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# A control structure for bilateral telemanipulation 

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#### Abstract

A framework for considering the stability of bilateral telemanipulator systems is considered. The approach adapts the work of Lawrence[3] to use a state-space formulation thus simplifying the identification of the stability conditions from the eigenvalues of the feedback system. Both numerical and symbolic stability conditions are considered.


Keywords: bilateral telemanipulator, control, stability

## 1 Background

Telemanipulator theory forms the basis for applications that include remote handling, surgical robots, exoskeletons and haptic systems[5]. In many cases, to avoid the complexity of the control system, the system operates as a strict master-slave system where position coordinates are generated by the master and the slave is servoed to follow these positions. In such cases the operator must rely on visual feedback when contact is made between the slave and the remote environment. Better control can be achieved when position and force information available at the slave is directed back to the master. One example is the OOEC Magpie[1] which is a foot operated assisted dining device that give direct mechanical feedback of forces encountered by the eating utensil to the operator's foot. A similar principal applies to orthotic devices such as the Wilmington Robotics Exoskeleton (WREX)[4] where there is a close coupling between the orthosis and the arm.

In more complex telemanipulator systems some form of closed-loop control around the actuator mechanisms is needed. In most cases this is based on position feedback control of small permanent magnet motors. Where there is backdrivable transmission between the motor and the linkage joint it is possible to estimate the external forces applied to the linkage[6], and these forces can then be reflected into the associated master or slave.

Lawrence[3] identified four connections that can be made between the master and slave of a backdrivable linkage telemanipulator system that can then allow permutations of position, force, impedance or admittance to be reflected into the master and slave systems.

## 2 Simplified structure of a master-slave telemanipulator

A variation of the Lawrence[3] control structure is shown in Fig 2 It consists of


Fig. 1. Bilateral telemanipulator as a coupled control system. The upper system ( $C_{1}$ $P_{1}$ ) will be considered as the master and the lower as the slave although in general the master and slave can be exchanged without loss of generality
two control systems that are assumed to be backdrivable. Thus the upper part of the figure (the master) consists of a plant $P_{1}$ that is assumed to contain the robot linkage and transmission, and the controller $C_{1}$ is assumed to also include the characteristics of the actuator. Evidently with this structure in a unity closedloop feedback system as shown it is possible to show that the position gain $y_{1} / u_{1}$ is given as

$$
y_{1}=\left(1+P_{1} C_{1}\right)^{-1} P_{1} C_{1} u_{1}
$$

Thus under a restricted set of conditions $P_{1} C_{1}$ can be considered to dominate with respect to unity and the output will try to match the input. These conditions require a high controller gain without local instability so are likely to be realised when the system is tuned with an algorithm such as Zeigler-Nichols. In a similar argument the gain due to the 'disturbance' $f_{1}$ can be expressed in the form

$$
y_{1}=\left(1+P_{1} C_{1}\right)^{-1} P_{1} f_{1}
$$

and in this case with the same restricted set of conditions the admittance of the mechanism, the position response to the disturbance force $f_{1}$, can be considered to be $C_{1}$. The controller gain can be seen to relate directly to the impedance (stiffness) of the closed-loop system and inversely to the admittance.

The four gains $k_{1}, k_{2}, k_{3}, k_{4}$ in the controller structure shown in Fig 2 can be considered in two parts. Gains $k_{1}$ and $k_{2}$ simply set the position demand, master to slave and slave to master. To assess the effect of the remaining two gains $k_{3}$ and $k_{4}$ it should be noted that the gains $k_{1} k_{4}$ supplement the controller $C_{1}$ and the gains $k_{2} k_{3}$ supplement the controller $C_{2}$. With this adaption the impedance of the master can be considered to be set by $C_{1}\left(1+k_{4} k_{1}\right)$ and the stiffness of
the slave is set by $C_{2}\left(1+k_{2} k_{3}\right)$. Alternatively the two controller gains $k_{1}, k_{3}$ can be chosen to be an estimate of $f_{1}$ and scaled to be a force demand of the slave with a similar argument for the gains $k_{2}, k_{4}[6]$.

Thus it can be seen that forces or positions from the master can be reflected into the slave, and vice versa.

### 2.1 A simplified state-space representation of a bilateral telemanipulator.

If we assume each 'plant' is a mass and damper so $\dot{x}=A x+B \epsilon$ and $y=C x$. This assumption provides a minimal system that uses Newton's second law along with the damper to provide a channel for the energy dissipation.

If each system has two states and decoupled we can generate a combined state matrix
where $x=\left[\begin{array}{llll}x_{1} & \dot{x_{1}} & x_{2} & \dot{x_{2}}\end{array}\right]^{T}$ and $\epsilon=\left[\begin{array}{ll}\epsilon_{1} & \epsilon_{2}\end{array}\right]^{T}$
For example the figure without the gain terms $k_{1}$ to $k_{4}$ could be considered as

$$
A=\left(\begin{array}{cccc}
0 & 1 & 0 & 0  \tag{1}\\
0 & -b_{1} & 0 & 0 \\
0 & 0 & 0 & 1 \\
0 & 0 & 0 & -b_{2}
\end{array}\right) \quad B=\left(\begin{array}{cc}
0 & 0 \\
c_{1} & 0 \\
0 & 0 \\
0 & c_{2}
\end{array}\right)
$$

The output matrix $C$ then selects outputs $y_{1}$ and $y_{2}$

$$
C=\left(\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 0 & 1 & 0
\end{array}\right)
$$

A gain matrix can be identified from

$$
\left[\begin{array}{cc}
1 & -k_{4} \\
-k_{3} & 1
\end{array}\right]\left[\begin{array}{l}
\epsilon_{1} \\
\epsilon_{2}
\end{array}\right]=\left[\begin{array}{cc}
-1 & k_{2} \\
k_{1} & -1
\end{array}\right]\left[\begin{array}{l}
y_{1} \\
y_{2}
\end{array}\right]
$$

That is $\epsilon=K y$ where

$$
K=\binom{-\frac{k_{1} k_{4}-1}{k_{3} k_{4}-1}-\frac{k_{2}-k_{4}}{k_{3} k_{4}-1}}{-\frac{k_{1}-k_{3}}{k_{3} k_{4}-1}-\frac{k_{2} k_{3}-1}{k_{3} k_{4}-1}}
$$

The feedback gain and original system can be combined to for a new statespace system of the form.

$$
\dot{x}=(A-B K C) x+B K r
$$

So the revised A matrix is

$$
A^{\prime}=\left(\begin{array}{cccc}
0 & 1 & 0 & 0  \tag{2}\\
\frac{c_{1}\left(k_{1} k_{4}-1\right)}{k_{3} k_{4}-1} & -b_{1} & \frac{c_{1}\left(k_{2}-k_{4}\right)}{k_{3} k_{4}-1} & 0 \\
0 & 0 & 0 & 1 \\
\frac{c_{2}\left(k_{1}-k_{3}\right)}{k_{3} k_{4}-1} & 0 & \frac{c_{2}\left(k_{2} k_{3}-1\right)}{k_{3} k_{4}-1} & -b_{2}
\end{array}\right)
$$

We can crosscheck see it is still stable by setting the $k$ gains to 0 and testing the eigenvalues, which require negative real part of the expression $-\frac{b_{1}}{2} \pm \frac{\sqrt{b_{1}^{2}-4 c_{1}}}{2}$ Setting any one of the gains $k_{1}, k_{2}, k_{3}, k_{3}$ to be non zero makes no change to the eigenvalues and hence to the system stability.

The eigenvalues of the full system 2 where all the gains $k_{1}, k_{2}, k_{3}, k_{3}$ are set, can be computed in Matlab but are too large to be of any value.

### 2.2 A strict symmetrical bilateral telemanipulator

By setting the master and slave to have identical components as well as ensuring $k_{2}=k_{1}$ and $k_{4}=k_{3}$ we get a symmetrical bilateral telemanipulator. In this case the eigenvalues relatively simple, that is

$$
\begin{aligned}
& \lambda=-\frac{b_{1}}{2} \pm \frac{1}{2} \sqrt{4 C_{1} \frac{1+k_{1}}{k_{3}-1}+{b_{1}}^{2}} \\
& \lambda=-\frac{b_{1}}{2} \pm \frac{1}{2} \sqrt{4 C_{1} \frac{k_{1}-1}{k_{3}+1}+{b_{1}}^{2}}
\end{aligned}
$$

The four values come about because $k_{1}$ and $k_{3}$ range from 0 to $\infty$ Evidently setting $k_{3}= \pm 1$ would result in an unstable response.

Essentially need the $C_{1}$ term to be negative. $C_{1}$ itself must be positive so $k_{1}$ must be less than 1 and $k_{3}$ greater than 1 . This strict arrangement is of limited value.

### 2.3 A simplified identical bilateral telemanipulator

A further simplification is to make the master and slave identical so that the controllers $c_{1}$ and $c_{2}$ are the same proportional gain, and both plants have a the same damping term. Under these conditions the eigenvalues are considerably simpler and the four values can be computed as.

The revised A matrix becomes

$$
A^{\prime}=\left(\begin{array}{cccc}
0 & 1 & 0 & 0 \\
-\frac{c_{1}\left(k_{1} k_{4}-1\right)}{k_{3} k_{4}-1} & -b_{1} & -\frac{c_{1}\left(k_{2}-k_{4}\right)}{k_{3} k_{4}-1} & 0 \\
0 & 0 & 0 & 1 \\
-\frac{c_{1}\left(k_{1}-k_{3}\right)}{k_{3} k_{4}-1} & 0 & -\frac{c_{1}\left(k_{2} k_{3}-1\right)}{k_{3} k_{4}-1}-b_{1}
\end{array}\right)
$$

so the eigenvalues are

$$
\lambda=-\frac{b_{1}}{2} \pm \frac{1}{2} \sqrt{\frac{4 c_{1}+2 c_{1} \beta-b_{1}^{2}-2 c_{1} k_{1} k_{4}-2 c_{1} k_{2} k_{3}+b_{1}^{2} k_{3} k_{4}}{k_{3} k_{4}-1}}
$$

where

$$
\beta= \pm \sqrt{{k_{1}^{2}}^{2} k_{4}^{2}-2 k_{1} k_{2} k_{3} k_{4}+4 k_{1} k_{2}-4 k_{1} k_{4}+{k_{2}}^{2} k_{3}^{2}-4 k_{2} k_{3}+4 k_{3} k_{4}}
$$



Fig. 2. Movement of eigenvalues towards the positive real axis. Test conditions are $m_{1}=m_{2}=1, b_{1}=.2 b_{2}=.24, c_{1}=c_{2}=.1, k_{1}=2, k_{3}$ is set to the values -1.501 and 1.5. $k_{4}$ is varied between -0.1 and 0.5 . Note that for values of $k_{3}$ below 1.5 the eigenvalues all move across into the positive half plane. Thus unusually a higher gain results in a more stable system, however this is at the expense of the forward position gain of the master-slave system.

## 3 Numerical simulation

Further insight is possible by numerical simulation. It is first assumed that the master and slave are independently stable via the linear controllers $c_{1}$ and $c_{2}$. Although the numerical simulation could enforce the master and slave to have identical plant and controller gains, a slightly less restrictive condition is investigated where the master and slave are simply close (in the sense of the damping values $b_{1}$ and $b_{2}$ having similar values. The simulations are all done with $k_{1}$ set to 2 so there is a position magnification of 2 .

## 4 Discussion

In reality exoskeletons and telerobotics are non-linear thus further complicating the stability analysis. Local stability can be considered by linearising around a set of operating points however it is unlikely that a completely general stability condition can be set, in particular once other nonlinear effects start to manifest, in particular the discontinuous forces that result from the slave making contact with the environment. It is possible that gain scheduling via Linear parametervarying control, or passivity estimators[2] may allow changing the gains to ensure stability of complete system across all operation modes.


Fig. 3. Step response of the numerical system with only the position forward gain $k_{1}$. The response in this case can be seen to be stable with the master acting as a second order system and the response from the slave following a forth order response.

## 5 Conclusions

This paper outlines the control considerations for a bilateral force reflecting feedback mechanisms, in particular the eigenvalues of a simple telemanipulator with no attempt to convey slave forces back to the operator, and a force feedback approach that uses the controller error term as an indication of impedance. The paper outlines a convenient state-space representation of a simple master-slave telemanipulator that facilitates analysis.
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