \) uses the radiance from all image pixels (Eq. 3, 4), \( T^\text{bEO}(\phi, \theta, i) \) only uses the pixels that contain surface type \( i \) (Appendix C). 

LOD2 \( T^\text{bEO}(\phi, \theta, i = \text{Roof}) \) hence isolates the contribution of a given facet type to the variations in anisotropy.
vary most with view angle (Fig. 10a, green vertical bars; Fig. 10b x-axes red points). Their pitched, micro-scale structure gives a range ($\Lambda$) of 0.6 K at 08:00, increasing to $\Lambda$ = 2.3 K (09:00) with later maximum of $\Lambda$ = 3.4 K (14:00). Whereas, LOD1 roofs maximum $\Lambda$ is 1.5 K (14:00), while LOD0 roof $\Lambda$ is always < 0.3 K as there is no variation in the roof view fraction or surface temperature (i.e. $f_i$ = roof, Fig. 9, or $T_{bEO}(\phi, \theta, i = \text{Roof})$, Fig. 10a).

LOD2 roofs have a cool bias of over 5 K around midday. This is explained by high albedo “cool” surfaces (Appendix B, ~17.9% of total roof area, Morrison et al. (2021)) along with micro-scale geometry effects of self-shadowing, particularly from sloped surfaces towards/away from the sun (e.g. compare Fig. 6 b, d).

For wall and ground components, all LODs have directional brightness temperature variations (Fig. 10a) as for each view direction different shaded/sunlit fractions are seen. Brightness temperatures for LOD2 ground are lower particularly at night – as LOD2 has a 0.17 grass fraction (Table 1) which has a relatively low surface temperature (Fig. B-1), whereas in the other LOD grass surfaces are unaccounted for. There is some unexplained azimuth variation in LOD1 wall and ground view fractions (Fig. 9b, e) perhaps from a bias in certain building orientations which, in central London, would be reduced when using a larger domain area containing more streets and buildings.

The combined anisotropy from walls and ground of LOD2 (Fig. 10b, blue) is similar to that of LOD1 and LOD0 (MAE$_{LOD1}$ = 0.15, MAE$_{LOD0}$ = 0.26 K) and thus contributes less to the overall inter-LOD $\Delta T_{bEO}$ differences (Fig. 8). The generally high correlation between all landscapes (Fig. 8) is further understood through analysis of inter-landscape view fractions (Fig. 9) and facet temperatures (Fig. 10) which combined (e.g. Eq. (5) give rise to the observed anisotropy.

3.2.3. Vegetation

To investigate the impact of vegetation density on daytime anisotropy (Fig. 11) we compare a baseline $\Delta T_{bEO}$ simulation with complex geometry but no vegetation ($\Delta T_{bEO}(\text{LOD} = 2, \text{LAD} = 0)$) to cases with varying leaf area density (LAD). Generally, the baseline $\Delta T_{bEO}$ has the most variation through time and with view angle. Adding vegetation reduces the anisotropy (consistent with Dyce and Voogt (2018)) with greater reductions where $\Delta T_{bEO}$ > 0 K (Fig. 11, x-axes). For these viewing directions, the landscapes with LAD > 0 have $\Delta T_{bEO}$ around 0.4–0.6 K less than the baseline. Once vegetation is accounted for, there is little sensitivity to LAD (Fig. 11, colours) and LOD (Fig. 11, columns).

4. Conclusions

Urban geometry and surface temperature data are used to simulate directional variations of satellite brightness temperature images - the effective thermal anisotropy. Three-dimensional (3D) modelling of urban form and thermal radiative transfer processes using the Discrete Anisotropic Radiative Transfer (DART) model are used to explore the
relative importance of the geometry description, surface temperature representation and presence of vegetation. The study demonstrates these processes for a mainly clear-sky summer day in central London when high-resolution measurements were available.

For the first time, modelling of effective thermal anisotropy is not constrained to idealised descriptions of urban form and temperature. A realistic geometry with sub-facet features (e.g. pitched roofs and 3D vegetation canopies) is used as a reference standard to assess implications of using highly idealised urban geometry descriptions, such as repeating cube buildings, similar to what may be assumed in operational corrections of effective thermal anisotropy.

The 420 m × 420 m study area is similar to the larger central city surroundings (3 km × 3 km around the study area), based on morphometric parameters (e.g. building height, plan area) variability (defined here by interquartile range), except for tree cover (17%) that is within the 75th – 80th percentile. If similar detailed 3D model information and very high-resolution surface temperature data were available for a wider range of urban forms, the current simulations and analyses could be extended to capture a more representative diversity of intra- and inter-city variations in thermal anisotropy. However, such data do not yet exist for extensive areas.

Simulations of satellite, or Earth Observation (EO), views of the surface are used to quantify the effective anisotropy, defined as the difference in brightness temperature \( T_b \) between a view direction that is off-nadir (oblique) and a nadir (downward) view direction. The simulations use classified surface temperatures observations, whose allocation includes shadow state obtained from simulations considering either (1) known histories, or (2) instantaneous patterns. Although the anisotropy “hot spot” is generally broader if shadow history throughout the day is accounted for, both have close daytime agreement (MAE = 0.2 K). This allows the conclusion that instantaneous shadow patterns are a reasonable simplification when assigning surface temperatures in this urban setting in DART.

With instantaneous shadows as the basis to assign the facet temperature distributions, the role of the level of detail (LOD) of the building geometry on anisotropy is analysed based on three cases: realistic buildings (LOD2), planar roofs/walls (LOD1) and repeating cubes (LOD0). Consistent with earlier studies, anisotropy increases with increasing morphology detail. Simulated anisotropy using LOD1 is in closer agreement (daytime MAE = 0.16 K) to LOD2 than when using LOD0 (daytime MAE = 0.44 K).

The contribution of each facet type (roof, wall, ground) to the effective anisotropy is quantified for the three LOD. Changes in roof geometry complexity between LOD2 and LOD1 become apparent but in general both LOD lead to similar directional variations in the fraction of wall, roof and ground “seen” by the satellite (view fraction). LOD2 roof temperatures are generally cooler (on average 5 K cooler around midday) because of micro-scale shadowing. This micro-scale shadowing cool bias is the same order of magnitude as prior observational analysis. LOD2 results have more anisotropy than the flat LOD1 (and LOD0) roofs. Daytime directional brightness temperatures for the LOD2 roofs have a maximum 3.4 K range (14:00) compared to 1.5 K (0.2 K) for LOD1 (LOD0) (also at 14:00). The thermal anisotropy for the combined wall and ground facets are more consistent between LODs.

Including vegetation (trees, shrubs taller than 2 m) reduces the anisotropy for the daytime hot spot directions by around 0.4–0.6 K. Anisotropy is generally insensitive to variation in leaf area density, but future work should use the 3D radiative transfer modelling capabilities to investigate additional vegetation parameters (sunlit and shaded distributions, optical properties, leaf angular distributions, tree trunks and branches). Overall, vegetation is less important than LOD variation.

In this study, vegetation (median height = 10.01 m) is generally shorter than the buildings (median height = 13.49 m). Where vegetation frequently exceeds building heights (e.g. some residential settings) it may have greater implications on the effective thermal anisotropy because it would affect the roof fraction “seen” by the satellite.

Surface temperatures are prescribed based on several micrometeorological processes (solar illumination, shadow history, materials). Future studies should include broader spatial extents from airborne measurements that are spatially and temporally filled with facet-scale surface temperatures from energy balance models. Exploring the relative importance of geometry under different weather and climate conditions requires more observations. For example, the sensitivity of roof geometry to sun angle may differ during low winter sun angles.

This work has implications for how satellite based EO surface temperatures should be interpreted within urban areas and how EO data could be used in data assimilation and model evaluation in the future. Modelled thermal anisotropy using the easily derived LOD0 data are shown to give rapid and reasonable estimates compared to the more realistic cases. However, care should be taken using these lower LOD urban forms without prior evaluation at higher LOD. Expansion of the methods across different geometry and material emissivity configurations could test if the idealised LOD0 cases are applicable globally. There is scope for improving the material description of the realistic LOD2 cases, using increasingly available surface emissivity datasets through airborne and high-resolution satellite products. Implications of using idealised bulk emissivities can be explored, given highly reflective and specular surfaces common in cities (e.g. metals, glass) are expected to play a role in LST view angle sensitivity.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request on zenodo.org (10.5281/zenodo.7896671).

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Appendix A. Properties and description of the landscapes

To characterize the landscape opaque surfaces (e.g. buildings, roads) a vector-based 3D digital surface model (DSM) consisting of a 3D mesh of triangles is used. The vegetation canopy elements (VCE, any vegetation taller than 2 m) are a voxel array with \( \Delta X = \Delta Y = 1 \text{ m} \) and \( \Delta Z = 0.1 \text{ m} \) resolution.

The spatial temperature and optical properties are resolved across voxels of uniform size in a 3D array at high resolution (\( \Delta X = \Delta Y = \Delta Z = 1 \text{ m} \)). The spatial resolution of the landscape is the portion of digital surface model (DSM) triangles that occupies the volume of one surface voxel (a “surface element”). The voxel array stores the surface temperature distribution and a series of surface properties as a surface component (Table 4). Each surface element is assigned three properties: orientation and material (\( \Sigma \)), sun-surface geometry (bidirectional reflectance factor, BRF) and shadow history (time in shade, \( t_{\text{shd}} \) (units = min)) which are all used to inform the upscaling of observed surface temperatures. The three properties combine to a unique surface component \( i \) at timestep \( t \) resulting in a 3D voxel array of surface components. By using surface elements, surface features such as geometry, material, optical and temperature properties can be determined at a flexible spatial resolution, instead of at the triangle scale of the DSM (e.g. radiosity models of Emig (2017); Ghandehari et al. (2018); SOLENE model of Henon et al. (2012)).

Optical properties at a wavelength of 11.02 \( \mu \text{m} \) are used, corresponding to the centre of MODIS (Moderate Resolution Imaging Spectroradiometer) band 31 (10.780–11.280 \( \mu \text{m} \)). For grass surfaces in LOD2 geometry, an emissivity based on the mean of all dry grass samples (\( f_{11.02\mu m} = 0.955 \)) in the MODIS UCSB (University of California, Santa Barbara) spectral library (Wan et al., 1994; Snyder et al., 1997) is used. As the surface material and associated emissivity are not well known for other DSM elements, the mean spectral emissivity (\( f_{11.02\mu m} = 0.933 \), min = 0.900, max = 0.968, \( n = 60 \)) from all non-metal and non-plastic impervious materials in the SLUM spectral library (Kotthau et al., 2014) is used.

The vegetation optical properties are parameterised using a spatially homogeneous turbid representation of leaves with a spherical angular distribution (Wang et al., 2007; Pisek et al., 2011) within each vegetation voxel. Leaves are given “deciduous leaf” optical properties from the DART spectral database (leaf transmissivity = 0.0145, reflectance = 0.0195) with a leaf area density (leaf area within voxel / voxel volume (\( \text{m}^2 \text{m}^{-3} \))) (Lalic and Mihailovic, 2004; Jeanjean et al., 2017).

The downwelling longwave radiation across the landscape is assigned a predetermined isotropic source of downwelling spectral radiance received from a horizontal layer of the atmosphere that intersects the first vertical voxel layer above the landscape features (the bottom of atmosphere, BOA). The spectral radiance is determined from broadband longwave observations at the site (Morrison et al., 2020).

Appendix B. Landscape-wide M21 surface temperature

A surface temperature \( (T_s) \) of surface component \( (i) \) at timestep \( (t) \) \( (T_s(i, t)) \) is allocated to a 3D voxel array of surface temperature \( (T_s(X, Y, Z, t)) \). An additional 3D voxel array that describes the surface components \( (i(X, Y, Z, t)) \) is used. Some surface component voxels can be ambiguous as they can contain DSM triangles with (e.g.) multiple surface orientations. For example, a voxel at the edge of a roof may contain a DSM triangle with both “south” and “north” wall properties. In these cases, when determining \( T_s(X, Y, Z, t) \), the mean temperature of all surface components involved is allocated.

B.1. Shadow history

The time series of binned bidirectional reflectance factor (BRF) in three-dimensions (\( \text{BRF}(X, Y, Z, t) \)) is used to estimate the time a surface element (Appendix A) has spent in shade (\( t_{\text{shd}} \) min). \( \text{BRF}(X, Y, Z, t) \) is compared to the prior timestep \( \text{BRF}(X, Y, Z, t−5 \text{ min}) \). If a surface element becomes shaded at time \( t \), it has spent \( t_{\text{shd}}(X, Y, Z, t) = 5 \text{ min} \) in shade. For the timestep prior to this \( (t−5 \text{ min}) \), the surface element has spent zero minutes in shade and has \( t_{\text{shd}}(X, Y, Z, t−5 \text{ min}) = 0 \text{ min} \). A surface element that continues to be in shade [i.e. \( \text{BRF}(X, Y, Z, t+5 \text{ min}) = -1 \)] has \( t_{\text{shd}}(X, Y, Z, t+5 \text{ min}) = 10 \text{ min} \) at the next timestep, etc.

A surface element can be part sunlit and part shaded, even across multiple timesteps. However, each voxel is reassigned as fully sunlit or fully shaded if appropriate based on a 50 min window around each timestep. Otherwise, if a surface element has \( \text{BRF}(X, Y, Z, t) > -1 \), is sunlit at \( t−25 \text{ min} \) and shaded at \( t+25 \text{ min} \), it is assumed the surface element could be partially sunlit. In these cases, the following threshold is used to determine if the surface element is more shaded than sunlit, and used to update \( t_{\text{shd}} \) by:

\[
 t_{\text{shd}}(X, Y, Z, t) = \begin{cases} 
 0 & \text{if } \text{BRF}(X, Y, Z, t) < 0.75 \times \text{BRF}(X, Y, Z, t−25 \text{ min}) \\
 5 & \text{otherwise}
\end{cases}
\]

(B-1)

When \( t_{\text{shd}}(X, Y, Z, t) = 0 \), surface elements are allocated the maximum \( \text{BRF}(X, Y, Z) \) that occurred up to 5 timesteps prior (i.e. \( \text{max} \{\text{BRF}(X, Y, Z, t−25 \text{ min} \rightarrow 0)\} \) ) to assign partially shaded surfaces with a fully sunlit status.

Observations are aggregated based on their classification for the complete landscape surface to give a 3D surface temperature distribution \( (T_{\text{D}}(X, Y, Z, t)) \) (Morrison et al., 2021) aggregated to give temperatures stratified by surface component \( (T_s(i, t)) \) (Fig. B-1). Where a given surface component was not observed, \( T_s(i, t) \) is gap-filled to ensure a temperature can be allocated to all surface elements.

Initial per-pixel surface temperature aggregation uses \( \Sigma \) and \( \text{BRF} \) for each timestep \( (T_s(\Sigma, \text{BRF}, t)) \), excluding “mixed” and/or “masked” pixels. As there are more \( T_s(\Sigma, \text{BRF}, t_{\text{shd}}) \) combinations than observed, a shaded temperature \( (T_s(\Sigma, \text{BRF} = -1, t)) \) is used.
Fig. B-1. Surface component temperatures used as input for the three-dimensional surface temperature ($T_{s3D}$) parameterisations with the range (vertical lines) of possible sunlit and recently shaded values that are used in the M21 parameterisation (Table 4), according to sun-surface geometry and time in shade and their mean (green points), with the ambient or “well shaded” surface temperature (red points) used in M21 and ILU and the ILU sunlit temperature (blue points) for bidirectional reflectance factor (BRF) of 1 (i.e. surface temperature representative of horizontal surfaces). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

B.2. Gap-filling surface component temperatures

As observations do not cover all possible facets of the entire study area (i.e. more surface component permutations exist in 3D than are observed) gap-filling is required. With no downward facing surfaces (e.g. underside of balconies) sampled by any camera, ‘all shaded walls’ observations are used for this class of per-pixel gap-filling. Further gap-filling details of the observed surface temperature are given in (Morrison et al., 2021).

Appendix C. Calculation of surface component radiance and view fractions

The fraction of surface type $i$ seen within an image ($f_i$) impacts directional variation in urban LST. If $f_i$ for a nadir viewed urban surface has a plan area index of 0.5 (i.e. $f_{Roof} = 0.5$) and the remainder is ground, then $f_{Ground} = 0.5$, (i.e. all seen types equal 1). These values and components will change with view angle.

The simplest method to determine $f_i$ for a given view angle ($f_i(\phi, \theta)$) is to sum the number of pixels per surface class $i$ (e.g. $L_{surf}(x, y, \phi, \theta, i)$) and calculate a fraction relative to the total image pixels. However, this is inaccurate if an image pixel has surface-leaving radiance contributions from more than one surface component: the view fraction can be double-counted. Approaches to address this include: sensor view “sub-patches” (Krayenhoff and Voogt, 2016) assuming all components of a “mixed” pixel has the same temperature; and sensitivity tests to a “counted” $f_i$ to the resolution of surface components derived from simulated RGB renders (Lagouarde et al., 2010).

Here we adopt a radiative transfer and energy conservation approach to calculation of $f_i$, using DART simulations. DART radiance images are calculated per surface component ($L_{surf}(x, y, \phi, \theta)$) and have surface-leaving radiance contribution after all scattering iterations. Whereas, $L_{surf}$ (Eq. 3)
will always have the combined radiance contribution from all surface components. \( L_{\text{surf}}^i(\phi, \theta) \) is related to \( L_{\text{surf}}^o(\phi, \theta) \) by:

\[
L_{\text{surf}}^o(\phi, \theta) = \frac{1}{n_{\text{pix}}} \sum_{n_{\text{pix}}} L_{\text{surf}}^i(\phi, \theta, x, y) \tag{C-1}
\]

\[
L_{\text{surf}}^i(\phi, \theta) = \sum_{n_{\text{pix}}} L_{\text{surf}}^i(\phi, \theta) \tag{C-2}
\]

i.e. the mean across all \((n_{\text{pix}})\) \( L_{\text{surf}}^i \) image pixels is \( L_{\text{surf}}^o(\phi, \theta) \) (Eq. C-1) and the sum of all \((n_{\text{img}})\) \( L_{\text{surf}}^i \) images is \( L_{\text{surf}}^o(\phi, \theta) \) (Eq. C-2). \( L_{\text{surf}}^i \) pixels without surface component \( i \) have \( L_{\text{surf}}^i(x, y, \phi, \theta, i) = 0 \). \( L_{\text{surf}}^i \) pixels containing only a fraction of surface component \( i \) will have the associated fractional radiance contribution, which is more accurate than the aforementioned “simple approach” that resolves pixel-level view fractions.

A DART simulation for each landscape LOD is run in the thermal domain (11 \( \mu \)m) with a known isothermal temperature across all surfaces (\( T_{3D} = 300 \) K). All \( L_{\text{surf}}^i \) images have radiance \( B^{-1}(300 \text{ K}, \lambda = 11 \mu \text{m}) = 9.57 \text{ W m}^{-2} \text{ sr}^{-1} \mu \text{m}^{-1} \). With this total radiance contribution known and held constant, \( L_{\text{surf}}^i(x, y) \) is then a fraction of \( L_{\text{surf}}^o(x, y) \):

\[
f_i(x, y, \phi, \theta) = L_{\text{surf}}^i(x, y, \phi, \theta) / L_{\text{surf}}^o(x, y, \phi, \theta) = 9.57 \cdot \text{C-3}
\]

Across a whole image with \( n_{\text{pix}} \) pixels, the view fraction of a surface component \( f_i(\phi, \theta) \) is:

\[
f_i(\phi, \theta) = \frac{1}{n_{\text{pix}}} \sum_{n_{\text{pix}}} f_i(x, y, \phi, \theta) \tag{C-4}
\]

and the sum of \( n \) surface component fractions is unity:

\[
\sum_i f_i(\phi, \theta) = 1 \tag{C-5}
\]

The post-processing of these DART simulations is done in \( R \) using the daRt package (Morrison and Benjamin, 2020).

Appendix D. Satellite brightness temperature by surface component

The surface component directional brightness temperature \( T_{\text{B}i}(\phi, \theta, i) \) considers the radiance contribution from image pixels of surface component \( i \) only. The DART radiance images \( L_{\text{surf}}^i(x, y, \phi, \theta, i) \) are processed to have their pixels indexable by surface component \( i \) (Table 4) as \( L_{\text{surf}}^i(x, y, \phi, \theta, i) \), which is first used to determine the image average radiance for a given surface component \( L_{\text{surf}}^i(\phi, \theta, i) \):

\[
L_{\text{surf}}^i(\phi, \theta, i) = \frac{1}{n_{\text{pix}}} \sum_{n_{\text{pix}}} L_{\text{surf}}^i(x, y, \phi, \theta, i). \tag{D-1}
\]

Here \( n_{\text{pix}}(i) \) is the number of pixels in the image that have a majority radiance contribution from surface component \( i \) \((f_i(x, y, \phi, \theta) > 0.5, \text{Eq. C-3})\). Finally, \( T_{\text{B}i}(\phi, \theta, i) \) is calculated from the inverse Planck function of \( L_{\text{surf}}^i(\phi, \theta, i) \) at the simulation wavelength (Eq. 6). Note: \( L_{\text{surf}}^i(x, y, \phi, \theta, i) \) differs from \( L_{\text{surf}}^o(x, y, \phi, \theta, i) \) (Appendix C).

Appendix E. Supplementary data

Supplementary data to this article can be found online at https://doi.org/10.1016/j.rse.2023.113579.

References


