

The effects of variation in snow properties on passive microwave snow mass estimation

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1 Title: The effects of variation in snow properties on passive microwave snow mass estimation

2
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7
8 **Abstract**

9
10 Estimating snow mass at continental scales is difficult, but important for understanding land-
11 atmosphere interactions, biogeochemical cycles and the hydrology of the Northern latitudes.
12 Remote sensing provides the only consistent global observations, but with unknown errors. We test
13 the theoretical performance of the Chang algorithm for estimating snow mass from passive
14 microwave measurements using the Helsinki University of Technology (HUT) snow microwave
15 emission model. The algorithm's dependence upon assumptions of fixed and uniform snow density
16 and grainsize is determined, and measurements of these properties made at the Cold Land Processes
17 Experiment (CLPX) Colorado field site in 2002-2003 used to quantify the retrieval errors caused by
18 differences between the algorithm assumptions and measurements. Deviation from the Chang
19 algorithm snow density and grainsize assumptions gives rise to an error of a factor of between two
20 and three in calculating snow mass. The possibility that the algorithm performs more accurately
21 over large areas than at points is tested by simulating emission from a 25km diameter area of snow
22 with a distribution of properties derived from the snow pit measurements, using the Chang
23 algorithm to calculate mean snow-mass from the simulated emission. The snow mass estimation
24 from a site exhibiting the heterogeneity of the CLPX Colorado site proves only marginally different
25 than that from a similarly-simulated homogeneous site. The estimation accuracy predictions are

26 tested using the CLPX field measurements of snow mass, and simultaneous SSM/I and AMSR-E
27 snow pit measurements.

28

29 Keywords: snow, remote sensing, passive microwave

30

31 **1. Introduction**

32

33 Remote sensing is the only feasible way to monitor the global distribution of snow mass, which is
34 important for water resource management, environmental risk assessment and to determine the
35 sensitivity of climate to change (Randall et al., 2007). Comparisons between global models,
36 reanalysis data and satellite observations have revealed differences in distribution and magnitude of
37 snow water equivalent (Clifford, 2010), but errors in the observations must be quantified in order to
38 assess the accuracy of the models. Chang et al. (1987) used a simple model of soil/snow microwave
39 emission to devise a means for estimating snow water equivalent (SWE) in mm from passive
40 microwave measurements, by multiplying the difference between the horizontally-polarised 19GHz
41 and 37GHz emission by a factor of 4.77, assuming snow density of 300kgm^{-3} . This technique,
42 which we refer to here as the Chang algorithm, was recommended for snow no deeper than a metre,
43 approximately equivalent to a snow water equivalent of 300mm, due to increasing non-linearity in
44 the relationship around this depth. The Chang algorithm has, with minor variations, been
45 operationally used since 1987 to estimate snow mass globally from satellite observations from
46 instruments such as SSM/I and AMSR-E.

47

48 There have been a few comparisons between snow mass measured by the Chang algorithm and by
49 ground-based observation, showing both substantial over- and underestimation. Armstrong &
50 Brodzik (2000) found a substantial underestimation around 20-40% in SWE when applying the
51 Chang algorithm to snow in the former Soviet Union in the Winter 1988-89 season, for SWE

52 between 10mm and 100mm. Pardé et al. (2007) found the Chang algorithm to overestimate snow
53 mass with an RMSE of 40mm over Winter in 2002-2003 in Central Canada, for a range of SWE
54 between about 20mm and 150mm. They improved this to an RMSE of 12mm by incorporating a
55 simultaneous retrieval of snow grain size into an inversion of the Helsinki University of Technology
56 (HUT) model (Pulliainen et al., 1999). Butt (2009) demonstrated that a retrieval applying the Chang
57 algorithm to SSM/I observations of snow in the UK with a mean depth of 90mm (so a SWE
58 approximately 30mm), with depths up to 500mm, underestimated snow depth by a mean of 51%.
59 He also demonstrated an approach to resolving this by a simultaneous retrieval of snow grain size,
60 improving performance to a mean 11% overestimate. This seems to indicate a considerable range of
61 performance of the Chang algorithm, apparently dependent upon the physical characteristics of the
62 snow local to each study. We aim here to explore more generally the relationship between the
63 physical characteristics of snow and the efficacy of the Chang algorithm, illustrate how simulating
64 the retrieval can identify the flawed assumptions, and validate the approach by estimating snow
65 mass from remotely-sensed data in an area with an extensive set of physical measurements.

66

67 By modelling the emission of microwave radiation by a snowpack and the underlying ground, we
68 firstly test the dependence of the microwave emission of a snowpack/ground combination upon the
69 physical characteristics of the snow, using the Helsinki University of Technology (HUT) snow
70 microwave emission model, and use this to estimate how the Chang algorithm performance would
71 be affected by variation in snow properties. To evaluate the effects of this variation on snow mass
72 estimation, we also need to know how much variability in these properties is typically found in
73 snow. We study this by using the planimetrically extensive measurements made at snow pits in the
74 CLPX Colorado site in 2002-3. We examine how accurately the Chang algorithm would retrieve
75 snow mass from snow with these characteristics by simulating emission with the HUT emission
76 model driven by measured snow properties. Finally, we compare our predictions of the accuracy of

77 the Chang algorithm over the CLPX area to the application of the algorithm to SSM/I and AMSR-E
78 measurements.

79

80 2. *Methods*

81

82 2.1. *The sensitivity of the Chang algorithm to snow grain diameter and density*

83

84 Most SWE retrievals make use of an empirical retrieval first derived by Chang et al. (1987),
85 consisting of a linear fit to brightness temperatures at 18GHz and 37GHz, equation (1):

86

$$\text{SWE(mm)} = 4.77 (\text{TB}_{18\text{H}} - \text{TB}_{37\text{H}}) \quad \text{Equation (1)}$$

87

88 where $\text{TB}_{18\text{H}}$ refers to the microwave brightness temperature measured at 18GHz at horizontal
89 polarization, and $\text{TB}_{37\text{H}}$ refers to the microwave brightness temperature measured at 37GHz at
90 horizontal polarization. The gradient of the linear fit, in this equation 4.77, depends on the density
91 and grain diameter of the snowpack. Whilst it is clear that a density of 300 kg m^{-3} was used to
92 determine the gradient, the grain diameter used is uncertain. Chang et al. (1987) refer to a figure
93 which shows brightness temperature curves as a function of SWE for two different grain radii,
94 0.3mm and 0.5mm, and describe the algorithm as a linear fit from the data shown in the figure, but
95 it is not clear which grain radius, or whether a combination of both, were used. Many authors (e.g.
96 Foster et al., 1997, Kelly et al., 2003, Butt, 2009) have assumed this algorithm relates to a grain
97 radius of 0.3mm.

98

99 To test the effect of variation in grain diameter, we use the Helsinki University of Technology
100 emission model (Pulliainen et al., 1999) driven by a range of snow water equivalents and grain
101 diameters to simulate emission at 19 and 37GHz, 53° from vertical, and apply the Chang algorithm

to estimate snow mass from this emission, indicating how the algorithm is affected by snow grain diameter. To investigate the effects of variation in snow density, we use a fixed grain diameter and range of snow water equivalents and densities, and apply the Chang algorithm to the emission to retrieve snow water equivalent. For the purposes here, some parameters have a negligible effect (Parde et al., 2007), and are kept constant, eg. soil moisture is assumed $0.1 \text{ m}^3 \text{ m}^{-3}$, soil temperature 272.15K, snow temperature 263.5K, and snow salinity set to zero.

2.2 *The dependence of snow variability on planimetric scale*

A semi-variance analysis is used to examine the characteristic length scale of variability of measured snow properties, to test for evidence that certain spatial scales are more suitable than others for averaging snow properties and estimating snow mass. It is possible that the increased variability of snow properties over large areas mean that the remote sensing relationships with areal snow mass are different, possibly better, than the relationships found at an individual field site. We attempt to identify whether the range of snow properties measured has a strong dependence upon spatial scale by geostatistical analysis of snow properties. The semivariance $\gamma(d)$ for distance d of a set of spatially distributed measurements of $z(\underline{x})$ is given by comparing all pairs of measurements of z separated by d , of which there are $n(d)$, using equation (2).

$$\gamma(d) = \frac{1}{2n(d)} \sum_{i=1}^{i=n(d)} (z(\underline{x}_i + d) - z(\underline{x}_i))^2 \quad \text{Equation (2)}$$

The NASA Cold Land Processes Experiment (CLPX) experiment produced a large number of measurements of snow properties, mass, and other variables in Colorado over 2002-2003 (Cline et al., 2002, Cline et al., 2002a, Elder et al., 2009). Figure 1 shows a map of the area of the experiment, and the locations of the main field sites. There were four Intensive Observation Periods (IOPs) during the snow seasons, over the periods February 2002, March 2002, February 2003 and

127 March 2003. Anisotropic distance semivariograms were calculated from the measurements of mean
128 snow grain diameter in the top 5cm snow layer, snow water equivalent, snow depth, and mean snow
129 density throughout the pack, using the North Park Meso-cell Study Area (MSA) measurements
130 made during IOP3 over 20-23 Feb 2003. Three small intensive sets of measurements within this
131 area were excluded from this analysis, since when analysed separately they showed semivariance
132 consistently around double that of the rest of the measurements, suggesting a different measurement
133 technique with a higher measurement error.

134

135 2.3. *Calculation of mean snow properties*

136

137 The snow pit measurements made during all four Intensive Observation Periods over the entire area
138 of the CLPX experiment in Colorado were used to calculate the mean snow grain diameter and
139 density within a number of SWE classes. These classes were designed to each encompass snow
140 with a range of SWE with similar properties. Each snow pit measurement set included the minor
141 and major axis diameters of medium size grains, and the mean of these measurements down through
142 the snow layers is used here as representative of the site grain diameter. The depth-integrated mean
143 snow density at each site was used to calculate the mean density within each SWE class.

144

145 2.4. *The effects of measured snow properties on snow mass retrieval via the Chang algorithm*

146

147 To assess the effects of measured values of density and grain diameter on the accuracy of the Chang
148 algorithm, microwave emission at 19 and 37GHz at 53° from the vertical was simulated using the
149 HUT model, driven by the mean snowpit measurements of SWE, density and grain diameter within
150 the SWE classes described in Section 2.3. For each SWE class, we applied the Chang algorithm to
151 the modelled emission, and compared the SWE estimated by the algorithm to the SWE driving the
152 emission model. To distinguish between the effects of grain diameter and density, they were

153 separately changed within the forward model from the Chang algorithm assumptions to the
154 measured class mean values. This demonstrates, for any given SWE, how accurately the Chang
155 algorithm would estimate snow mass, depending on whether its assumptions of grain diameter and
156 snow density are correct, or whether one or both more closely correspond in reality to the
157 measurements on the CLPX site.

158

159 *2.5. The effect of heterogeneity in snow properties on snow mass retrieval via the Chang algorithm*

160

161 To test the hypothesis that the spatial heterogeneity in snow properties over a large area improves
162 the accuracy of the Chang algorithm, the microwave emission from a snowpack with the
163 distribution of SWE found within CLPX site was modelled. Having considered the case of a simple,
164 homogeneous snowpack, where the density and grain diameter are a function of SWE in Section 2.4
165 above, we here consider a more realistic heterogeneous snowpack, with the range of density and
166 grain diameter occurring in the CLPX site within each SWE class. We simulated this by estimating
167 probability density functions (PDFs) of these properties within each class, rather than, as in
168 Section 2.4, simply using the mean of class measurements. In this case, the relationship between
169 modelled and retrieved SWE was calculated for each class by modelling the emission for a range of
170 density/grain diameter combinations, 20 density values between 40kgm^{-3} and 400kgm^{-3} , and 27
171 grain diameter between 0.2mm and 5.4mm, and weighting the mean emission according to the
172 PDFs. This allows us to predict for a site with any given SWE, what the algorithm estimate of SWE
173 will be, if the site has a plausible distribution of grain diameter and density. The effect on the
174 overall SWE estimation from a site with the distribution of SWE measured within North Park MSA
175 during IOP3 was also calculated.

176

177 2.6. *Comparison of snow mass estimates from satellite data to ground measurements.*

178

179 We empirically tested the accuracy of the Chang algorithm by calculating the remotely-sensed SWE
180 for the site for each of the IOPs, using the SSM/I (Brodzik, 2003) and AMSR-E (Brodzik, 2003a)
181 measurements taken within the ground measurement time span. Armstrong & Brodzik (2001) show
182 that reducing the brightness temperature difference in this equation by 5K provides more accurate
183 results with SSM/I data, primarily because the algorithm was designed for 18GHz and 37GHz
184 measurements, rather than the 19GHz and 37GHz used by SSM/I and AMSR-E, and we apply this
185 correction in applying the algorithm.

186

187 3. *Results*

188

189 3.1. *The sensitivity of the Chang algorithm to snow grain diameter and density*

190

191 The Figure 2(a) ordinate shows the SWE used to simulate snowpack emission, the abscissa shows
192 the SWE that would be retrieved from this emission using the Chang algorithm, and the 1:1 line
193 represents a perfect retrieval. The retrieval which assumes a grain diameter of 0.8mm follows the
194 perfect retrieval 1:1 line closely for low SWE, which suggests that the algorithm constant proposed
195 in Chang et al. (1987) was chosen to work with a snow grain diameter of 0.8mm, or a radius of
196 0.4mm, mid-way between the two radii 0.3mm and 0.5mm showed in the figure. Using
197 Chang et al. (1987)'s Figure 1, it is easy to show that if only the 0.3mm radius emission curves had
198 been used to calculate the constant, as has been widely assumed, the ratio between SWE and
199 $(TB_{18H} - TB_{37H})$ would have been around 6, rather than the 4.77 given (after assuming snow density
200 of 300kgm^{-3}), yielding SWE estimates 26% higher than an estimate based on the 0.3mm radius

assumption. The coefficient given seems to derive from the mean of the ratio between SWE and $(TB_{18H} - TB_{37H})$ at 40cm SWE, averaged across both 0.3mm and 0.5mm snow grain radii.

Figure 2(b) shows the algorithm's sensitivity to variation in density assuming the grain diameter is fixed at 0.8mm. The effect ranges from underestimation at density of 400kgm^{-3} to overestimates of a factor of six at a density of 50kgm^{-3} . It can be seen that the algorithm is most accurate where the density and grain diameter exactly match the values used to formulate the algorithm, and that it starts to fail above about 150mm SWE. The suggestion in Chang et al. (1987) that the algorithm not be applied to snow depth greater than 1 meter, equivalent to approximately 300mm SWE given a snow density of 300kgm^{-3} , seems to be a judgment based on the degree of acceptable error, possibly around a SWE estimation error of 10%.

The relationships between modelled and estimated SWE shown in Figure 2 strongly suggest that the Chang algorithm constant was formulated to fit snow with a grain diameter of 0.8mm, rather than the 0.6m diameter, 0.3mm radius often assumed. The impact of this misinterpretation on subsequent work is probably small, as the range of snow grainsize found in work citing it (e.g. Foster et al., 1997, Kelly et al., 2003, Butt, 2009) is far larger than this discrepancy.

3.2. *The dependence of snow variability on planimetric scale*

The data density in the IOP measurements allowed semivariograms with reasonable uncertainty to be calculated between lags of 5km and 25km. These showed negligible change in semivariance of mean grain diameter, density and snow water equivalent over this lag range. Mean grain diameter showed a semivariance around 0.27mm^2 , regardless of distance lag, suggesting a standard deviation in measurements of 0.7mm which is invariant with sample spacing within the 5km-25km range. SWE semivariance varies little from 500mm^2 , snow depth semivariance is around 70cm^2 , and mean

227 density semivariance $3000\text{kg}^2\text{m}^{-6}$. This suggests that heterogeneity is scale-independent over the
228 5km-25km distance range. We have therefore not considered further the effect of spatial scale
229 within this work, as the sampling density within these data will not provide reliable results outside
230 this range.

231

232 The only other comparable work in geostatistical analysis of snow properties covers the northern
233 Great Plains region of the USA (Chang et al., 2005), and indicates that ground-measured snow
234 depth has a nugget (minimum) semivariance of about 100cm^2 , and reaches a sill (maximum) of
235 approximately 400cm^2 at a lag of 500km. The 70cm^2 snow depth semivariance in the CLPX
236 measurements indicates that they are more consistent than those taken during the Great Plains
237 fieldwork, possibly reflecting a more accurate measurement system. Assuming this to be the case,
238 the lack of a trend in semivariance across the 5km - 25km lag range would not be inconsistent with
239 the semivariance behaviour within the Great Plains data, which varied little over the same distance
240 range. The implication that might be deduced from this is that in order to estimate snow variability
241 over a 25km scale, sampling a sub-area of 5km should prove adequate. This result may well not be
242 globally applicable however, as the measurement sites in this experiment were of necessity close to
243 roads rather than evenly distributed through the area, and the range of snow depth is not globally
244 representative.

245

246 3.3. *Calculation of mean snow properties*

247

248 The class SWE ranges, and means of snow density and grain diameter within the classes for the
249 observations made over Intensive Observation Periods (IOPs) 1, 2, 3 and 4 at the CLPX Colorado
250 site are shown in Table 1, and illustrated in Figure 3. Snow water equivalent measurements were
251 made to the nearest whole mm.

252

253 The snow properties for snow mass in the sub-300mm SWE range where we expect the Chang
254 algorithm to be effective show considerable deviation from the values assumed in the algorithm.
255 Whilst measurements using different techniques can give a variety of snow grain size estimates,
256 making the absolute grain size values subject to interpretation, the considerable variability in snow
257 grain diameter in the low SWE range should be reflected by any self-consistent measurement
258 system. In this data, snow diameter only reaches a value consistently close to that assumed by the
259 Chang algorithm above 300mm SWE, in a regime where the algorithm is not applied because of
260 nonlinearity in the modelled relationship. Similarly, there is a substantial variation in the range of
261 snow density at low SWE, mostly more than 100kgm^{-3} below the 300kgm^{-3} algorithm assumption.
262 The mean snow density over all pits during IOP3 was in fact 145kgm^{-3} , less than half the algorithm
263 assumed value. This dataset has limitations, since the pit locations are of necessity close to roads,
264 and the snow depth is relatively low, however it remains the most appropriate for this work, and
265 similar measurements taken at Reynolds Creek Experimental Watershed over thirty years (Marks et
266 al, 2000) show a similar relationship between density and SWE, with density about 30kgm^{-3} higher
267 than the CLPX measurements for SWE below 300mm.

268

269 3.4. *The effects of measured snow properties on snow mass retrieval via the Chang algorithm*

270

271 The effect of using the mean snow grain diameter and density measurements from the CLPX site
272 (Table 1, Figure 3) in the emission model is shown in Figure 4. The snow water equivalent used in
273 the forward modelling is shown along the ordinate; the abscissa denotes the snow water equivalent
274 calculated from the simulated microwave emission driven by the measured mean values of mean
275 snow density and grain diameter. A line shows the 1:1 mapping expected if the Chang algorithm
276 exactly calculated the snow water equivalent. The other lines show the mapping between the input

277 SWE and that derived from applying the Chang algorithm to the HUT model driven by these
278 different assumptions of snow grain diameter and density :-

- 279 • Snow grain diameter of 0.8mm and density of 300kgm^{-3} , both as assumed by the Chang
280 algorithm
- 281 • Snow grain diameter of 0.8mm as assumed by the Chang algorithm, snow density according
282 to the CLPX measurements in Table 1
- 283 • Snow grain diameter according to the CLPX measurements in Table 1, snow density
284 300kgm^{-3} , as assumed by the Chang algorithm
- 285 • Snow grain diameter and density both according to the CLPX measurements in Table 1.

286

287 For most of the range of SWE, the algorithm overestimates SWE by a factor of between 2 and 3.
288 The relative effects of the deviation from the algorithm values of grain diameter and density can be
289 seen by replacing the algorithm values used within the emission model individually. The dashed
290 line shows that using the algorithm grain diameter of 0.8mm in the HUT model, and using only the
291 density from the snowpit measurements gives rise to a small increase in the estimated SWE over the
292 expected retrieval. Using the snowpit grainsize measurements with the 300kgm^{-3} algorithm density
293 in the emission model gives a far greater estimated SWE difference, indicating that the difference
294 between the grainsize assumed in the algorithm and that measured in the snow pits is the dominant
295 cause of this SWE over-estimation. Below 300mm SWE, the mean departure from exact retrieval
296 caused by the CLPX-measured grain size is just over five times greater than that caused by using
297 the CLPX-measured density.

298

299 3.5. *The effect of heterogeneity in snow properties on snow mass retrieval via the Chang*
300 *algorithm*

301

302 The Chang algorithm estimates of SWE from the HUT-simulated emission are shown in Figure 5,
303 for each class for homogeneous snow, and heterogeneous snow where variability in individual pit
304 measurements is incorporated. The mean simulated emission from the 109 North Park MSA pits
305 measured during IOP3 would yield an overall retrieved SWE of 62.4mm assuming snow was
306 homogeneous within the SWE classes, and 72.8mm for heterogeneous snow. The field
307 measurements of SWE used to drive the emission model had a mean of 23.8mm.

308

309 The heterogeneity does not seem to make a significant difference, though there is an apparent
310 reduction for SWE above 150mm. This would imply, for example, that a snow pack with a mean
311 SWE of 200mm with the range of snow properties seen at this site for such a SWE would have a
312 retrieved SWE of 370, whereas a snowpack with a SWE of 200mm and appropriate uniform mean
313 properties would have a retrieved SWE around 500mm. For most of the SWE regime, this indicates
314 that the variation in properties seen on this scale does not give rise to a substantial improvement in
315 soil moisture retrieval from the Chang algorithm.

316

317 3.6. *Comparison of snow mass estimates from satellite data to ground measurements.*

318

319 Whilst SSM/I measurements were available for all four IOPs, AMSR-E measurements were only
320 available for IOPs 3 and 4. Snow liquid water content was assessed qualitatively on-site by those
321 taking the physical measurements for a number of pits as either ‘dry’, ‘moist’ or ‘wet’, and the
322 results are tabulated in Table 2. These indicate that during IOP2, the snow was judged to be far

323 wetter than during the other periods, and we expect the estimation accuracy to be poor in such
324 conditions.

325

326 The snow mass estimates calculated from the satellite-measured brightness temperatures and the
327 mean of the snow water equivalent snow-pit measurements is plotted for each IOP in Figure 6; the
328 temporal extent of the snow-pit lines indicates the time span of the pit measurement campaign. The
329 SWE estimates based on applying the Chang algorithm to the mean brightness temperatures during
330 each campaign are also given in Figure 6, with the mean of the pit SWE measurements for each
331 IOP.

332

333 These figures show an estimated mean snow mass calculated from SSM/I and AMSR-E
334 measurements approximately twice the value measured on the ground, in line with the analysis of
335 Section 3.4 and Figure 4. For IOP3, where AMSR-E measurements are also available, they are
336 somewhat lower than those based on the SSM/I measurements, through it is difficult to draw
337 conclusions from such a small set of observations. The estimation fails as expected for the IOP2
338 measurements because the liquid water within the snow has substantially reduced penetration of the
339 19GHz radiation through the snow pack.

340

341 4. *Conclusions*

342

343 Based on the physical properties of the snow measured at the CLPX Colorado site, and the HUT
344 microwave emission model, snow mass calculations using the Chang algorithm overestimate snow
345 mass by a factor of two or more, predominantly because of the assumption of fixed grain diameter,
346 which shows substantial variation in the SWE range below about 300mm where the algorithm is
347 usable. This overestimation does not appear to be significantly affected by the heterogeneity in
348 snow properties exhibited at the site over a 25km distance.

349

350 While the CLPX measurements only indicate the range of variation of snow properties at one site,
351 we have no reason to believe that this site is exceptionally heterogeneous, or that the snow found in
352 the rest of the world corresponds more uniformly to the assumptions implicit in the Chang
353 algorithm. The SWE overestimation found by Pardé et al. (2007) in Central Canada suggests a snow
354 pack with similar grainsize characteristics to those found at the CLPX site. While the retrieved
355 effective grain diameter fitted in their retrieval shows a mean diameter around 3mm, between 2mm
356 and 4.5mm, ground measurements ranged between 1.3mm and 3.2mm. The sensitivity plot
357 Figure 2(a) indicates that the underestimates found by Armstrong & Brodzik (2000) in data from
358 the former Soviet Union, and Butt (2009) in the UK, could be attributed to a snow grain diameter
359 around 0.6mm.

360

361 Estimation of snow mass from its interaction with microwave radiation is strongly affected by other
362 snow characteristics, and consequently any improvement in snow mass retrieval via passive
363 microwave measurement will require grain size information. This could be acquired by a
364 simultaneous retrieval from microwave observations or possibly from visible and infra-red snow
365 surface reflectivity, which has been shown to be strongly dependent on grain diameter (Nolin and
366 Dozier, 2000). Tedesco et al. (2007) developed an approach based on this, and using MODIS
367 AQUA and TERRA near-infrared measurements of the CLPX area we have studied in this work,
368 North Park MSA, estimated the grain diameter of the top snow layer with an accuracy of
369 approximately 0.18 mm. This result should be considered in the context of the gap of a day between
370 satellite data acquisition and ground truth due to cloud conditions, and the difference between the
371 punctual ground measurements and the area-integrated estimates imposed by the 500m wide
372 MODIS pixels.

373

374 While this approach will not provide explicit information on the grain diameter throughout the
375 height of the snow pack, it is possible that a physical model of the snow pack, driven by a range of
376 measurements such as reflectivity-derived surface grain diameter estimates from satellite
377 instruments, and numerical weather predictions of temperature and precipitation, could provide the
378 necessary grain size information. Improved characterisation of snow structure could be used to
379 drive a multilayer version of the single-layer HUT model used here (Lemmetyinen et al., 2010).
380 Such a system would serve not only to improve our ability to invert an emission model to derive
381 snow mass from passive microwave emission, but also to indicate where the emission model, and
382 therefore the inversion, will fail. For example, the temperature within the snow pack would indicate
383 where melt and refreeze events are likely, flagging where the presence of ice lenses and liquid water
384 will cause problems for the emission model. The dynamic relationship between the physical model,
385 the emission model and the observations suggests the need for a data assimilation framework to
386 improve snow mass estimation. Data assimilation can be used to provide estimates of the snow
387 properties through physically-based simulations of the snow cover, constrained by independent
388 remote sensing estimates of eg. the grain size. These snow properties are then used to drive a
389 microwave emission model. Comparison between observed and simulated brightness temperatures
390 can be used to update the state of the modelled snowpack, and should enable more accurate
391 retrievals of snow mass.
392

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394

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397

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| Table 1. Classes defined by SWE ranges, and mean snow properties within the ranges over all pits for IOPs 1,2,3,4 | | | | | |
|---|----------------|-------|--------------------------------------|-----------------------------|------------------------|
| Class | SWE range (mm) | | Mean density (kg/m ³) | Mean grain diameter (mm) | Number of pits used |
| | Lower | Upper | | | |
| 1 | 3 | 7 | 122 | 0.46 | 66 |
| 2 | 8 | 10 | 120 | 0.58 | 33 |
| 3 | 11 | 13 | 138 | 0.59 | 29 |
| 4 | 14 | 17 | 152 | 0.76 | 32 |
| 5 | 18 | 24 | 191 | 1.21 | 32 |
| 6 | 25 | 44 | 225 | 1.21 | 53 |
| 7 | 45 | 68 | 235 | 1.25 | 29 |
| 8 | 69 | 86 | 223 | 1.46 | 5 |
| 9 | 87 | 104 | 244 | 1.35 | 12 |
| 10 | 105 | 163 | 230 | 1.36 | 55 |
| 11 | 164 | 221 | 235 | 1.40 | 28 |
| 12 | 222 | 290 | 253 | 1.00 | 36 |
| 13 | 291 | 433 | 281 | 0.99 | 69 |
| 14 | 434 | 570 | 298 | 0.96 | 65 |
| 15 | 571 | 700 | 318 | 0.93 | 38 |
| 16 | 701 | 825 | 341 | 0.80 | 21 |
| 17 | 826 | 1029 | 354 | 0.72 | 11 |
| 18 | 1030 | 1282 | 336 | 0.73 | 6 |

| | | | |
|---|-----|-------|-----|
| Table 2. Snow moisture assessment as a percentage of the number of pits with an estimate. | | | |
| Period | Dry | Moist | Wet |
| IOP1 | 55% | 35% | 9% |
| IOP2 | 40% | 10% | 50% |
| IOP3 | 49% | 49% | 3% |
| IOP4 | 58% | 42% | 0% |

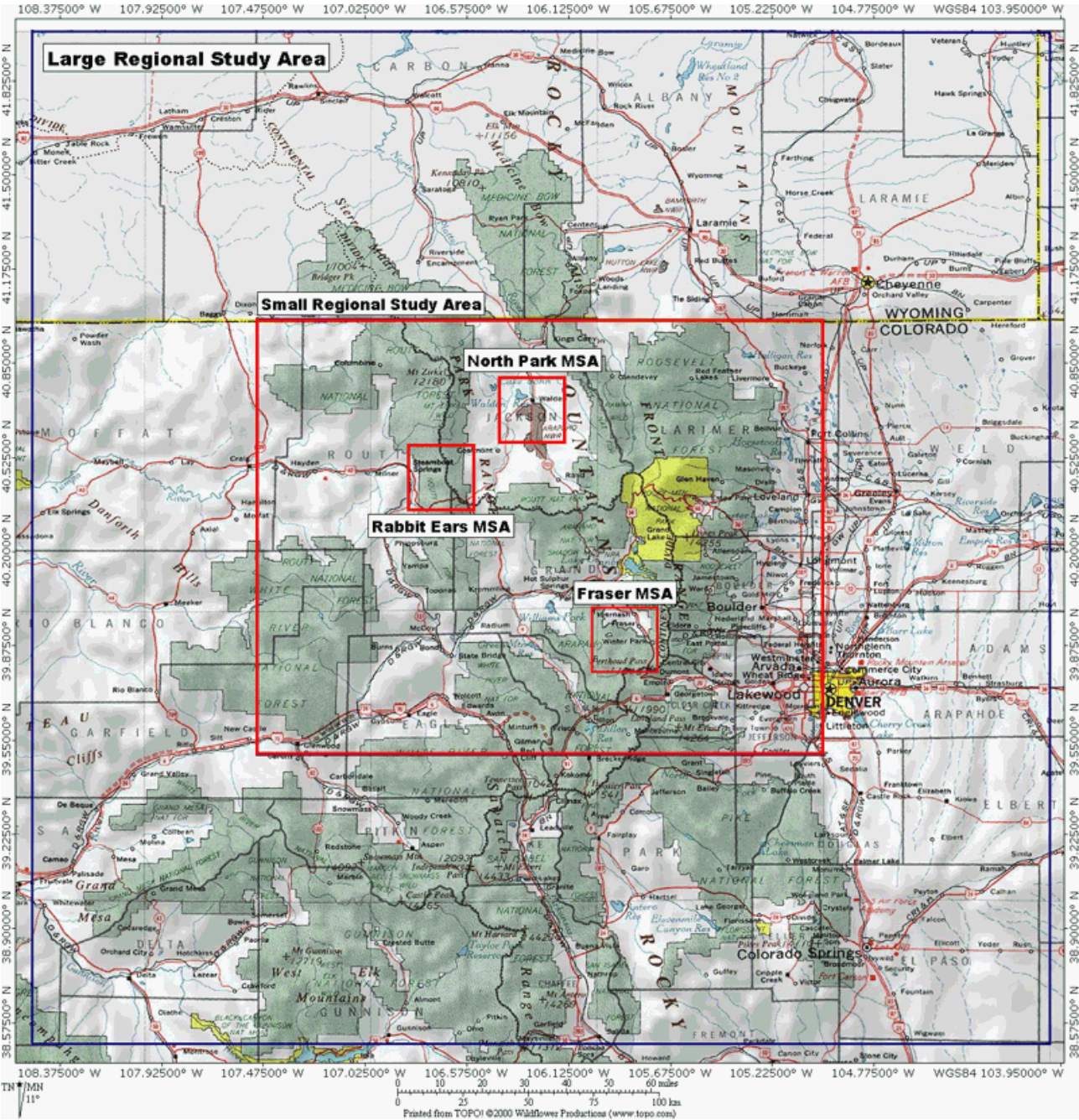


Figure 1. Nested study areas for the Cold Land Processes Field Experiment

(after <http://www.nohrsc.nws.gov/~cline/clpx.html>)

COLOUR, ONLINE VERSION

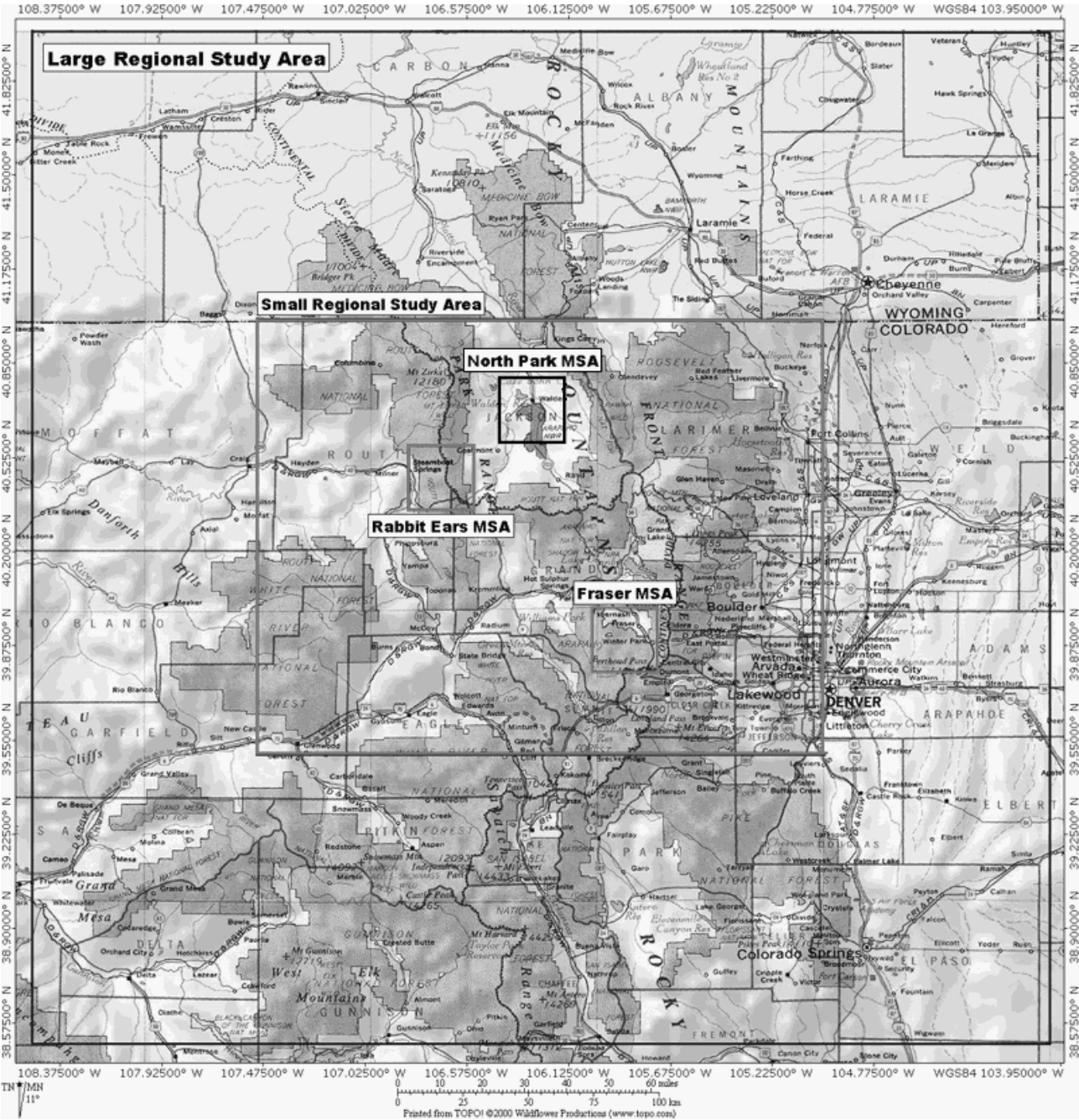
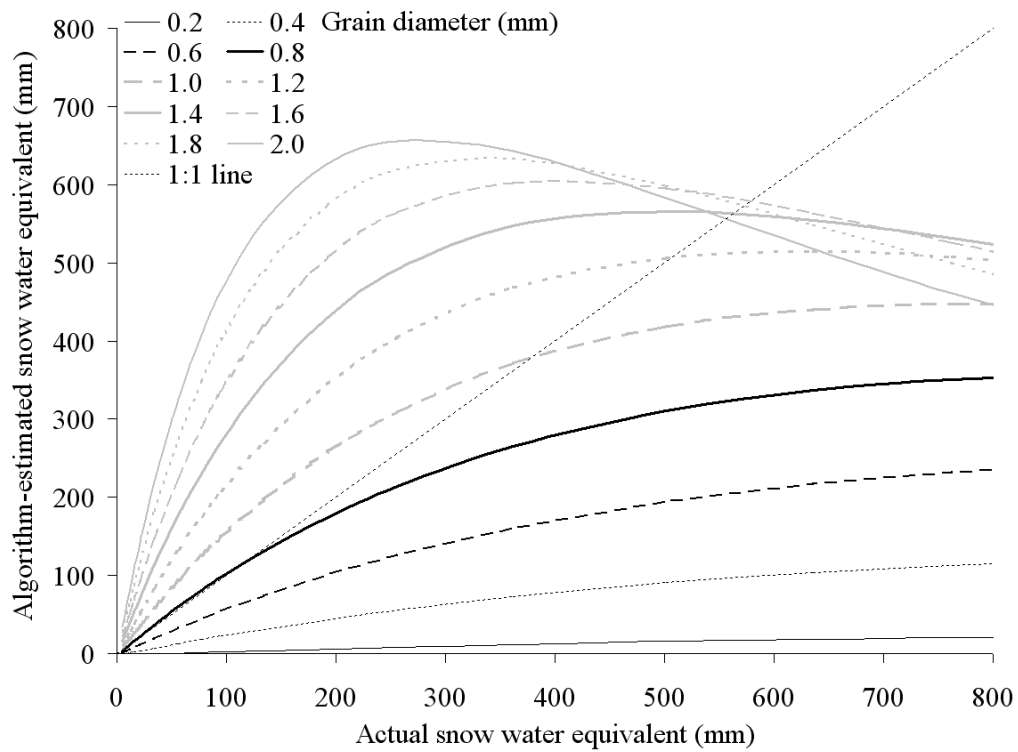


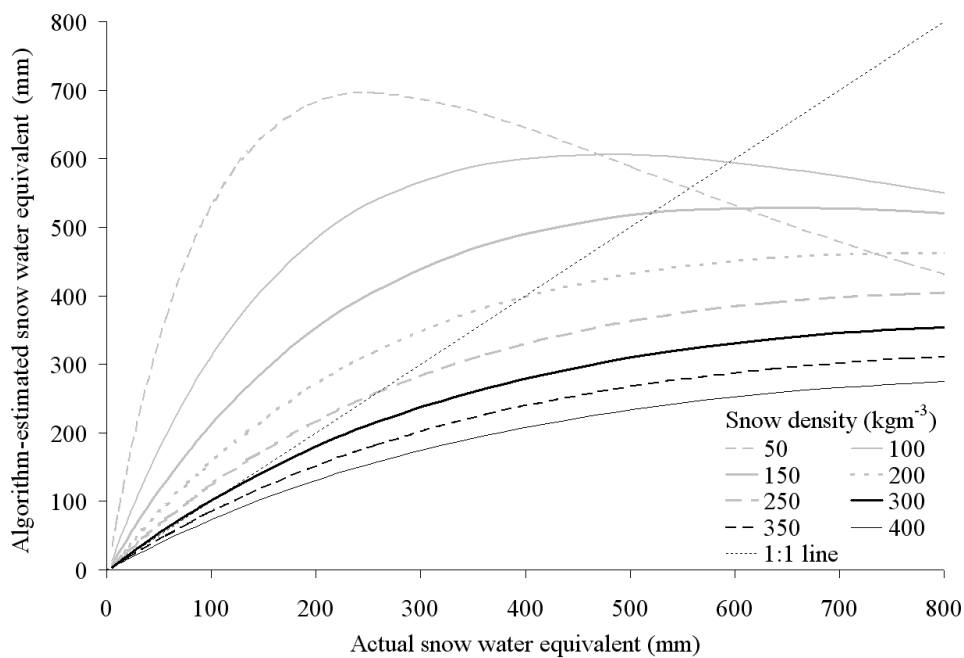
Figure 1. Nested study areas for the Cold Land Processes Field Experiment

(after <http://www.nohrsc.nws.gov/~cline/clpx.html>)

GREYSCALE, PRINT VERSION

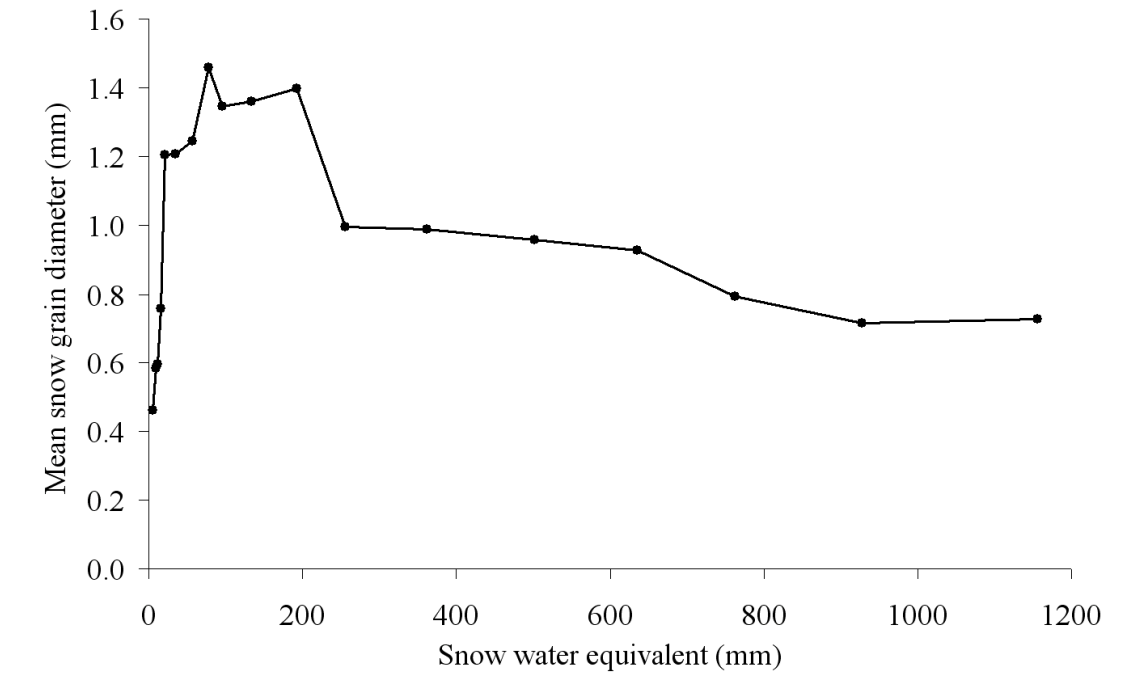


(a) Retrieval error caused by deviation of snow grain diameter from ideal value of 0.8mm while snow density is fixed at 300 kg m^{-3} .

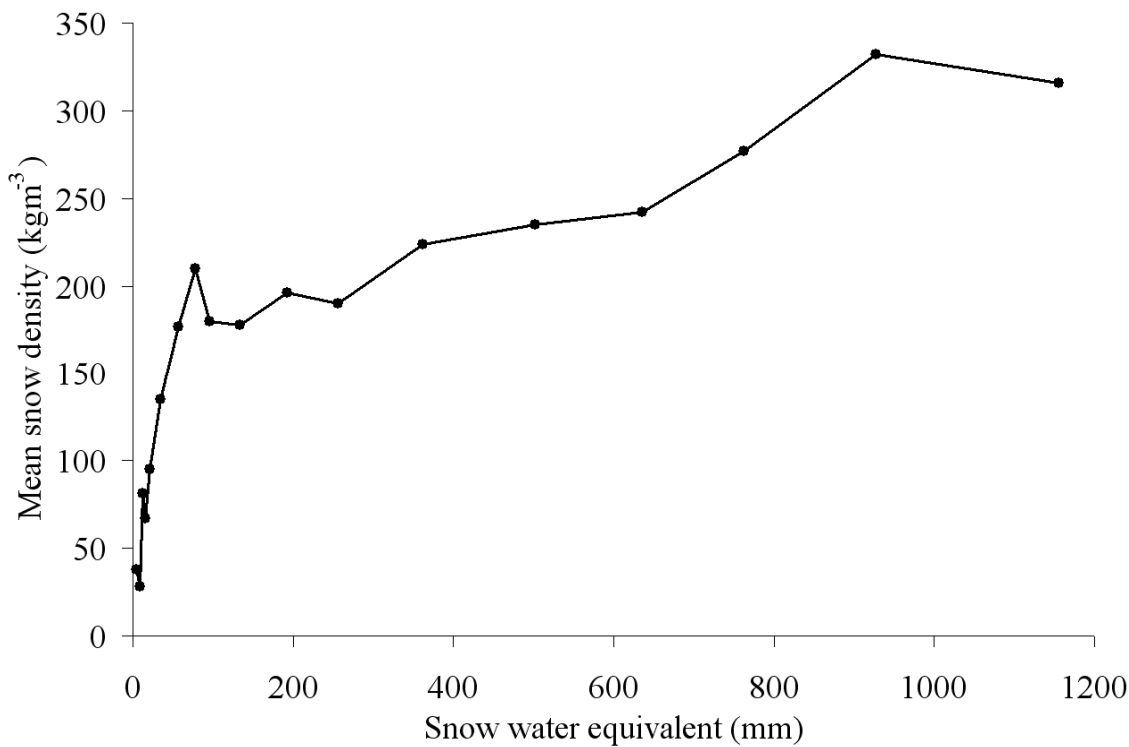


(b) Retrieval error caused by deviation of snow density from ideal value of 300 kg m^{-3} while snow grain diameter is fixed at 0.8mm.

Figure 2. Chang algorithm retrieval error caused by deviation of snow grain diameter and density from ideal values.



(a) Snow grain diameter



(b) Snow density

Figure 3. Mean snow properties within SWE classes calculated from CLPX measurements.

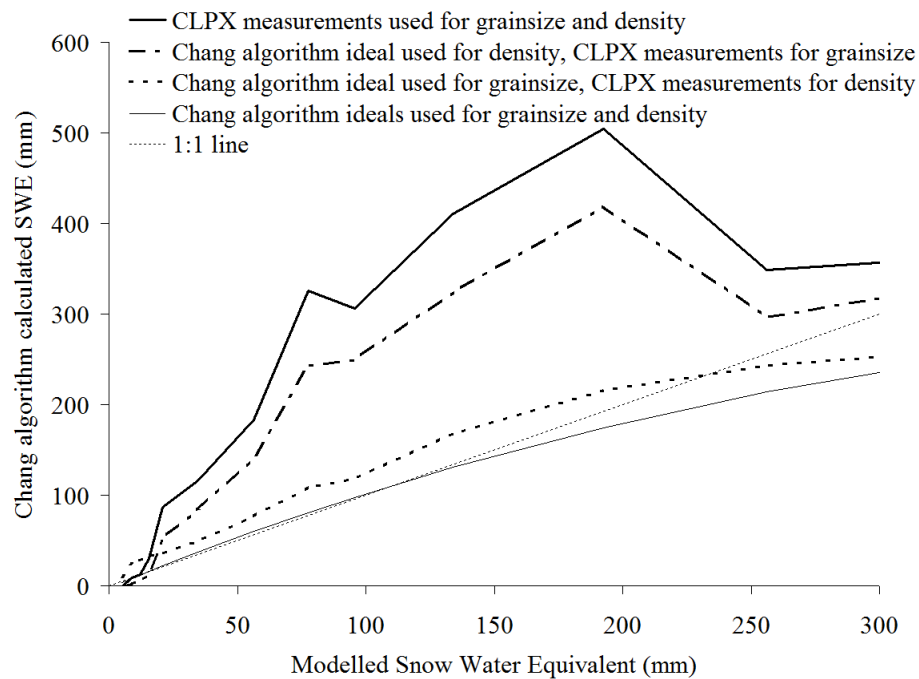


Figure 4. The effect of CLPX snow grain diameters and densities on the accuracy of snow water equivalent retrieval from the Chang algorithm, using the HUT model to calculate microwave emission.

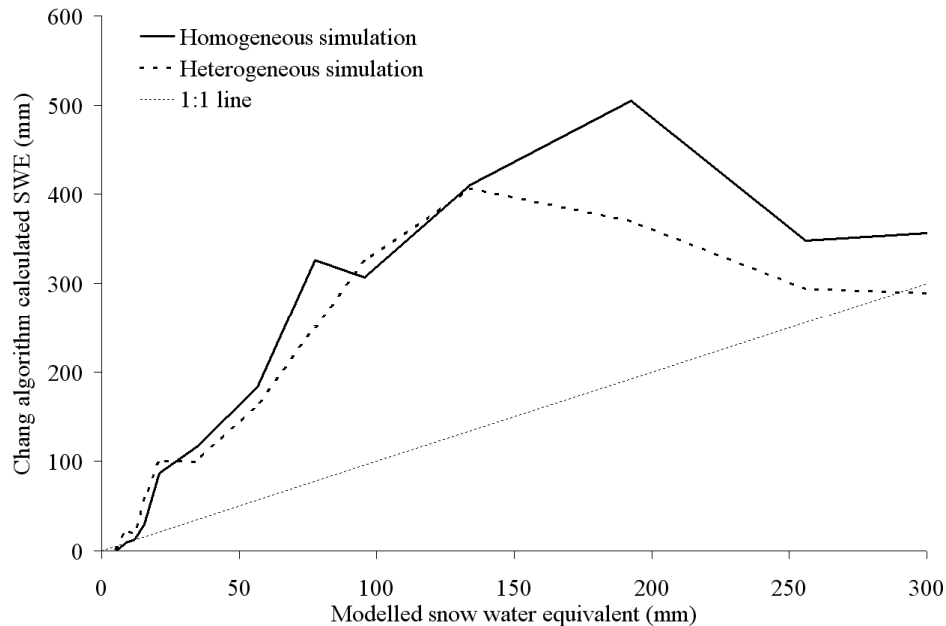
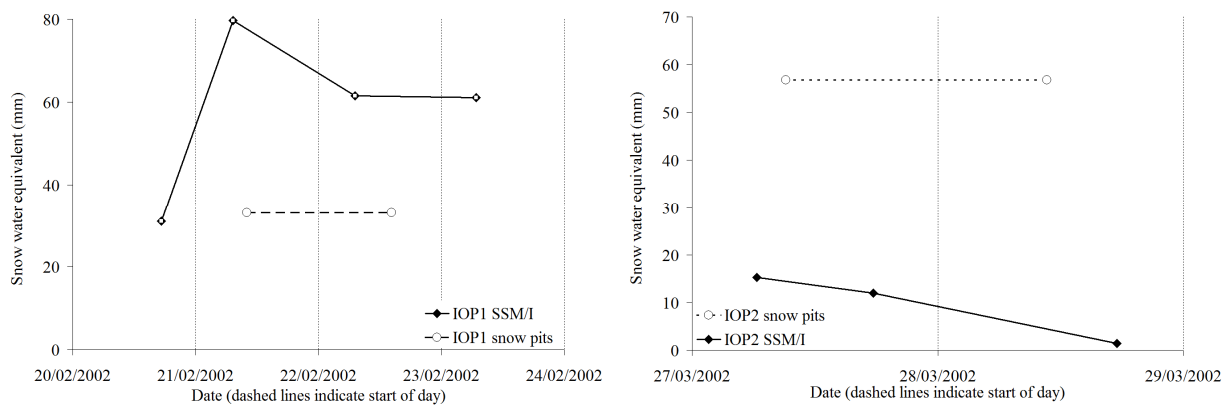
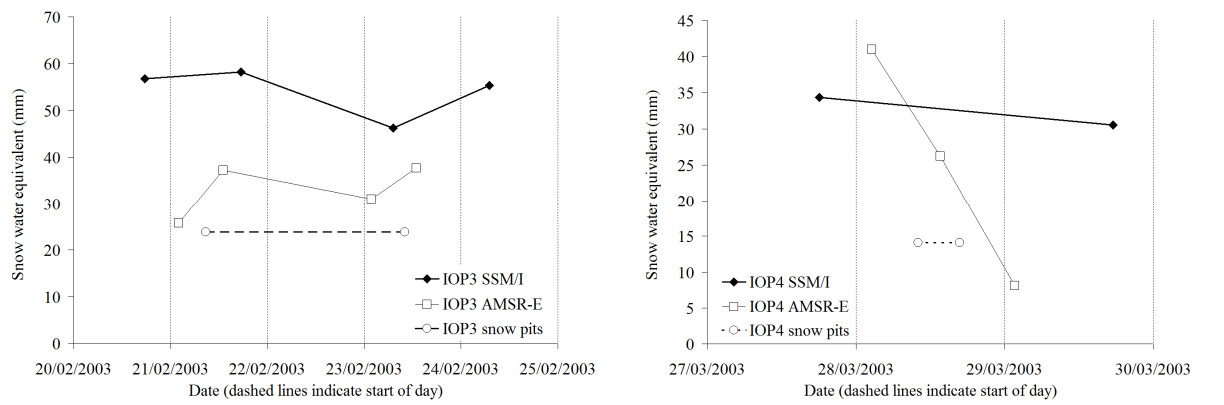


Figure 5. Snow water equivalent retrieved from microwave emission simulated by using CLPX measurements in the HUT model. Mean snow characteristics within each SWE class are used for the homogeneous line, the heterogeneous line uses a distribution of snow characteristics within each class derived from the CLPX measurements to reflect measured snow variability.



(a) IOP1, 20-24 Feb 2002, mean pit-measured SWE 33.1mm, SSM/I 70.6mm
(b) IOP2, 27-28 March 2002, mean pit-measured SWE 56.8mm, SSM/I 9.5mm



(c) IOP3, 20-23 Feb 2003, mean pit-measured SWE 23.8mm, SSM/I 52.2mm, AMSR-E 32.9mm
(d) IOP4, 28th March, 2003, mean pit-measured SWE 14.1mm, SSM/I 32.4mm, AMSR-E 25.1mm

Figure 6. Snow water equivalent in CLPX North Park MSA during the four Intensive Observation Periods, measured during ground campaigns and estimated from SSM/I and AMSR-E satellite data using the Chang algorithm.