

# *Have greenhouse gases intensified the contrast between wet and dry regions?*

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# <sup>1</sup> Have greenhouse gases intensified the contrast <sup>2</sup> between wet and dry regions?

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3 **Abstract.**

4 While changes in land precipitation during the last 50 years have been at-  
5 tributed in part to human influences, results vary by season, are affected by  
6 data uncertainty and do not account for changes over ocean. One of the more  
7 physically robust responses of the water cycle to warming is the expected  
8 amplification of existing patterns of precipitation and evaporation. Here, pre-  
9 cipitation changes in wet and dry regions are analysed from satellite data  
10 for 1988-2010, covering land and ocean. We derive fingerprints for the ex-  
11 pected change from climate model simulations that separately track changes  
12 in wet and dry regions. The simulations used are driven with anthropogenic  
13 and natural forcings combined (ALL), and greenhouse gas forcing or natu-  
14 ral forcing only. Results of detection and attribution analysis show the fin-  
15 gerprint of combined external forcing is detectable in observations and that  
16 this intensification of the water cycle is partly attributable to greenhouse gas  
17 forcing.

## 1. Introduction

As temperatures rise in response to increasing greenhouse gas concentrations, the global water cycle is expected to intensify [Allen and Ingram, 2002; Trenberth et al., 2003]. This should lead to increasing atmospheric water vapor and moisture transport, from water exporting to importing regions, enhancing existing patterns of precipitation (P) minus evaporation (E) [Held and Soden, 2006; Seager and Naik, 2012]. Due to energy budget constraints in the atmosphere, the precipitation response in models is 2-3% K<sup>-1</sup> [Held and Soden, 2006; Stephens and Ellis, 2008], less than the increase in the water vapour concentrations of  $\sim 7\%$  K<sup>-1</sup> near to the surface [Santer et al., 2007; Willett et al., 2010].

The pattern of wet regions becoming wetter and dry regions becoming drier is seen in multiple satellite based datasets of precipitation [Liu et al., 2012; Chou et al., 2013], in studies of atmospheric moisture transport using reanalysis data [Zahn and Allan, 2011], modeling studies of past and projected changes [Sun et al., 2007; Seager and Naik, 2012; Lau et al., 2013; Liu and Allan, 2013] and changes suggested by ocean salinities [Durack et al., 2012]. It is also consistent with a wider frequency distribution of precipitation [Lintner et al., 2012; Giorgi et al., 2011; Biasutti, 2013].

Changes in zonally averaged land precipitation since the 1950s have been partly attributed to anthropogenic forcing [Zhang et al., 2007; Polson et al., 2013] using fingerprint detection and attribution (D+A) methods. Changes over the land and ocean combined should show higher signal-to-noise ratio [Balan Sarojini et al., 2012] and the expected change pattern is less clear over land than oceans [Held and Soden, 2006]. Here we apply a D+A analysis [Allen and Stott, 2003] to satellite data for land and ocean precipitation

for the years 1988 to 2010. This is a short timescale for analyzing precipitation trends compared to natural variability, however *Seager and Naik* [2012] find anthropogenically induced changes in P-E are beginning to emerge for the satellite period using model and reanalysis data. Our analysis focuses on changes in wet and dry regions separately, relying on expected changes from well understood physical processes and the predicted response to warming. It follows the wet and dry regions as they move over time, tracking the changes in these regions independently of their location [*Liu et al.*, 2012] and thus accounting for changes in atmospheric circulation due to natural variability, or in response to warming, for example, poleward migration of the subtropical dry regions [*Seager and Naik*, 2012].

Climate model simulations of the 20th century are used to derive fingerprints of precipitation response to all external forcings and greenhouse gas only forcing. Natural forcing can also affect precipitation. Aerosols from volcanic eruptions reduces precipitation particularly in the wet regions for up to 6 years after the eruption in climate models [*Iles et al.*, 2013]. The eruptions of El Chichon in 1982 and Pinatubo in 1991 may have impacted precipitation during first half of the observation period [*Trenberth and Dai*, 2007], leading to a naturally forced trends that are similar to those due to greenhouse gas forcing.

## 2. Data: Observations and Models

We use the satellite-based Global Precipitation Climatology Project (GPCP) gridded dataset of monthly precipitation [*Adler et al.*, 2003] for the years 1987-2010 (for which measurements from the Special Sensor Microwave Imager (SSM/I) are available). Two observational datasets of monthly land precipitation, the Climate Research Unit (CRU) [*Harris et al.*, 2013] and the Global Precipitation Climatology Centre (GPCC) [*Schneider*

*et al.*, 2011] datasets, are included for comparison. ENSO is removed from the observations as the short record means it will influence the trends (note the supplement discusses the robustness of our findings, including to removing ENSO).

Model data are from the Climate Model Intercomparison Project Phase 5 (CMIP5) archive [Taylor *et al.*, 2011]. We use historical runs with anthropogenic and natural forcings (ALL), greenhouse gas only forcing (GHG) and natural only forcing (NAT). We also analyze the expected change for 2011-2033, based on the rcp4.5 scenario (Table S1). Data are aggregated to a 5°x5° grid and gridboxes split into land and ocean using the model land fraction data with a cutoff of 50%.

### 3. Analysis of changes in Wet and Dry Regions

Data were divided into zonal bands from 60°-40°S, 40°-20°S, 20°S-0°, 0°-20°N, 20°-40°N and 40°-60°N and then split into wet and dry regions (see below). As satellite observations are less reliable poleward of 50-55° (Huffman pers. comm.), the mid and high latitudes are excluded from the D+A analysis. The data were grouped into four seasons; January, February and March (JFM), April, May June (AMJ), July, August and September (JAS) and October, November and December (OND), to capture the tropical wet and dry seasons, and precipitation averaged across the three months. Precipitation changes are calculated for 1988-2010, to ensure OND and JFM are consistent, OND is from the previous year (1987-2009). Two methods are used to define the dry and wet regions in each zonal band, with all D+A analysis using the precipitation changes from method 1.

*Method 1* uses dry and wet regions of fixed size that move from season to season and year to year. For each zonal band,  $\hat{P}_x(i, t)$  is the mean precipitation in the dry or wet

region for season  $i$  and year  $t$  where  $x$  is *dry* or *wet*. gridboxes are sorted from lowest to highest precipitation so that

$$\hat{P}_{dry}(i, t) = \sum_{n=1}^{L_{33}} P_n(i, t) \quad (1)$$

where  $P_n$  is the precipitation in gridbox  $n$  and  $\hat{P}_{dry}(i, t)$  is the mean precipitation for all gridboxes in the lower 33.3 percentile ( $n \in [1, L_{33}]$ ), for season  $i$ , year  $t$ .  $\hat{P}_{wet}(i, t)$  is the mean precipitation of all gridboxes in the upper 33.3 percentile ( $n \in [U_{33}, N]$ ), where  $N$  is the total number of gridboxes in each zonal band. A linear least squares regression is used to calculate the change in  $\hat{P}_x(i, t)$  over all years,  $\dot{P}_x(i)$  where  $\dot{P}_x(i)$  is expressed as a percentage relative to  $\hat{P}_x(i, t)$  averaged over all years.

*Method 2* uses a fixed cutoff value in each zonal band for dry and wet regions for all years. This allows the regions to move and change size from season to season and year to year. For each zonal band,  $P_{33}(i)$  is the 33.3 percentile for all gridboxes, in all years for season  $i$  and  $P_{66}(i)$  is the 66.67 percentile. If  $P_n(i, t)$  are sorted from lowest to highest

$$\hat{P}_{dry}(i, t) = \sum_{n=1}^{n_{P33}} P_n(i, t) \quad (2)$$

here  $n \in [1, n_{P33}]$  are all gridboxes where  $P_n(i, t) \leq P_{33}(i)$ . For  $\hat{P}_{wet}(i, t)$ ,  $n \in [n_{P66}, N]$  are all gridboxes where  $P_n(i, t) \geq P_{66}(i)$ .  $\dot{P}_x(i)$  is then calculated as in method 1.

The same methods are applied to individual simulations to calculate  $\dot{P}_x(i)$  in each, these are averaged to give the multi-model mean changes. This allows for differences in the precipitation patterns and model error in the location of climatological precipitation.



Thus the model fingerprints are more physically consistent than that obtained by simply averaging across all simulations which may smear out changes.

#### 4. Detection and Attribution

Total least squares regression [Allen and Stott, 2003] determines the magnitude of the fingerprint,  $\mathbf{F}$ , of the response to external forcing, in the observations  $\mathbf{y}$ .

$$\mathbf{y} = (\mathbf{F} + \varepsilon_{\text{finger}}) \cdot \beta + \varepsilon_{\text{noise}} \quad (3)$$

where  $\mathbf{y}$  is rank- $l$  vector and  $\mathbf{F}$  is a  $l \times p$  matrix for  $p$  external climate forcings.  $\beta$  is a vector of scaling factors with  $p$  entries giving the magnitude of each fingerprint in the observations,  $\varepsilon_{\text{noise}}$  is the residual associated with internal climate variability and is compared to samples of model variability using the F-test [Allen and Stott, 2003].  $\varepsilon_{\text{finger}}$  is a  $l \times p$  matrix of variability superimposed on the fingerprint.

Here, single fingerprints ( $p = 1$ ) are used for ALL, GHG, NAT and RCP4.5. In each case  $\mathbf{F}$  is the multi-model mean  $\dot{P}_x(i)$  for the 4 zonal bands in the tropics and subtropics for seasons  $i = 1, 4$ , giving  $l = 16$  for the dry and wet regions separately and  $l = 32$  for the dry and wet regions combined. A two-signal approach was applied to GHG and NAT forcing. All analysis was repeated for land+ocean, land only and ocean only. Optimized fingerprints were tried but did not improve the signal-to-noise ratio.

Multiple samples of climate noise are added to  $\mathbf{F}$  and  $\mathbf{y}$  and  $\beta$  recalculated. If  $\beta > 0$  at the 5% significance level, then the fingerprint response pattern is detected in the observations [Hegerl et al., 2007]. As models may underestimate precipitation variability,  $\beta$  is also calculated for double the model variance [Zhang et al., 2007; Polson et al., 2013].

## 5. Results

The location and size of the GPCP dry and wet regions do not change much from year to year (Figure 1) with 70%-85% of the dry and wet regions remaining fixed from one year to the next. The models tend to locate the dry and wet regions in the same gridboxes as the observations. If the observations define a gridbox as dry(wet) in over 75% of years then on average, 73%(65%) of simulations will also define that gridbox dry(wet) in over 75% of years. The size of the regions from the start to the end of the observation period change by less than the maximum year-to-year variation, except in SH mid-latitudes.

The tropics and subtropics show a pattern of dry regions becoming drier and wet regions becoming wetter from 1988-2010 for the observations and multi-model means for models with greenhouse gas forcing (ALL, GHG, RCP4.5, see Figure 2). The NAT only multi-model mean also shows a tendency for dry to get drier and wet to get wetter, but not as consistently for all zonal bands and seasons. However, these patterns are not consistent across all simulations. 20-30% of the ALL, GHG and RCP4.5, and 40% of the NAT only individual simulations give more (i.e zonal bands and seasons) dry regions becoming wetter. Wet regions becoming wetter is a more consistent result with exceptions of less than 10% of the ALL forced and GHG only simulations and <20% of the RCP4.5 and NAT forced simulations. While the pattern of moistening and drying persists over both land and ocean in observations and models (Figures S13 and S14), dry becoming drier is more consistent over oceans than land. Comparison of the GPCP land only changes with two other station-based observational datasets, GPCC and CRU (masked to the wet and dry regions of GPCP), shows consistency between the datasets (Figures S15 and S16).

140 The detection analysis for the combined fingerprint of the wet and dry regions and all  
141 seasons combined shows that ALL forcing had a significant influence on satellite measure-  
142 ments of precipitation (Figure 3(a)). The changes from GHG and RCP4.5 simulations  
143 are similarly detected in the observed changes, while NAT forcing is not (Figure S17).  
144 Changes are also detected over ocean only, but not land only, likely due to poorer signal-  
145 to-noise ratio with a smaller fraction of the wet and dry regions coinciding with land than  
146 ocean and a quicker response to more localized forcing (see *Balan Sarojini et al.* [2012]).  
147 SH tropical dry regions in OND and JFM, and SH subtropical wet regions in AMJ and  
148 JAS were excluded from the land only analysis because few gridboxes coincide with land.

149 Changes in the dry and wet regions separately are also detected for ALL, GHG and  
150 RCP4.5 forcing, (over ocean for ALL forcing, Figure S19). The fingerprint of NAT forcing  
151 is also detectable for the wet regions, possibly reflecting the influence of volcanoes during  
152 the first half of the observation period [*Iles et al.*, 2013]. To distinguish the influence of  
153 GHG from NAT forcing, a 2-signal D+A was applied, simultaneously estimating GHG  
154 and NAT forcing. The results for the combined dry and wet fingerprint shows that GHG  
155 forcing is detectable while NAT forcing is not (Figure 3(b)).

156 Our results were robust to not removing ENSO and using the Nino-3.4 SST index from  
157 CPC, NOAA (see supplement), except when ENSO is not removed, ALL forcing for the  
158 dry+wet fingerprint was not detected for land+ocean, while GHG forcing was detectable  
159 in the dry regions for the GHG and NAT 2-signal analysis.

## 6. Discussion and Conclusions

160 Precipitation from GPCP observations and models that include GHG forcing (i.e. ALL,  
161 GHG only and RCP4.5) clearly show a tendency for dry regions to get drier and wet regions

162 to get wetter, consistent with theory [Allen and Ingram, 2002; Held and Soden, 2006]. The  
163 NAT only simulations show a similar pattern for the wet regions and to a lesser extent  
164 in the dry regions due to the influence of the El Chichon and Pinatubu eruptions in the  
165 first half of the observation period.

166 The zonal mean changes for the GPCP data are dominated by changes over the ocean  
167 which are thought to be less reliable than changes over land (e.g. Liu et al. [2012]).  
168 While the pattern of wet regions becoming wetter holds over both land and ocean, drying  
169 in the dry regions is less consistent over land. There is evidence that land and ocean  
170 precipitation are anti-correlated [Liu et al., 2012], however, on short timescale, this is due  
171 to the influence of ENSO, hence we lose much of this anti-correlation here.

172 Detection and attribution analysis shows all external forcings and greenhouse forcing are  
173 detectable in precipitation changes over the last 20 years in the tropical and subtropical  
174 dry and wet regions. Fingerprints based on future change are also detectable showing  
175 they are expected to enhance the pattern of change already observed.

176 If the wet and dry signals are combined, greenhouse gas forcing can be detected sep-  
177 arately to natural forcing. The precipitation response to volcanic eruptions in the dry  
178 regions is small compared to the greenhouse gas signal, which may explain why the green-  
179 house gas signal is detectable in the dry regions while the natural signal is not in the  
180 1-signal analysis. Our analysis did not include aerosol changes explicitly as not enough  
181 runs were available to characterize changes with reasonable signal-to-noise ratio.

182 Our results are subject to uncertainty in trends derived from satellite data and the  
183 shortness of the observational record. However, our results are consistent with results  
184 attributing salinity changes to human influences [Durack et al., 2012] over ocean, and

changes recorded over land are broadly similar to those recorded by in-situ data. Thus our results suggest an emerging pattern of wet regions becoming wetter and dry regions becoming drier that appears to be at least in part due to greenhouse gas forcing. This provides evidence of an anthropogenically-induced intensification of the water cycle.

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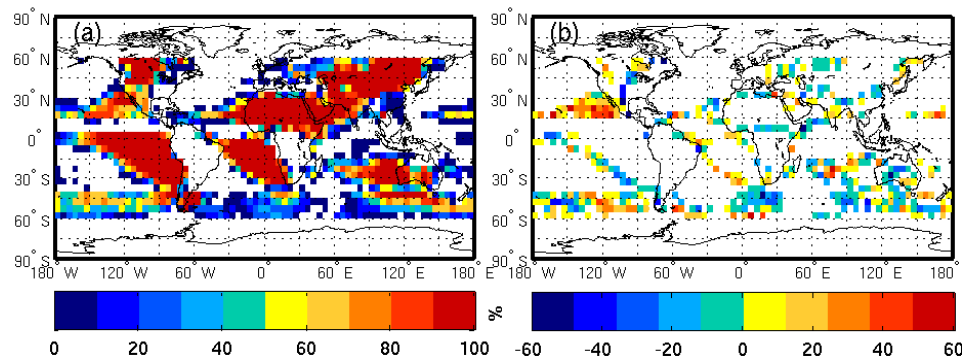
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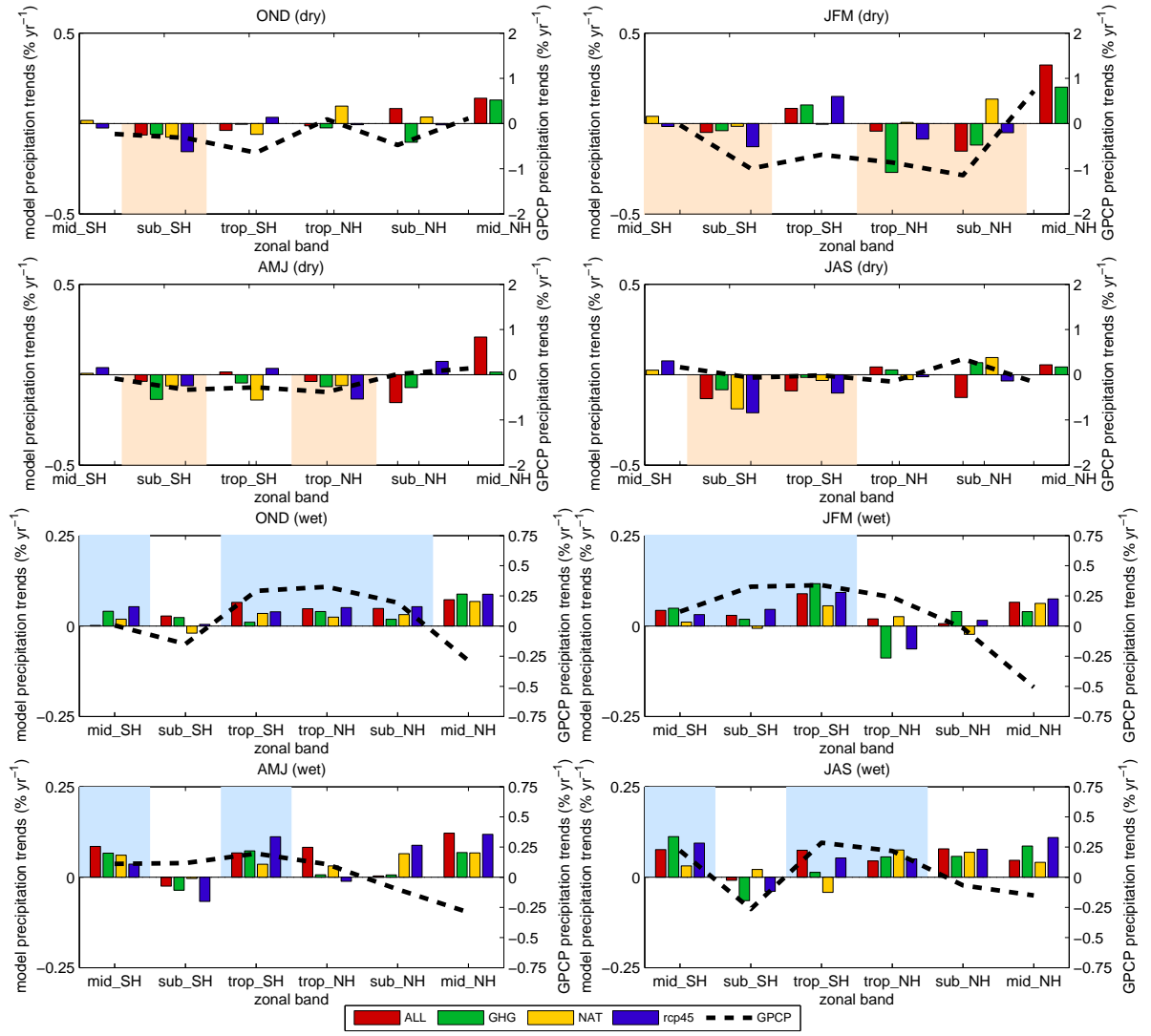
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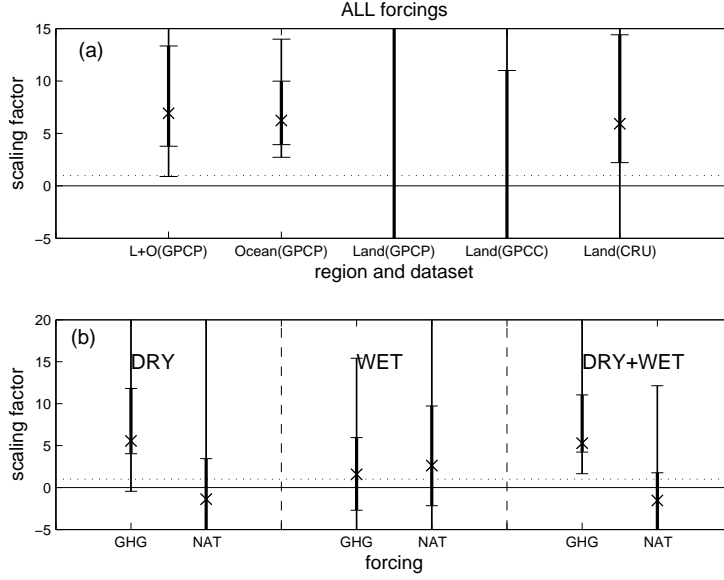




**Figure 1.** GPCP dry regions for October, November and December (OND is 1987-2009) from method 1. (a) The percentage of years a gridbox is defined as dry for 1987-2009. (b) Percentage of years dry in 2000-2009 minus 1987-1996, only gridboxes where the change is not zero are plotted. ENSO removed from observations. Similar results for other seasons (see supplement).



**Figure 2.** Observed and model simulated zonal mean changes (% per year) in the dry (TOP FOUR PANELS) and wet (LOWER FOUR PANELS) regions for land and ocean 1988 to 2010 (OND is 1987-2009). The colored bars give the multi-model mean changes for the ALL, GHG, NAT and RCP4.5 simulations. The orange/blue shading show where GPCP, ALL and RCP4.5 are all negative/positive. Note GPCP is plotted on a larger scale and the influence of ENSO is removed from observations.



**Figure 3.** (a) Scaling factors for the wet and dry regions combined for ALL forced simulations. L+O is land+ocean. (b) Scaling factor for 2-signal D+A of GHG and NAT forcing. Crosses show the 'best-guess' scaling factor for the multi-model mean, thick lines are the 90% confidence interval for the raw model variance added as noise and thin lines are the 90% confidence interval for double the variance. Influence of ENSO is removed from observations. The residual consistency test is passed in all cases.