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1 Statistical characterisation of the growth and spatial 2 scales of the substorm onset arc

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D R A F T

Abstract. We present the first multi-event study of the spatial and temporal structuring of the aurora to provide statistical evidence of the near-Earth plasma instability which causes the substorm onset arc. Using data from ground-based auroral imagers, we study repeatable signatures of along-arc auroral beads, which are thought to represent the ionospheric projection of magnetospheric instability in the near-Earth plasma sheet. We show that the growth and spatial scales of these wave-like fluctuations are similar across multiple events, indicating that each sudden auroral brightening has a common explanation. We find statistically that growth rates for auroral beads peak at low wavenumber with the most unstable spatial scales mapping to an azimuthal wavelength $\lambda \approx 1700 - 2500$ km in the equatorial magnetosphere at around 9-12 R_E . We compare growth rates and spatial scales with a range of theoretical predictions of magnetotail instabilities, including the cross-field current instability and the shear-flow ballooning instability. We conclude that, although the cross-field current instability can generate similar magnitude of growth rates, the range of unstable wavenumbers indicates that the shear-flow ballooning instability is the most likely explanation for our observations.

1. Introduction

The causal sequence of events leading to energy release and auroral breakup during substorms remains unknown, primarily due to a lack of spatial and temporal resolution when investigating the physical processes occurring within the first 2 minutes of substorm onset in such a vast 3D volume of space. The discrepancy and uncertainty in timings between magnetospheric processes and auroral signatures prior to the expansion phase has caused a controversial and currently unresolved debate over the physical process leading to the substorm expansion phase onset. This debate has predominantly focussed on two substorm onset paradigms: (1) Magnetic reconnection at the Near Earth Neutral Line (NENL) [Baker *et al.*, 1996; Hones, 1976] causing Earthward plasma flows which destabilise the central plasma sheet, or (2) a near-Earth magnetospheric disturbance triggering Current Disruption (CD) in the central plasma sheet [Roux *et al.*, 1991; Lui *et al.*, 1991]. Other models include the boundary layer dynamics model [Rostoker and Eastman, 1987], near-Earth geophysical onset model [Maynard *et al.*, 1996], and global Alfvénic interaction model [Song and Lysak, 2001]. The NENL and CD model have been most extensively discussed in the field e.g. [Angelopoulos *et al.*, 2008, 2009; Lui, 2009], however no consensus has yet been reached. Further complexity to the NENL model has since been added e.g. Nishimura *et al.* [2010]; Sergeev *et al.* [2012] where the impacts of flow bursts on auroral breakup are discussed.

Substorm onset is marked in the ionosphere by a sudden brightening of the most equatorward auroral arc or, in some instances, the formation of a new arc that brightens [Akasofu, 1977] and is followed by auroral breakup. Early observations of substorm au-

42 rora provided by the Viking mission enabled the discovery of small-scale azimuthal auroral
 43 fluctuations, nicknamed ‘auroral beads’ [Henderson, 1994] or subsequently azimuthal au-
 44 roral forms (after *Elphinstone et al.* [1995]) which form along the onset arc in the minutes
 45 leading up to auroral breakup. Auroral beads observed with space-based imagery have
 46 only been sporadically reported since [Henderson, 2009].

47 The aim of the Time History of Events and Macroscale Interactions during Substorms
 48 (THEMIS) [Angelopoulos, 2008; Sibeck and Angelopoulos, 2008] mission is to uncover the
 49 temporal sequence of processes linked with substorms. The increased spatial coverage
 50 provided by THEMIS all-sky imagers (ASI) [Mende et al., 2008] together with its high
 51 spatial and temporal resolution has led to the renewed interest in small-scale azimuthal
 52 auroral beads forming along the onset arc [Friedrich et al., 2001; Liang et al., 2008; Sak-
 53 aguchi et al., 2009; Rae et al., 2009a, 2010]. From here on we will refer to this phenomenon
 54 as auroral beads. Auroral beads have been interpreted in a variety of ways. *Rae et al.*
 55 [2010] and *Motoba et al.* [2012] conclude that they are the ionospheric signature of a mag-
 56 netospheric instability. In contrast *Haerendel* [2010, 2015] interpret the origin of auroral
 57 beads as the ‘*point of preferred entry of magnetic flux from the central current sheet of the*
 58 *tail*’ due to a current sheet collapse. The latter concluding that flow bursts are stalled due
 59 to a stop layer of the width of an ion inertial length, leading to the formation of closely
 60 spaced field aligned currents which are responsible for the periodic auroral beads.

61 *Motoba et al.* [2012] observed magnetically conjugate auroral beads in ASI data from
 62 both Northern and Southern hemispheres and suggested that the beads have a common
 63 driver originating in the magnetosphere. In addition to these wave-like signatures in the
 64 aurora, simultaneous magnetic pulsations of ULF waves have also been observed in the

minutes surrounding substorm onset [*Mann et al.*, 2008; *Milling et al.*, 2008; *Murphy et al.*, 2009a; *Murphy et al.*, 2009b; *Rae et al.*, 2009a, b; *Walsh et al.*, 2010; *Rae et al.*, 2011]. Moreover these ULF pulsations are repeatably observed at frequencies similar to those observed in the auroral beads [*Rae et al.*, 2012], suggesting an inextricable link between the auroral and magnetic waves.

The previously discussed studies of auroral beads were limited to descriptions of the initial azimuthal wavelength and its temporal evolution. *Rae et al.* [2010] provide optical analysis of substorm auroral arc azimuthal wavenumber spectra during a single event which demonstrates that the beading of the substorm onset arc is characteristic of an instability in the near-Earth magnetosphere. *Rae et al.* [2010] report that the frequency, spatial scales and growth rates of the auroral structures are most consistent with either a Cross-Field Current Instability (where growth rates peak at $\sim 0.4 \text{ s}^{-1}$) [*Lui et al.*, 1991; *Lui*, 2004] or a Shear-Flow Ballooning Instability (where growth rates peak at $\sim 0.2 \text{ s}^{-1}$) [*Voronkov et al.*, 1997]. However, *Rae et al.* [2010] could not identify which of these two instabilities acted during this event, nor could they definitively rule out the Kelvin-Helmholtz e.g. [*Yoon et al.*, 1996] or entropy anti diffusion instability e.g. [*Lee et al.*, 1998] due to unknown magnetotail conditions.

In this paper we perform a more quantitative optical analysis to that first outlined in *Rae et al.* [2010] over multiple events that display wave-like auroral beads along the substorm onset arc in the minutes leading to substorm onset. For each substorm and pseudo-breakup (a sudden auroral brightening in the midnight sector which does not lead to poleward motion or auroral breakup) event, we characterise the spatial and temporal scales of auroral bead growth and azimuthal propagation. This allows the statistical

relationship between wavenumber and growth rate of auroral beads to be found, which we then compare with theoretical predictions of instability characteristics.

2. Optical Analysis

In this study, we use data from the NASA THEMIS mission ASIs. The fields of view of the ASIs form an overlapping array spanning the auroral oval across Canada and Alaska, which covers up to 12 hours of local time. The THEMIS ASIs are white-light auroral imagers that primarily respond to 557.7 nm (green emission) aurora [Mende *et al.*, 2008] and so throughout this study, we assume an emission altitude of 110 km. At zenith the THEMIS ASIs provide up to 1 km spatial resolution and capture images at a 3 s cadence.

An example of a typical isolated substorm onset event used in this study occurs at 04:57 UT on 2nd October 2011 (2011-10-02) and is presented in Figure 1. This event is characterised by a sudden brightening of the auroral arc at 04:57:30 UT followed by poleward expansion. Figure 1*a-f* shows the raw data from the ASI at Gillam (GILL) and the formation and evolution of auroral beads during the 2011-10-02 event. The white box in Figure 1 shows the portion of the ASI field-of-view used in subsequent analysis. Figure 1*a* shows the initial formation of bead-like azimuthal structure along the most equatorward auroral arc. Subsequently, the beads brighten and are visible at regular intervals along the auroral arc (Figure 1*b-d*). In Figure 1*e*, the arc brightens further and starts to move poleward and finally the arc shows non-regular structuring (or “break-up”) and expands poleward out of the field of view of the analysis box. We limit our analysis to the time interval before the aurora expands outside of the white box.

Figure 2a shows a north-south slice (keogram) perpendicular to the arc orientation, which is aligned geomagnetically east-west. The line along which the keogram is made is shown in white in Figure 1a.

In general, the substorm onset arc is closely aligned with geomagnetic latitude [Akasofu, 1964], a fact we utilise in order to characterise the spatial and temporal behaviour of the auroral bead evolution through substorm onset within our denoted field-of-view. Figure 2 panels *b-e* demonstrate our analysis as performed on the 2011-10-02 substorm observed at GILL. Figure 2b shows auroral intensity within our box as a function of geomagnetic longitude (east-west keogram) along the onset arc. The clear formation of auroral beads (Figure 2b) along the substorm onset arc are first observed at the same time as the rapid auroral brightening ($\sim 04:57:30$ UT). The periodic auroral beads initially have a westward phase propagation, but interestingly develop eastward phase propagation around 20 s later. Figure 2c shows the time evolution of the spatial Fourier transform in the longitudinal direction in order to quantify the spatial periodicity of the auroral beads during this substorm. In order to reduce edge effects, we de-trend the data in time and space using a 2-D Hanning window and re-apply the appropriate corrective factor to recover the correct Power Spectral Density (PSD) values. The dynamic PSD in Figure 2c shows that the highest powers are located at $k_{lon} \approx 0.5 - 1.5 \times 10^{-4} \text{ m}^{-1}$ during the initial beading. It is important to note that the power over a range of k_{lon} grows exponentially over an interval that encompasses the visually-identified onset at 04:57:30 UT. Hence, for each k_{lon} , we identify intervals of exponential growth that occur during substorm onset. Figure 3 shows an example of an exponentially growing mode during this event at $k_{lon} = 0.9 \times 10^{-4} \text{ m}^{-1}$. We use an algorithm to detect exponential growth of the

power spectral density time series. We use a linear fitting method based upon the least absolute deviations technique to determine growth rate, duration and start and end time (given by the start and end of the linear fit) for each k_{lon} . This algorithm requires *a)* that exponential growth must be continually present over a duration longer than 30 s, since this is the typical period of a bead fluctuation [Rae *et al.*, 2010], *b)* that it occurs before the aurora expand poleward out of the analysis field-of-view and *c)* that it must start within the window identified to contain substorm onset. In order to define a reasonable onset window, we define the onset window start time as the mean exponential growth start time (the mean of the individual wavenumbers displayed in Figure 2*c*) for all $k_{lon} \pm 1.5\sigma$ where σ is the standard deviation of the growth start times over all k_{lon} . This criteria ensures that wavenumbers which start to grow much earlier or much later than substorm onset are not taken into account, as we assume they are not part of the linear evolution of the instability. The linear stage of an instability is when the wave amplitudes grow exponentially in time [Treumann and Baumjohann, 1997]. The duration for which each individual wavemode exhibits exponential growth as found by the linear fitting algorithm is shown by the coloured bars in Figure 2*d*. The coloured bars represent the growth rate that each mode has. The onset window start time is denoted by the first vertical black line (average start time over all k_{lon} as discussed above), and the second vertical black line denotes the time at which the auroral beads expand poleward outside the analysis field-of-view marked in white in Figure 1. Finally, Figure 2*e* shows growth rates as a function of k_{lon} in the ionosphere ($k_{lon,i}$) and the magnetosphere ($k_{lon,m}$). From this plot we can infer the most unstable wavenumber, the wavenumber which exhibits the highest growth rate. This wavenumber and corresponding growth rate allows us to compare with

plasma instability theory (see Section 3) in order to identify which instability agrees with our observations of the highest growth rates at specific spatial scales.

Figure 2 demonstrates that although the sudden brightening of the auroral arc can be visually identified at 04:57:30UT, the analysis of the spectral content of the aurora shows that exponential growth of individual wavenumbers commences around 04:56:15UT. The growth rates peak at 0.045 s^{-1} at longitudinal wavenumbers measured in the ionosphere of $k_{lon,i} = 2.0 \times 10^{-4} \text{ m}^{-1}$ in this event, or $k_{lon,m} = 6.0 \times 10^{-6} \text{ m}^{-1}$ when mapped into the magnetosphere using a T96 model [Tsyganenko, 1995].

3. Statistics of Auroral Beads

We use the technique outlined in the previous section to analyse the growth rates and spatial scales of each of 17 isolated substorm and pseudo-breakup onset arcs that contained visually-identifiable auroral beads which form along a pre-existing arc. We note that the auroral beads in our identified events always form along a pre-existing arc, which brightens and corresponds to the substorm onset arc. Hence, beading, pre-existing arc, and substorm onset arc all refer to the same arc. We limit these events to those whose longitudes are close to the centre of the field-of-view of the ASIs so that the beads are generated within the analysis box and remain in the same ASI for the duration of the exponentially growing phase. Table 1 provides our event list and relevant characteristics including magnetic local time (MLT), magnetic latitude and longitude of the arc and direction of bead propagation. These characteristics were all identified from the auroral data only. Of particular note is that all 17 wave-like auroral events occurred in the pre-midnight sector. There is no consistent azimuthal phase propagation; the direction of bead propagation varies between eastward (8 events), westward (3 events), both directions (3 events) and non-propagating

(3 events), and so there is only a slight preference towards Eastward propagation (i.e., towards midnight in the pre-midnight sector). The magnitude of growth rates measured varies widely between events; maximum growth rates range over an order of magnitude between $0.03 - 0.3 \text{ s}^{-1}$, with a median growth rate of 0.05 s^{-1} . However, for each individual event it was usually possible to discern a peak in growth rates at a particular spatial scale. The upper growth rates are not limited by the frequency of the ASI as we require a minimum duration of growth of 30 s. This allows us to observe growth rates above the cadence of our imager.

Using global auroral imaging, *Henderson* [2009] estimated the a growth rate of 0.005 s^{-1} from the total auroral intensity changes over three consecutive images spanning 4 minutes. *Henderson* [2009] notes that ‘*as described by Cowley and Artun [1997], the growth could have been associated with an even faster “explosive” instability that leads to a “detonation”*’. Since our ASI analysis is at a significantly higher temporal resolution and we can resolve individual wavenumbers, we conclude that it is very likely that *Henderson* [2009] has indeed underestimated the growth rates. We discuss the ramifications of this result further below.

Figure 4 shows growth rates as a function of k_{lon} in two formats. Figure 4 (left) shows box plots of the statistical analysis of growth rate as a function of spatial scale, where median occurrence is highlighted as blue horizontal lines, the large boxes represent the range of upper and lower quartiles (25th - 75th percentiles) and the smaller boxes represent the upper and lower deciles (10th - 90th percentiles). Figure 4 (right) shows the probability occurrence statistics of growth rate as a function of spatial scale to demonstrate how likely a particular growth rate and k_{lon} will be observed.

Figure 4a shows statistics of growth rates as a function of ionospheric wavenumber, $k_{lon,i}$, which are calculated assuming an emission height of 110 km altitude. It is evident from both the (left) median and (right) probability distributions that growth rates as a function of ionospheric wavenumber appear relatively flat and the median varies between $0.04 - 0.05 \text{ s}^{-1}$ as a function of $k_{lon,i}$. The Mann-Whitney U-test confirmed that the small difference observed in median growth rates is not statistically significant [Mann and Whitney, 1947]. This means that there is no preferred or more unstable wavenumber than others as deduced solely from ionospheric measurements.

We propose that auroral beads are the ionospheric manifestation of a magnetospheric plasma instability, as previously concluded by Rae *et al.* [2010]; Motoba *et al.* [2012]. To investigate the growth and structuring of magnetospheric waves that could be responsible for these ionospheric auroral beads, we map the azimuthal bead structure from the ionosphere into the equatorial plane of the magnetosphere. We use the Tsyganenko 1996 (T96) magnetic field model which depends upon solar wind dynamic pressure and y and z components the interplanetary magnetic field and the geomagnetic Disturbance Storm-Time index (Dst) [Tsyganenko, 1995]. Magnetospheric mapping during highly dynamic substorm times is unreliable, however magnetospheric mapping is important in this study in order to estimate the magnetospheric wavenumber and remove latitudinal effects from the scaling of the ionospheric wavenumber. Equilibrium magnetic field mapping cannot be assumed to be reliable at substorm times due to the stretching of the tail as flux builds up in the lobes during the substorm growth phase. This means that field line stretching is likely to be underestimated. We chose only events that demonstrate steady equatorward motion of the growth phase arc prior to rapid auroral brightening, indicative of a classic

substorm growth phase [McPherron, 1970]. This will not eliminate errors, however this allows us to assume that the magnetic field model systematically underestimates substorm auroral bead spatial scales in the magnetosphere. The mapped spatial scales are therefore directly comparable between events even if the absolute value is likely to be lower than its actual magnitude [Pulkkinen *et al.*, 1991]. Using the T96 model to estimate the source location of the auroral arcs, we find that the arcs map to a range of distances between 8-18 R_E in the equatorial plane of the magnetosphere, with the majority lying between 9-12 R_E . Beyond 9 R_E the model predicts magnetic field strengths in the plasma sheet which are < 20 nT.

Using this assumption, Figure 4b shows the statistics of mapping $k_{lon,i}$ along a T96 magnetic field to estimate $k_{lon,m}$. Again, growth rates appear relatively flat as a function of azimuthal wavenumber, suggesting that there is no preferred wavenumber observed during these events in the magnetosphere either. This might be a result of the tail being in differing states during each substorm creating a continuum of unstable wave numbers; statistically this would result in the flat distribution we observe. However the Mann-Whitney U-test on this distribution suggests that the growth rates in the ranges $k_{lon,m} = 2.5 - 5.0 \times 10^{-6} \text{ m}^{-1}$ are larger than the others, and that this result is statistically significant to a 95% certainty.

As noted previously, in general there is a well-defined peak in growth rate in individual case studies, but the size of the growth rate varies dramatically from event to event, by an order of magnitude. Assuming that a specific magnetospheric instability explains the azimuthal auroral beading and auroral substorm onset, it is entirely conceivable that the rate of growth is dependent upon unknown magnetospheric parameters such as plasma

density or temperature [Forsyth *et al.*, 2014], or that solar wind driving affects the ionospheric response [Sergeev *et al.*, 2014]. In other words, even though we cannot determine the specific magnetotail characteristics during each substorm, we assume that a single magnetotail instability could explain our results and investigate the implications. It must be noted that our observations demonstrate that only one instability is operating in the first few minutes of auroral beading since the exponential growth of each k-mode exhibits only one well-defined growth rate during this interval. After the aurora expands outside of our analysis domain, any number of additional instabilities may be operating.

Hence in Figure 4c we normalise the growth rates during each event to the largest growth rate in that event to investigate whether the magnetospheric spatial scales are repeatable across events. By assuming that the same instability can grow at different rates, Figure 4c shows a discernible peak in growth rates at $k_{lon,m} \approx 2.5 - 3.75 \times 10^{-6} \text{ m}^{-1}$ in both occurrence and medians, which corresponds to an azimuthal magnetospheric wavelength of $\lambda_{\perp} \approx 1700 - 2500 \text{ km}$ (where $\lambda_{\perp} = 2\pi/k_{lon,m}$). This is comparable to the ion gyroradius in a 6 – 9 nT field and therefore provides evidence that the ions may play an important part in the evolution of the instability. The Mann-Whitney U-test confirms that the peak observed in this wavenumber range is statistically significant to a 98% certainty when the growth rates are normalised. We reiterate that the wavelength is likely to be underestimated due to magnetospheric mapping during the substorm growth phase, discussed above [Pulkkinen *et al.*, 1991]. We note that using a different empirical magnetic field model such as T89 does not change the result that there is a distinct peak of growth rates with magnetospheric wavenumber, across a similar range.

4. Comparison with Candidate Plasma Instabilities

Previous studies of auroral beads suggest that this ionospheric phenomenon is triggered by a magnetospheric instability. However, there has been no explicit quantitative and statistical comparison of values of the temporal (i.e., growth rates) and spatial (i.e., azimuthal wavenumbers) evolution of the beads in order to compare with instability theory.

Lui [2004] and references therein identified numerous plasma instabilities which may be involved in the initiation of substorm onset. Our observations allow us to rule out several promising plasma instabilities for our substorm events: - The tearing instability [*Coppi et al.*, 1966] and the drift kink/sausage instability [*Zhu and Winglee*, 1996] have too slow growth rates and a radial k structuring; - The current-driven Alfvénic instability [*Perraut et al.*, 2000] and lower-hybrid drift instability [*Yoon et al.*, 1994] predict growth rates and frequencies which are larger by an order of magnitude than those observed. However, in a previous study of an isolated event, *Rae et al.* [2010] were unable to rule out the Kelvin-Helmholtz instability which is predicted to have growth rates that peak at low k_{lon} by *Yoon et al.* [1996]. Our statistical observations allow us to rule this out, because the growth rates associated with this instability are over of an order of magnitude greater than the rates we observe [*Hallinan and Davis*, 1970]. These instabilities have been ruled out on a combination of the growth rate magnitude and the spatial structuring of the excited waves. This means that the systematic errors acquired by magnetospheric mapping do not affect this conclusion.

This leaves the Cross-Field Current Instability [*Lui et al.*, 1991; *Lui*, 1996, 2004] and the Ballooning Instability [*Voronkov et al.*, 1997; *Pu et al.*, 1999; *Zhu et al.*, 2004], both of which can explain azimuthal structuring of the onset arc and growth rates consistent with

time scales observed. We directly compare Shear-Flow Ballooning Instability [Voronkov
et al., 1997] and Cross-Field Current Instability with our observations.

The challenge with studying the plasma instabilities invoked in substorm onset is to
determine where the instability is initiated in the magnetotail. The Cross-Field Current
Instability as outlined in *Lui et al.* [1991] is studied using plasma sheet parameters ob-
served in a statistical study of 15 current disruption events outlined in *Lui et al.* [1992] at
radial distances of 7.4 - 8.8 R_E . As previously stated we estimate that the auroral onset
arcs do not map this close to Earth, but to the region 9-12 R_E typically associated with
the substorm onset initiation. This location is where the field changes from dipole-like to
a more stretched tail-like configuration [Samson *et al.*, 1992a; Rae *et al.*, 2014]. Hence,
the current disruption events observed from space in *Lui et al.* [1992] may have been ini-
tiated at larger radial distances in the tail than inferred. Later, the instability is observed
closer to Earth as the substorm current wedge (SCW) expands radially and azimuthally.
Lui et al. [1991] present growth rates as a function of magnetospheric wavenumber of
the Cross-Field Current Instability in the near-Earth and mid-tail plasma sheet. In the
near-Earth region the B_z component of the magnetic field is 25 nT. Assuming a T96 field;
 $B_z = 25$ nT maps to $\sim 8.5 R_E$ in the tail. This agrees with the locations where the in-
stability was observed by *Lui et al.* [1992]. Hence, the substorm onset arc and location of
the auroral beading is broadly consistent with the magnetic field magnitudes in the tran-
sition region between stretched and dipolar field lines Samson *et al.* [1992a]; *Lui* [1991],
although $\sim 8.5 R_E$ is closer than our field mapping implies. In the mid-tail region *Lui*
et al. [1991] selects 5 nT for the B_z component of the magnetic field, which corresponds
to $\sim 13 R_E$ in the tail using T96. There is a similar problem with the Shear-Flow Bal-

looming Instability as described by *Voronkov et al.* [1997], which does not quantitatively specify a region where the instability is likely to be triggered, but simply states ‘*the inner edge of the plasma sheet*’ where ‘*magnetic field lines are slightly stretched tail ward*’. The analysis of *Voronkov et al.* [1997] uses $B_z = 40$ nT which, from the T96 model maps to $7.6 R_E$ downtail. However *Zhu et al.* [2004] find that the ballooning instability is excited for plasma β values in the range of $\sim 1 - 100$. In plasmas with a higher β the high plasma pressure and therefore compression stabilises the linear ballooning instability. The plasma parameters given by *Lui et al.* [1991, 1992] give a beta values of $\beta = 4.4$ which lies in this range. However it is unclear how different magnetic field strengths affect the growth rates of this instability. There is a large region of the plasma sheet that satisfy these β values [*Walsh et al.*, 2013], which suggests that a large area of the plasma sheet could be unstable to the Ballooning instability. In order to investigate whether it is possible for this instability to be triggered with lower B_z a full analysis of the relevant equations is required, which is beyond the scope of this work and will be explored in future.

4.1. Cross-Field Current Instability

The Cross-Field Current Instability (CFCI), as its name suggests, obtains its free energy from the cross-field current due to an increase in resistivity in the near-Earth region of the inner plasma sheet when the edge of the plasma sheet moves Earthward during the substorm growth phase. The plasma sheet thins down to a thickness comparable with an ion gyro-radius, allowing the ions to become demagnetised and drift duskward whilst electrons remain frozen to magnetic field lines. The instability takes the form of an ion Weibel mode (IWI) [*Lui et al.*, 1993] with wavenumbers parallel to the background magnetic field and the modified two-stream instability (MTSI) with wavenumbers per-

pendicular to the background magnetic field *Lui et al.* [1991]. The angle of the waves excited is dependent on the relative ion drift speed. Higher θ (more perpendicular) waves are generated at lower drift velocities (V_0), corresponding to the domination of the MTSI. The more parallel propagating waves (IWI) excited at higher drift velocities have shorter wavenumbers (k). If the IWI mode is suppressed by a thin current sheet, then the MTSI will dominate leading to a more perpendicular wave propagation [*Lui et al.*, 1991]

Lui et al. [1991, 1992] investigate the CFCI using parameters representative of the inner-edge and mid tail region of the plasma sheet. For the inner-edge $V_0 = 0.5v_i$, $n_e = n_i = 0.6 \text{ cm}^{-3}$, $T_i/T_e = 4$ $T_i=12 \text{ keV}$ and $B_z = 25 \text{ nT}$. For the mid-tail region $V_0 = v_i$, $n_e = n_i = 0.3 \text{ cm}^{-3}$, $T_i/T_e = 10$ $T_i=2 \text{ keV}$ and $B_z = 5 \text{ nT}$. Note that a full analysis of all parameters is beyond the scope of this work and will be explored in future with added constraints from spacecraft data. Figure 5 shows the growth rates as a function of wavenumber from both the inner-edge and mid-tail plasma parameters. The growth rates for the inner-edge parameters are higher in comparison to our auroral observations. However a clear peak in growth rates can be observed at $k_{lon} = 7.0 \times 10^{-6} \text{ m}^{-1}$. The maximum growth rate for the mid-tail parameters is lower, however the growth rate distribution is almost flat at low wavenumbers. *Lui et al.* [1991] calculate the maximum growth rates for a variety of drift velocities. These are shown in Table 2 and demonstrate that the growth rates predicted in the near-Earth plasma sheet are much too high. The maximum rate for the mid-tail plasma sheet with a drift velocity of $V_0 = 0.3v_i$ is more consistent with our observations.

Figure 6a shows a comparison of our statistical results with the characteristics of the CFCI for varying plasma sheet locations. Our statistical results demonstrate maximum

growth rates at small wavenumbers. The magnitudes of the growth rates are in better agreement with the mid-tail parameters, however the observed variation of growth rate with wavenumber is not replicated by the CFCI.

In summary, using plasma sheet parameters indicative of the mid-tail magnetotail region with low drift velocities, the CFCI predicts growth rate magnitudes of the same order as those inferred from auroral growth rates. At higher B_z corresponding to close to the inner edge of the plasma sheet, the peak in growth rate becomes more pronounced, but occurs at larger wavenumbers and higher growth rates than inferred. The growth rates for the mid-tail parameters do not exhibit a clear peak in growth rates we infer when assuming that the beads are the signature of the same instability. Further investigation of the effect of changing the parameters needs to be done in order to definitively rule this instability in or out.

4.2. Shear-Flow Ballooning Instability

The Shear-Flow Ballooning Instability (SFBI) is a hybrid instability incorporating the Kelvin-Helmholtz instability, driven by small-scale shear flows and the Rayleigh-Taylor instability, driven by large-scale Earthward-directed pressure gradients. Strong azimuthal shear velocities have been observed in the equatorial regions of field line resonances. For example *Samson et al.* [1996] report of shears up to 200 km s^{-1} over radial distances of the order of $0.1 R_E$. The hybrid SFBI possesses significantly faster growth rates and shorter time scale exponential growth than a pure Kelvin-Helmholtz mode, making it a suitable candidate to compare with the growth rates obtained from our optical analysis. The substorm onset arc is tied to the boundary between stretched and more dipolar field at

the inner edge of the plasmashet *Samson et al.* [1992b], and in precisely the region where pressure gradients control the physics behind the Shear-Flow Ballooning Instability.

The MHD equations for the radial component of the shear flow velocity V_x is given by:

$$V_x'' = k^2 V_x \left(1 - \frac{V_0''}{k(\omega - kV_0)} - \frac{W}{(\omega - kV_0)^2} \right) \quad (1)$$

where

$$W = -\frac{g\rho_0'}{\rho_0} - \frac{g^2}{V_f^2}$$

and $\omega - kV_0(x)$ is a Doppler-shifted wave frequency, $V_f^2 = C_s^2 + V_a^2$ is the square of the fast mode velocity, C_s is the acoustic velocity, V_a is the Alfvén velocity and $V_0(x)$ the shear flow velocity, V_x'' and V_0'' denotes the second derivative with respect to x and g is the centripetal acceleration of the particles as a result of magnetic curvature and particle inertia. When $W > 0$ the pressure gradient is stable, and for $W < 0$ it is unstable and hence able to take part in substorm onset.

Using magnetic field component: $B_z = 40nT$ and plasma sheet mass density $\rho = 4.06 \times 10^{-21} \text{ kg m}^{-3}$ as given in *Voronkov et al.* [1997], we find that the growth rate peaks at 0.2 s^{-1} and there is an inverse relationship between the most unstable spatial scales and the size of the shear flow region. This is in contrast to the CFCI, where an increase in magnetic field strength or ion drift velocity increases the wavenumber at which the growth rate peaks. This is shown in Figure 5 where the absolute growth rates predicted by the SFBI and CFCI are compared. The growth rates as a function of wavenumber for the CFCI presented in *Lui et al.* [1991] with inner-edge and mid-tail plasma sheet parameters are shown in comparison to the growth rates to the SFBI growth rates from *Voronkov et al.* [1997] for a shear flow width of $d = 650 \text{ km}$.

Figure 6b shows a comparison of our statistical results with the characteristics of the SFBI for varying shear-flow regions. Our statistical results demonstrate maximum growth rates at small spatial scales which agree well if the SFBI was driven by a shear flow width in the magnetosphere of 600-700 km. This is an extremely localised region in the magnetosphere, but we should note that if the spatial scales of the instability have been underestimated due to the errors in magnetospheric mapping, this would also underestimate the size of the shear flow region predicted.

Our analysis of the SFBI suggests that some combinations of plasma and magnetic field characteristics are able to explain our observed results. This indicates that the SFBI could be the cause of the substorm onset arc.

5. Discussion & Conclusion

The optical analysis technique presented in this paper provides a quantitative method to remote-sense the physics of substorm onset from spatial analysis of substorm-related aurora. In the ionosphere, we have observed the auroral beads with wavelengths of ~ 60 km, evolving to ~ 120 km, in agreement with previous individual case studies e.g. *Friedrich et al.* [2001]; *Sakaguchi et al.* [2009]; *Rae et al.* [2010]. The statistical analysis of multiple auroral brightenings has yielded vital new constraints on the nature of the plasma instability associated with substorm onsets and pseudobreakups.

Specifically, we find that:

1. The statistical result of the analysis of auroral spatial scales demonstrates the most unstable azimuthal wavelength of the magnetospheric instability is at least $\lambda_{\perp} \approx 1700 - 2500$ km;

2. The most unstable spatial scales have growth rates ranging from $0.03 - 0.3 \text{ s}^{-1}$ with a median growth rate of 0.05 s^{-1} ;

3. The Cross-Field Current Instability in the near-Earth plasma sheet predicts growth rates which are too high and at much smaller azimuthal scales (or larger k) to explain our observations;

4. The Cross-Field Current Instability in the mid-tail region ($B \sim 5 \text{ nT}$) with a drift velocity $V_0 = v_i$ agrees better with the magnitude of the inferred growth rates, however the theoretical growth rates at the same magnetic field strength do not show a clear peak at the right wavenumber as observed. Lower drift velocities ($V_0 = 0.3v_i$) predict growth rates closer to those observed;

5. The Shear-Flow Ballooning Instability with a localised shear flow region of $\sim 650 \text{ km}$ and plasma sheet magnetic field strength of 40 nT can explain our observed results.

More work is necessary to fully investigate the range of plasma and magnetic field conditions that may support the instabilities identified by our analysis of the substorm aurora.

Even though the CFCI predicts waves at similar temporal and spatial scales, further analysis of the plasma characteristics is required in order to conclude whether combinations of the plasma sheet parameters and drift velocities can predict a peak in growth rates at the spatial scales we observe.

In our analysis we assumed that the same instability was acting in the magnetotail for each event. This would result in the same shape of growth rate as a function of wavenumber, although the magnitude of growth may be different in each instance. Assuming that only one instability is causing the substorm onset arc suggests that the instability most

likely to play a part in the trigger of substorm onset is the Shear-Flow Ballooning Instability, as the peak growth rate of 0.2 s^{-1} at spatial scales of $k_{lon} = 2.5 - 3.75 \times 10^{-6} \text{ m}^{-1}$ is predicted by this instability with a shear flow region of $\sim 650 \text{ km}$. The effect of different plasma parameters such as density, B_z and pressure gradient on the growth rate amplitude and shape as a function of wavenumber requires further investigation. However if this assumption is incorrect and the instabilities occurring in each event are different, then this normalisation is unjustified. Without any additional information on the magnetotail plasma and magnetic field state, we cannot explore whether only one instability could be responsible for generating auroral beads.

The purpose of this manuscript is to statistically show that the formation and evolution of auroral beads are a signature of the linear stage of an instability. We have used our analysis to provide the characteristics of the growth rates and spatial scales of the most unstable wavenumbers of this instability. However how the instability accelerates auroral electrons to form the auroral beads we observe is the next logical step.

We show for the first time a quantitative comparison between observations of the spatial and temporal structuring of the substorm onset arc and its relation to proposed magnetotail instability mechanisms. We statistically demonstrate the evolution in space and time of the substorm onset arc, providing the clearest indication yet that the substorm onset arc itself is both wave-driven and is inextricably linked to a magnetotail instability. The auroral beads exhibit exponential growth across a broad range of spatial scales in the ionosphere initially suggesting that there are no preferential spatial scales for auroral bead growth. However when we make two relatively simple and reasonable assumptions, that magnetic field mapping introduces a systematic error, and that substorms can grow

at different temporal rates, we find that there is indeed a preferred k spectrum peaking at low wavenumbers. To provide further evidence that we are measuring the ionospheric optical manifestation of a magnetospheric instability in-situ space measurements are required. Our results provide the strongest evidence yet that the substorm onset arc is created by a plasma instability such as the Shear-Flow Ballooning Instability [Voronkov *et al.*, 1997]. We use a combination of ground-based data and magnetic field mapping to predict the location of the instability in space and its spatial scales. By doing so, we provide important estimates of the characteristics of the magnetotail region driven unstable during the substorm and containing the substorm onset arc. Using these predictions, we suggest the first observational test in the magnetotail that could finally identify the magnetospheric source of the substorm plasma instability and ultimately the cause of the substorm onset arc itself.

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Figure 1. Auroral beads along the onset arc during the auroral substorm observed at GILL ASI on 2011-10-02. Lines of geomagnetic latitude at 67.8° and 68.4° and geomagnetic longitude at -33.0° and -24.0° define the field of view of our analysis and show the onset arc is aligned with constant geomagnetic latitude. We track the temporal and spatial evolution of the auroral beads within this white box in our subsequent analysis. The line perpendicular to the arc along which we use for the keogram in Figure 2a is shown in Figure 1a. The formation and evolution of the beads is observed with time. After 04:58:30 UT (*e*) the aurora expands poleward out the box, as can be seen at a later time in (*f*).

Figure 2. Optical analysis for substorm at Gillam on 2011-10-02. (a) North-South Keogram to show auroral brightening and poleward propagation. (b) East-West Keogram along a line of geomagnetic latitude (as a function of longitude) to track periodic azimuthal structure along the onset arc. (c) Power Spectral Density as a function of longitudinal wavenumber measured in the ionosphere, $k_{lon,i}$. (d) periods of exponential growth for each $k_{lon,i}$, where the duration of exponential growth is marked by the length of the horizontal line and the growth rate denoted by the colour. The interval encompassing substorm onset is marked by the vertical lines. Only wavenumbers that grow for over 30s and start within 1 standard deviation of the median start time are used and (e) Growth rate as a function of azimuthal wavenumber for those wavenumbers that demonstrate exponential growth according to (d).

Figure 3. Exponential growth rate determination. The log of the power from the power spectral density (Figure 2c) for a single wavenumber, $k_{lon} = 0.9 \times 10^{-4} \text{ m}^{-1}$, plotted against time shows the times between which there is exponential growth denoted by the linear fit (red). The growth rate is given by the gradient of the fit.

Figure 4. (left) A boxplot statistical analysis of growth rate as a function of spatial scale, where medians are denoted by the blue line, the large boxes represent the range of upper and lower quartiles and the smaller boxes represent the upper and lower deciles and (right) Growth rate probability occurrence plot as a function of (a) wavenumber $k_{lon,i}$ measured in the ionosphere, (b) $k_{lon,i}$ mapped to space using T96 magnetic field model, $k_{lon,m}$ and (c) Growth rates normalised to maximum growth rate for each event as a function of $k_{lon,m}$. Subscripts i and m denote ionosphere and magnetosphere respectively. Note that in order to render meaningful statistics, we group spatial scales into larger bins than are observed in (a) & (b). The boxes shown in grey indicate that less than 20 points are represented in this wavenumber range.

Figure 5. The growth rates as a function of wavenumber for the Cross-Field Current Instability with inner-edge (green) plasma sheet parameters: $V_0 = 0.5v_i$, $T_e = 3$ keV, $T_i = 12$ keV and $n_e = n_i = 0.6$ cm⁻³, and mid-tail (orange) plasma sheet parameters: $V_0 = v_i$, $T_e = 0.2$ keV, $T_i = 2$ keV and $n_e = n_i = 0.3$ cm⁻³. The growth rates as a function of wavenumber for the Shear-Flow Ballooning Instability (blue), where $\rho = 4.06 \times 10^{-21}$ kg m⁻³, $B = 40$ nT and shear flow width, $d = 650$ km. The SFBI predicts lower growth rates than the CBCI with a peak at wavenumbers of $k_{lon,m} \approx 3.0 \times 10^{-6}$ m⁻¹.

Figure 6. The normalised growth rate as a function of spatial scale for: (left) the Cross-Field Current Instability for inner-edge plasma sheet parameters (green) where $V_0 = 0.5v_i$, $T_e = 3$ keV, $T_i = 12$ keV and $n_e = n_i = 0.6$ cm⁻³ and mid-tail plasma sheet parameters (orange) where $V_0 = v_i$, $T_e = 0.2$ keV, $T_i = 2$ keV and $n_e = n_i = 0.3$ cm⁻³. (right) Shear Flow Ballooning instability, where $\rho = 4.06 \times 10^{-21}$ kg m⁻³, $B = 40$ nT. Keeping these parameters constant, different growth rate curves are obtained by varying the width of the shear-flow region. The growth rate curves have been normalised to 0.7 which corresponds to a growth rate of 0.2 s⁻¹ to facilitate qualitative comparison with the normalised growth rates from observation. The boxes shown in grey indicate that less than 20 points are represented in this wavenumber range.

Date	ASI Station	Time UT	MLT	Arc MLAT	Arc MLON	Bead Propagation
2008-03-28	GILL	05:36:00	22:26:00	66.2 - 66.8	-33.0 - -22.0	Eastward
2005-11-28	FYKN	10:08:00	22:56:00	64.5 - 66.0	-100.0 - -90.0	Eastward
2006-01-27	FYKN	10:00:00	22:52:00	66.0 - 67.4	-100.5 - -91.5	None
2006-02-22	FSMI	06:26:30	21:32:00	66.4 - 67.1	-60.0 - -52.0	Westward
2006-02-28	WHIT	09:09:30	22:40:00	66.5 - 67.2	-88.0 - -80.0	Eastward
2007-02-14	GILL	05:07:00	22:24:00	64.9 - 65.8	-35.0 - -20.9	Eastward
2007-03-07	SNKQ	05:50:00	23:35:00	64.9 - 66.1	-15.0 - -5.5	Eastward
2008-10-02	SNKQ	04:29:00	22:56:00	66.8 - 67.15	-8.0 - -2.0	None
2009-01-03	GILL	04:36:00	21:18:00	66.7 - 67.2	-35.0 - -24.0	Westward
2009-02-24	FSIM	07:32:00	21:50:00	67.3 - 67.6	-70.0 - -63.0	None
2009-03-15	GILL	04:28:00	21:36:00	67.7 - 68.2	-30.0 - -20.0	Westward
2010-03-07	GILL	05:15:00	22:08:00	64.8 - 66.0	-39.0 - -25.0	Both
2010-12-31	FSMI	06:37:00	21:22:00	66.2 - 67.1	-64.0 - -53.0	Eastward
2011-03-08	GILL	06:24:00	23:06:00	66.9 - 67.3	-38.0 - -27.0	Eastward
2011-10-02	GILL	04:55:00	21:16:00	67.8 - 68.4	-45.0 - -15.0	Eastward
2008-03-23	GILL	05:44:00	22:24:00	67.4 - 68.0	-31.0 - -25.0	Eastward
2008-02-26	RANK	04:50:00	21:22:00	69.3 - 71.0	-35.0 - -22.0	Both

Table 1. Event list-The substorm and pseudo-breakup event list used in this study, including date, ASI station, substorm time and MLT, onset arc initial magnetic latitude and longitude, bead propagation direction and whether this auroral arc brightened but did not expand polewards (pseudo-breakup) or whether the arc expands poleward and “breaks-up” (substorm)

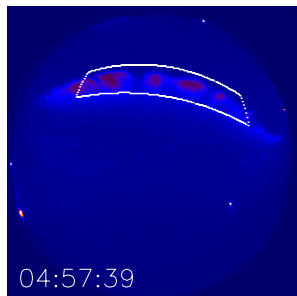
V_0/v_i	0.3	0.5	1.0	2.6	9.0
γ - mid-tail	0.052			0.62	2.0
γ - near-Earth		0.36	1.12		

Table 2. Table of maximum growth rates predicted for different drift velocities for waves in the near-Earth and mid-tail current sheet from *Lui et al.* [1991]

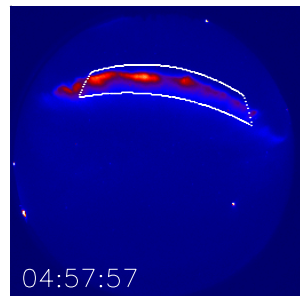
a)



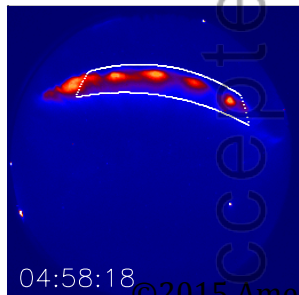
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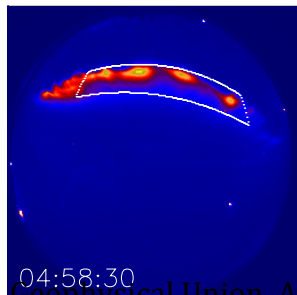
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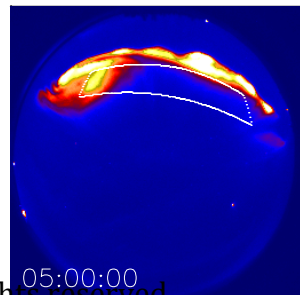
d)



e)



f)



04:55:00 04:57:00 04:59:00 05:01:00 05:03:00

