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Lattice Dynamics and Negative Thermal Expansion in the Framework Compound $\text{ZnNi}(\text{CN})_4$ with 2-D and 3-D Local Environments

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Abstract

$\text{ZnNi}(\text{CN})_4$ is a 3-D framework material consisting of two interpenetrating PtS-type networks in which tetrahedral $[\text{ZnN}_4]$ units are linked by square-planar $[\text{NiC}_4]$ units. Both the parent compounds, cubic $\text{Zn}(\text{CN})_2$ and layered $\text{Ni}(\text{CN})_2$, are known to exhibit 3-D and 2-D negative thermal expansion (NTE), respectively. Temperature-dependent inelastic neutron scattering (INS) measurements were performed on a powdered sample of $\text{ZnNi}(\text{CN})_4$ to probe phonon dynamics. The measurements were underpinned by *ab-initio* lattice dynamical calculations. Good agreement was found between the measured and calculated generalized phonon density-of-states, validating our theoretical model and indicating that it is a good representation of the dynamics of the structural units. The calculated linear thermal expansion coefficients are $\alpha_a = -21.2 \times 10^{-6} \text{ K}^{-1}$ and $\alpha_c = +14.6 \times 10^{-6} \text{ K}^{-1}$, leading to an overall volume expansion coefficient, α_V of $-26.95 \times 10^{-6} \text{ K}^{-1}$, pointing towards pronounced NTE behaviour. Analysis of the derived mode-Grüneisen parameters shows that the optic modes around 12 and 40 meV make a significant contribution to the NTE. These modes involve localised rotational motions of the $[\text{NiC}_4]$ and/or $[\text{ZnN}_4]$ rigid units, echoing what has previously been observed in $\text{Zn}(\text{CN})_2$ and $\text{Ni}(\text{CN})_2$. However, in $\text{ZnNi}(\text{CN})_4$, modes below 10 meV have the most negative Grüneisen parameters. Analysis of their eigenvectors reveals that a large transverse motion of the Ni atom in the direction perpendicular to its square-planar environment induces a distortion of the units. This mode is a consequence of the Ni atom being constrained only in two dimensions within a 3-D framework. Hence, although rigid-unit modes account for some of the NTE-driving phonons, the added degree of freedom compared with $\text{Zn}(\text{CN})_2$ results in modes with twisting motions, capable of inducing greater NTE.

I. Introduction

Negative thermal expansion (NTE) is a counter-intuitive phenomenon attracting keen fundamental and applied scientific interest. NTE often occurs in framework materials in 1-, 2- or 3-dimensions [1]. With better understanding of its mechanism, there is the potential to tailor materials with a targeted thermal response or composite materials with an overall zero thermal expansion. Applications range from aerospace technology (for example, in telescope mirrors and optics exposed to extreme temperature in space) to biomedical engineering (for example, in prostheses, implants and dental fillings).

NTE in inorganic framework compounds stems from anharmonic lattice vibrations that shorten the mean distances between atoms [2]. Well-known NTE compounds include Ag_2O , ReO_3 , ScF_3 , ZrW_2O_8 and $\text{Sc}_2\text{Mo}_3\text{O}_3$ [1]. Due to the *tension effect*, the transverse displacement of bridging ligands, neighbouring metals are brought closer together. An increase in temperature results in an increase in amplitude of such a transverse vibration and hence a reduction in lattice parameter. For structures, such as those above, consisting of corner-sharing polyhedra, little or no polyhedral distortion results from the phonon modes giving rise to the *tension effect*. These modes are known as rigid-unit-modes (RUMs), and are often related to NTE. As a diatomic ligand, such as $\text{C}\equiv\text{N}$, would reduce the structural constraints of a RUM, NTE is often observed in transition-metal cyanides [3, 4, 5, 6].

Metal cyanides exhibiting NTE include $\text{Zn}(\text{CN})_2$ and $\text{Ni}(\text{CN})_2$ [4, 5]. $\text{Zn}(\text{CN})_2$ adopts a cubic structure consisting of two interpenetrating diamondoid frameworks formed from corner-sharing tetrahedra [5]. It exhibits 3-D NTE with a linear thermal expansion coefficient, α_a , of $-16.9 \times 10^{-6} \text{ K}^{-1}$, corresponding to a volume thermal expansion, α_v , of $-51 \times 10^{-6} \text{ K}^{-1}$ [7]. In contrast, $\text{Ni}(\text{CN})_2$ has a layered structure consisting of Ni^{2+} -centred corner-sharing square-planar units. This leads to 2-D NTE in the plane of the layers with α_a equal to $-6.5 \times 10^{-6} \text{ K}^{-1}$, where $a = b$ is the in-plane lattice parameter, and a positive thermal expansion perpendicular to the layers resulting in an overall positive volume expansion, α_v , of $+48 \times 10^{-6} \text{ K}^{-1}$ [4]. In both compounds, the dimensionality of the NTE follows the dimensionality of the structure, a feature also displayed by the Group 11 metal cyanides (e.g. CuCN , AgCN and AuCN), which have structures based on 1-D chains and show 1-D NTE [3, 8]. Inelastic neutron scattering (INS) and *ab initio* studies of $\text{Ni}(\text{CN})_2$ and $\text{Zn}(\text{CN})_2$ have confirmed the existence of low-energy phonon modes with negative Grüneisen parameters, which give rise to NTE [9]. In $\text{Zn}(\text{CN})_2$, Fang *et al.* have shown that there is a strong correlation between a mode having a negative Grüneisen parameter and its resemblance to a pure RUM [10].

The structures of $\text{Ni}(\text{CN})_2$ and $\text{Zn}(\text{CN})_2$ contain metals in only one type of coordination geometry, with Ni^{2+} in a 2-D (square-planar) and Zn^{2+} in a 3-D (tetrahedral) environment. Recent studies combining 3-D units (tetrahedral or octahedral) with pseudo 1-D units (from Group 11 metals) within the same compound have resulted in materials with three-dimensional structures which have very large linear thermal expansion coefficients. Examples include $\text{ZnAu}_2(\text{CN})_4$ and $\text{Ag}_3[\text{Co}(\text{CN})_6]$ [11, 12, 13]. The lower constraint of a 1-D metal environment within a 3-D framework naturally induces phonons with large RUM-like motions.

This work reports on $\text{ZnNi}(\text{CN})_4$, the structure of which contains metals in both 2-D and 3-D local environments [14]. Single crystals of $\text{ZnNi}(\text{CN})_4$ were first reported by Yuan *et al.* [14]. The tetragonal structure consists of two interpenetrating cooperite (PtS) type $\text{ZnNi}(\text{CN})_4$ frameworks (Figure 1). A second crystal structure, also tetragonal, but consisting of a single $\text{ZnNi}(\text{CN})_4$ framework was later reported [15].

The dual metal-environment dimensionality of $\text{ZnNi}(\text{CN})_4$ provides a different and interesting system for studying phonon dynamics and its relationship to NTE. Indeed, another PtS-type framework compound, $\text{Cd}(\text{NH}_3)_2[\text{Cd}(\text{CN})_4]$, has recently been discovered as a new NTE material [16]. Here we present a detailed lattice dynamical study of $\text{ZnNi}(\text{CN})_4$ using INS and *ab initio* calculations. In addition, total neutron diffraction, powder X-ray diffraction (XRD), infra-red (IR) and Raman spectroscopy data are also reported and discussed. This work, to the best of our knowledge, is the first of its kind to report the lattice dynamics of a compound with a PtS-type structure.

II. Experimental Details

A 2 g sample of $\text{ZnNi}(\text{CN})_4$ was synthesised as follows: 50 ml aqueous solution of $\text{K}_2\text{Ni}(\text{CN})_4 \cdot n\text{H}_2\text{O}$ (Aldrich) (5.2808 g, 0.022 mol) was added to 50 ml of $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ (BDH) (6.5199 g, 0.022 mol). The resulting gelatinous precipitate, cream in colour, was stirred for three hours, filtered, and repeatedly washed with distilled water. The wet product was then dried in a vacuum oven for 1 hour at 373 K. The sample density was measured at room temperature using a Quantachrome micropycnometer with helium gas as the working fluid. IR frequencies were measured with a Perkin Elmer Spectrum 100 spectrometer and Raman frequencies with a Renishaw InVia Raman microscope ($\lambda_{\text{exc}} = 785$ nm). A powder X-ray diffractogram was collected in transmission mode at room temperature using a Bruker D8 diffractometer equipped with primary monochromatic $\text{Cu K}\alpha_1$ radiation ($\lambda = 1.54060$ Å). The sample was finely ground and loaded into a quartz capillary (0.9 mm O.D.)

Total neutron diffraction data were collected at 15 and 295 K using the time-of-flight GEM diffractometer (ISIS Neutron and Muon Source, Didcot), designed to collect data over a wide-angle range ($1.2 \leq 2\theta \leq 171.4^\circ$). The interference function, $Q_i(Q)$, was obtained by merging data from detector banks 2 - 5 with a Q_{max} of 40 \AA^{-1} and extrapolating the low- Q region with a function of the form $a + bQ_i(Q)^2$ (where a and b are constants). The total neutron correlation function, $T_N(r)$, was obtained by Fourier transform of $Q_i(Q)$, using the Lorch function [17, 18] to reduce the termination ripples. The bond lengths were extracted by fitting the first peaks in the $T_N(r)$ shown in Figure 2 using the method described elsewhere [19, 20].

INS measurements were performed on 2 g sample of $\text{ZnNi}(\text{CN})_4$, using the cold-neutron, time-of-flight, time focusing, IN6 spectrometer (Institut Laue-Langevin, Grenoble), operating in the high-resolution mode, and offering a good signal-to-noise ratio. The IN6 spectrometer supplies a typical flux of $10^6 \text{ n cm}^{-2} \text{ s}^{-1}$ on the sample, with a beam-size cross section of $3 \times 5 \text{ cm}^2$ at the sample position. The sample was placed inside a thin-walled aluminium container and fixed to the tip of the sample stick of an orange cryofurnace. An optimized small sample thickness of 1

mm was used, to minimize effects such as multiple scattering and absorption. An incident wavelength of 4.14 Å was used, with an elastic energy resolution of 0.17 meV, as determined from a standard vanadium sample. The vanadium sample was also used to calibrate the detectors. Data were collected up to 100 meV in the up-scattering, neutron energy-gain mode, at 200, 300 and 400 K. On IN6, under these conditions, the resolution function broadens with increasing neutron energy, and it can therefore be expressed as a percentage of the energy transfer. The ILL program LAMP [21] was used to carry out data reduction and treatment, by performing detector efficiency calibration, background subtraction and multiphonon correction [22]. Background reduction included measuring an identical empty container in the same conditions as sample measurements. At the used shortest-available neutron wavelength on IN6, $\lambda = 4.14$ Å, the IN6 angular coverage ($\sim 10 - 114^\circ$) corresponds to a maximum momentum transfer of $Q \sim 2.6$ Å⁻¹.

The Q -averaged, one-phonon generalized phonon density of states (GDOS) [23], $g^{(n)}(E)$, was obtained using the incoherent approximation [25, 26]. This method has been used previously to investigate phonon dynamics and anomalous thermal expansion in a number of transition-metal cyanides [9, 11, 13, 47, 27]. In the incoherent, one-phonon approximation, $g^{(n)}(E)$ is related to the measured scattering function $S(Q, E)$ from INS by,

$$g^{(n)}(E) = A \left\langle \frac{e^{2W(Q)}}{Q^2} \frac{E}{n(E, T) + \frac{1}{2} \pm \frac{1}{2}} S(Q, E) \right\rangle \quad (1)$$

where A is a normalisation constant, $2W(Q)$ is the Debye-Waller factor and $n(E, T)$ is the thermal occupation factor equal to $[\exp(E/k_B T) - 1]^{-1}$. The + or - signs correspond to neutron energy loss or gain respectively and the bra-kets indicate an average over the whole Q -range [28].

III. Computational Details

Projector-augmented wave potentials (PAW) [29, 30] calculations were carried out using the Vienna *ab initio* simulation package (VASP) [31, 32, 33, 34]. The generalised gradient approximation (GGA) was adopted within the Perdew-Burke-Ernzerhof (PBE) scheme [35, 36]. An energy cut-off of 700 eV was set and Gaussian broadening implemented with a smearing width of 0.01 eV.

The tetragonal crystal structure (Figure 1) published by Yuan *et al.* [14] was used as an input structural model for the *ab initio* calculations. Total structural relaxation, followed by constant volume relaxation at seven different volumes close to equilibrium, was performed using a $5 \times 5 \times 2$ k -point mesh generated using the Monkhorst-Pack method [37].

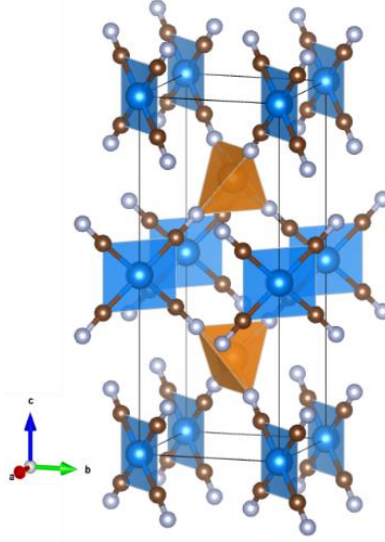


Figure 1: Structural model of $\text{ZnNi}(\text{CN})_4$ (showing the square-planar $\text{Ni}(\text{CN})_4$ and tetrahedral $\text{Zn}(\text{NC})_4$ units), which was used for *ab initio* calculations [14]. Key: Ni, blue, Zn, orange, C, brown, N, light blue.

The results of total energy calculations at varying volumes were fitted to a Birch-Murnaghan equation of state to establish the bulk modulus, B_0 , and its pressure derivative, B_0' , defined as,

$$B_0 = -\left(\frac{\partial \ln V}{\partial P}\right)_{T,P=0}^{-1} \quad B_0' = -\left(\frac{\partial B}{\partial P}\right)_{T,P=0}^{-1} \quad (2)$$

For comparison, bulk modulus calculations were also carried out for the parent compounds, $\text{Zn}(\text{CN})_2$ and $\text{Ni}(\text{CN})_2$, using the crystal structures published in [5] and [4], respectively. Due to the layered nature of $\text{Ni}(\text{CN})_2$, the vdW-DF2 functional [38, 39, 40, 41] was used to account for possible van der Waals' interactions between neighbouring layers.

Phonon calculations using the direct method [42] were performed for each volume on a $2 \times 2 \times 2$ supercell with a $2 \times 2 \times 1$ k -point mesh. The calculated partial vibrational density-of-states (PDOS) of the k^{th} atom contributes to the measurable GDOS via,

$$g^{(n)}(E) = B \sum_k \left(\frac{4\pi b_k^2}{m_k}\right) g_k(E) \quad (3)$$

where B is a normalisation constant, b_k is the neutron scattering length and m_k the mass of the k^{th} atom [28]. The constant $(4\pi b_k^2 / m_k)$ represents the neutron weighting factor of the k^{th} atom with values: Ni, 0.3152, Zn, 0.0632, C, 0.4622, N, 0.8216 barns amu^{-1} [43]. The mean square displacement (MSD) of the k^{th} atom in the \hat{x} direction at temperature, T , is related to the PDOS projected along \hat{x} as follows,

$$\langle |u_k^x|^2 \rangle = \int \frac{\hbar}{m_k \omega} \left(\frac{1}{2} + n(\omega, T)\right) g_k^x(\omega) d\omega \quad (4)$$

The integrand in equation (4) represents the contribution of modes with energy $\hbar\omega$ to the MSD.

Thermal expansion stems for anharmonic phonon modes, whose frequencies changes with temperature [2]. The expansion is negative when the sum over all mode Grüneisen parameters, defined as $\gamma_i = -(d\ln\omega_i/d\ln V)$, is also negative [44]. The total anharmonicity can be split into two terms as follows,

$$\begin{aligned} \left(\frac{\partial\omega_i}{\partial T}\right)_P &= \left(\frac{\partial\omega_i}{\partial T}\right)_V + \left(\frac{\partial\omega_i}{\partial V}\right)_T \left(\frac{\partial\omega_i}{\partial T}\right)_P \quad (5) \\ &= \left(\frac{\partial\omega_i}{\partial T}\right)_V - \alpha\omega_i\gamma_i^T \quad (6) \end{aligned}$$

where ω_i is the mode frequency, α is the volume expansion coefficient and γ_i^T is the isothermal Grüneisen parameter [45]. The first term, where the frequency is changing with temperature at constant volume, is the explicit anharmonicity sometimes referred to as the true anharmonicity. The second term is the implicit anharmonicity and is due to volume effects.

The quasi-harmonic approximation (QHA), where phonon calculations at different volumes are used to mimic a temperature effect [2], was used to calculate the thermal expansion coefficient and mode Grüneisen parameters. Equation 5 and 6 can be rearranged as follows,

$$\gamma_i^P = \gamma_i^T - \frac{1}{\alpha\omega_i} \left(\frac{\partial\omega_i}{\partial T}\right)_V \quad (7)$$

where γ_i^P is the isobaric Grüneisen parameter. In the QHA, γ_i^T is equal to γ_i^P as the explicit anharmonic effects are ignored [45]. The QHA is valid for low temperatures [46] and has frequently been used to compute accurate negative thermal expansion coefficients using calculated Grüneisen parameters [9, 11, 13, 47, 48, 49, 50, 51, 52, 53]. However, there are limitations to the method when explicit anharmonicity is dominant [54, 55]. It is worth noting that throughout this paper, calculated Grüneisen parameters are, in fact, isothermal Grüneisen parameters. The phonon density-of-states, mode frequencies and Grüneisen parameters were determined using the Phonopy software [56].

IV. Results and Discussion

1. Structure

A single crystal of the doubly-interpenetrating $\text{ZnNi}(\text{CN})_4$ structure was synthesised by Yuan *et al.* via slow diffusion of $\text{Zn}(\text{SO}_4)$ and $\text{K}_2[\text{Ni}(\text{CN})_4]$ in a mixture of ethanol and water [14]. A second crystal structure consisting of a single $\text{ZnNi}(\text{CN})_4$ framework was later synthesised by a similar method [15]. It was noted for both structures that, when removed from the mother liquor, the crystals disintegrated to a powder [14, 15]. In the case of the single network structure, this is likely to be due to loss of occluded solvent molecules. It is unclear as to why crystals of the double framework should pulverise upon removal from the solvent, but it correlates with our observation that powder samples of the doubly interpenetrating form are poorly crystalline, as

shown by the XRD pattern (Figure 2). INS measurements were of necessity carried out on a large, solvent-free, and therefore poorly crystalline sample of $\text{ZnNi}(\text{CN})_4$.

The sample density measured at room temperature was 2.0539 g cm^{-3} , comparable to that obtained for the double interpenetrating framework (2.106 g cm^{-3}) [14], and almost double the density calculated for the single-framework material (1.047 g cm^{-3}) [15]. The peak positions in the powder XRD pattern match those of the doubly-interpenetrating structure. However, the broad peaks renders measurement of thermal expansion coefficients impossible by refinement of unit-cell parameters at varying temperature.

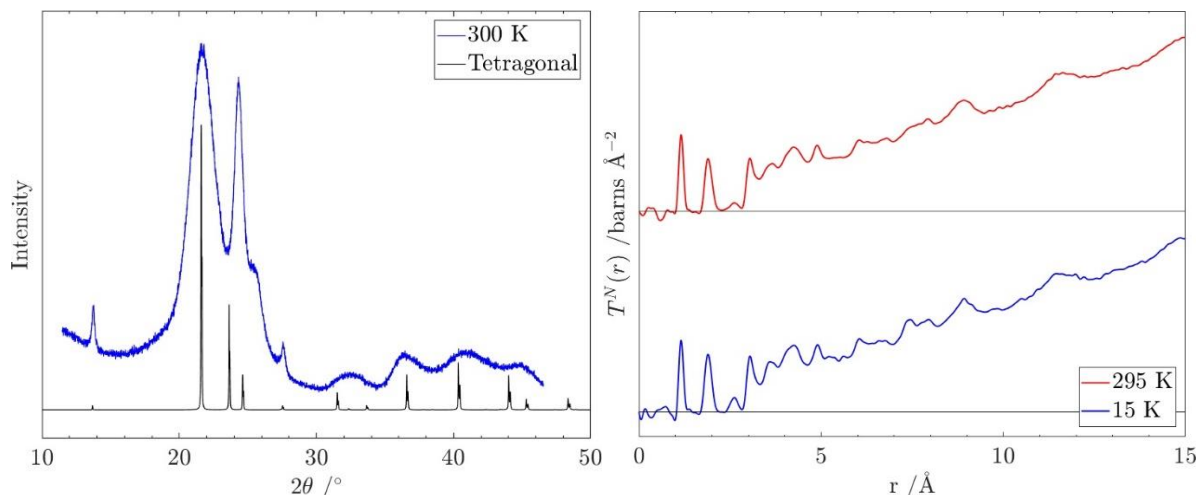


Figure 2: Left: Comparison of the measured X-ray powder diffraction pattern (blue) with a theoretical pattern calculated from the tetragonal double interpenetrating structure [14]. Right: The total correlation function of $\text{ZnNi}(\text{CN})_4$ at 15 and 295 K obtained from Fourier transformation of the $Q_i(Q)$ measured by total neutron diffraction.

Structural relaxation of the room-temperature crystal structure obtained by Yuan *et al.* [14] converged easily. In the relaxed structure, there was a slight deviation from linearity of the Zn-NC-Ni linkage, with the sum of the individual bond lengths being 0.02 Å larger than the Zn...Ni distance. Such a deviation reduces the decreasing effect any transverse motion of the ligand would have on the unit-cell parameters. Nevertheless, the unit-cell volume after the DFT-based structural relaxation (at 0 K) increased by 6 Å^3 , with an increase in the a parameter and slight decrease in the c parameter (Table 1).

The single-crystal X-ray diffraction study by Yuan *et al.* [14] reported that the cyanide ligand bonds to Ni exclusively through C rather than N [9]. This orientation was confirmed by the neutron PDF analysis. Total energy calculations of the relaxed and unrelaxed crystal structure were carried out and then repeated with the CN ligand flipped. In both cases, an energy difference of $\sim 3 \text{ eV}$ between the two configurations was found, providing further confirmation of the original atom assignment and the formation of Ni-C \equiv N-Zn linkages.

The bond lengths resulting from analysis of the neutron correlation function, $T_N(r)$, are listed in Table 1, together with those from [14] and those resulting from our structural relaxation. There is a significant discrepancy between the bond-length values from [14] and those extracted from the $T_N(r)$, the former being unusual and possibly incorrect. The bond lengths derived from our

theoretical model are much closer to the values from the total neutron diffraction study and correctly identify the Ni-C bond as the shorter of the two single bonds.

Table 1: Bond lengths extracted from the total neutron diffraction data (*n*-PDF), together with those from the crystal structure of Yuan *et al.* [14] and those from the relaxed computational model. For the latter two the unit-cell parameters are also listed. The relaxed structural model correctly identifies that the Zn-N bond is longer than the Ni-C bond.

Bond Length / Å	<i>n</i> -PDF 295 K	<i>n</i> -PDF 15 K	Yuan Structure 300 K [14]	Relaxed Structure 0 K
C≡N	1.159(1)	1.153(1)	1.128	1.169
Ni-C	1.870(5)	1.857(3)	1.921	1.835
Zn-N	1.980(6)	1.970(4)	1.892	1.968
Unit-cell parameter <i>a</i> / Å				5.2629(15)
Unit-cell parameter <i>c</i> / Å				5.32
				12.95

The bulk modulus, B_0 and its pressure derivative, B_0' , were calculated for $\text{ZnNi}(\text{CN})_4$ and its parent compounds, $\text{Zn}(\text{CN})_2$ and $\text{Ni}(\text{CN})_2$. The results together with other values from the literature are listed in Table 2.

Table 2: Values of the bulk modulus, B_0 , and its pressure derivative, B_0' , for $\text{ZnNi}(\text{CN})_4$ and its parent compounds, $\text{Ni}(\text{CN})_2$ and $\text{Zn}(\text{CN})_2$. A comparison is given of DFT calculations carried out in this study with those from previous studies and experimentally acquired data at 300 K. The larger values for B_0 and B_0' from the DFT calculations compared to those experimentally derived is expected, due to the temperature-dependence of these properties [57].

	This work			Previous Calculations		Experimental 300 K	
	$\text{Ni}(\text{CN})_2$	$\text{Zn}(\text{CN})_2$	$\text{ZnNi}(\text{CN})_4$	$\text{Ni}(\text{CN})_2$	$\text{Zn}(\text{CN})_2$	$\text{Ni}(\text{CN})_2$	$\text{Zn}(\text{CN})_2$
Bulk Modulus, B_0 / GPa	18.4	44.9	41.8	63.4 [9]	84.1 [9], 59 [45], 46.4 [57], 45.0 [58]	12.4 [59]	34.2 [60], 33.4 [57], 25±11 [61]
Bulk Modulus Derivative, B_0'	9.2	4.6	-2.5		7.2 [57]	4 [59]	-4.2 [57]

A study by Fang *et al.* of the temperature dependence of the bulk properties of $\text{Zn}(\text{CN})_2$ reported measurements of B_0 and B_0' between 30 and 300 K [57]. These revealed that B_0 increased with decreasing temperature by 5.77 GPa over the investigated temperature range. However B_0' decreased from -4 at 300 K to -9 at 250 K and then increased slowly, reaching -2 at 30 K. This behaviour was then reproduced by the authors using molecular-dynamics simulations. The temperature dependence accounts for the difference between the values from our DFT calculations (0 K) and the experimentally measured values (300 K) in Table 2.

Our values of B_0 and B_0' for $\text{Ni}(\text{CN})_2$ are also slightly higher than the experimental values, and this is also likely to arise from temperature dependence. Our value for B_0 is much closer to the experimental value than that from a previous study in which calculations were performed only on a single layer of $\text{Ni}(\text{CN})_2$ which did not take into account inter-layer interactions [9].

The calculated value of B_0 for $\text{ZnNi}(\text{CN})_4$ is much closer to that of $\text{Zn}(\text{CN})_2$ than that of $\text{Ni}(\text{CN})_2$. This is not unexpected as the structures of $\text{ZnNi}(\text{CN})_4$ and $\text{Zn}(\text{CN})_2$ both contain two interpenetrating 3-D frameworks, in contrast to the layered structure of $\text{Ni}(\text{CN})_2$. The calculated value of B_0' for $\text{ZnNi}(\text{CN})_4$ is lower than that of both parent compounds. Furthermore, the value is negative meaning that, even close to 0 K, the compound undergoes anomalous softening of the elastic modulus.

2. Dynamics

The measured GDOS [23] of $\text{ZnNi}(\text{CN})_4$, at 200, 300 and 400 K, are shown in Figure 3. The spectra contain several well-pronounced vibration bands, whose energies do not exhibit any detectable temperature dependence in terms of frequency shifts. A low-energy shoulder observed around 6.5 meV decreases in intensity with temperature. It is located between the lowest-energy bands seen in the phonon spectra of $\text{Zn}(\text{CN})_2$ and $\text{Ni}(\text{CN})_2$, at 4 meV and 10 meV, respectively [9]. A large band between 7.5 and 20.0 meV contains several small features. The instrumental resolution does not allow their positions to be accurately determined. Other prominent bands are at 24, 41, 58 and 68 meV, along with two smaller bands at 32 and 51 meV. The latter are most clearly observed at 200 K due to the reduced Debye-Waller broadening at lower temperature. This justifies the use of the spectrum acquired at 200K to compare hereafter with the calculation $\text{ZnNi}(\text{CN})_4$. Figure 4 shows the calculated GDOS for $\text{ZnNi}(\text{CN})_4$ which reproduced the measured GDOS well, in terms of both peak positions and intensities. This good agreement provides a further validation of the use of the ordered tetragonal model for lattice dynamical studies.

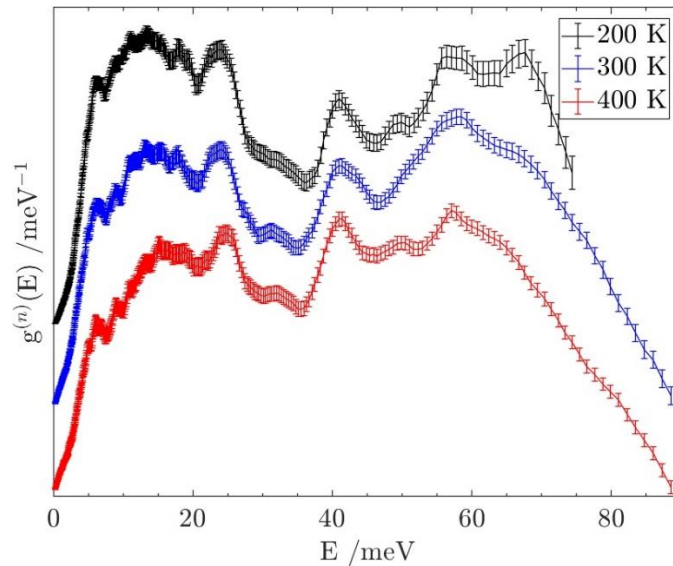


Figure 3: The generalised phonon density-of-states (GDOS) [23] of $\text{ZnNi}(\text{CN})_4$ at 200, 300 and 400 K. Measurements were carried out with an incident wavelength of 4.14 Å on the IN6 spectrometer at the ILL. The spectra are vertically shifted with respect to each other to aid comparison.

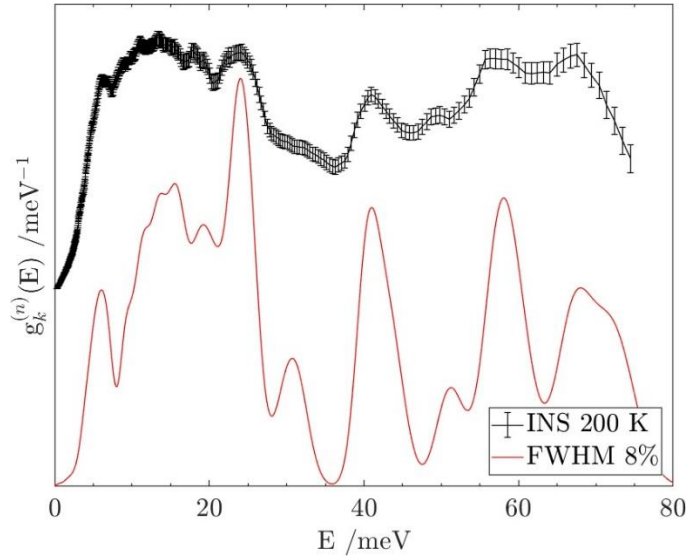


Figure 4: Comparison between the calculated and experimental phonon spectra of ZnNi(CN)_4 . The calculated spectrum has been convoluted with a Gaussian of a FWHM of 8% of the energy transfer to describe the effect of the experimental energy resolution.

The calculated, neutron-weighted, partial vibrational density-of-states (PDOS) of each atomic species projected along the x (y) and z directions contributing to the total, are shown in Figure 5. The calculated C≡N stretching modes lie between 270 and 280 meV (2170 - 2260 cm^{-1}), which are in the same region of the stretching frequencies as found in the IR for Zn(CN)_2 (2218 cm^{-1}) and Ni(CN)_2 (2202, 2215 cm^{-1}) [9]. The figure shows that dynamics involving Ni atoms moving primarily in the xy plane contribute the most to the low-energy feature seen in the GDOS at around 7 meV. In addition, it reveals that Zn moves very little even compared to Ni, indicating it is well anchored within the structure.

Below 40 meV, N contributes more to the total density-of-states than C. This observation can be interpreted as a greater freedom of movement around the tetrahedrally-coordinated Zn. Above 40 meV, the peaks are sharp and well defined indicating that these vibrations are localised and hence will resemble the vibrations of isolated tetrahedral and square-planar units. As the symmetry of the unit cell is the same as that of the $[\text{NiC}_4]$ unit, all the motions of a structural unit with D_{4h} symmetry are possible (A_{2u} , B_{1g} , B_{2g} and E_u), however only the E vibration of the tetrahedral unit will be present, as the T_2 vibration will be lost due to the lack of three-fold symmetry. This would explain the larger contribution of C than N in this region. The peaks at 68 and 72 meV are from stretches of the Zn-N and Ni-C single bonds. The higher-energy of the two involves strong movement of the Ni and hence corresponds to the asymmetric stretch characterised by the irreducible representation, E_u , within the D_{4h} local symmetry. The peaks between 50 and 65 meV are likely to arise from localised deformations of the units. The similarity of the C and N peak profiles between 40 and 50 meV, along with the almost stationary state of the metals, indicate a symmetry between the motions of the different units, which could correspond to rotational RUMs.

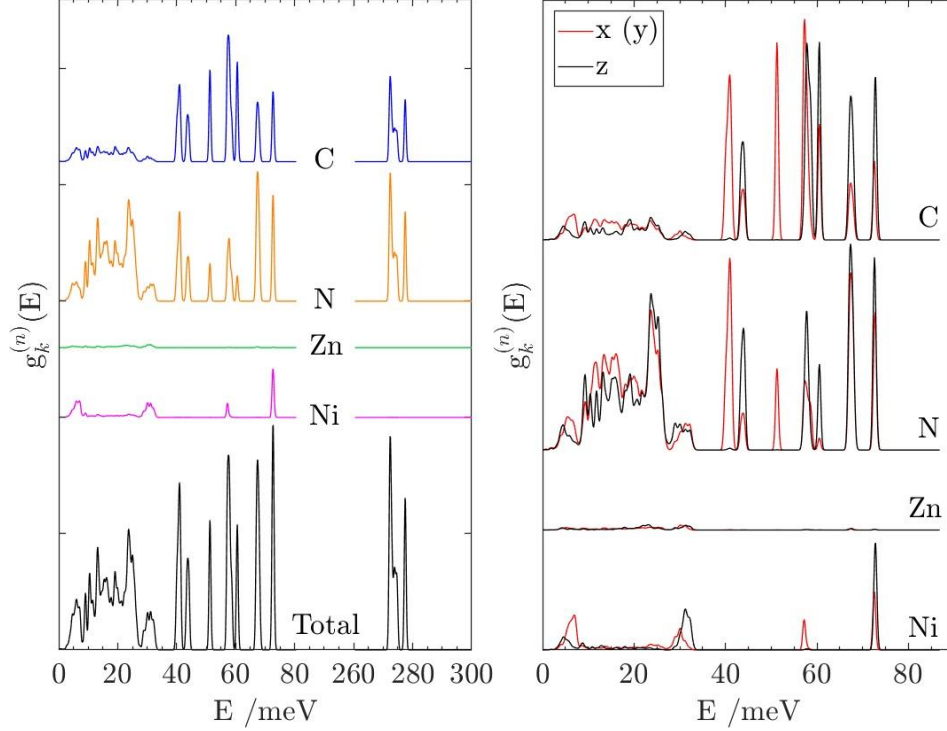


Figure 5: Left: The calculated PDOS for each atom in $\text{ZnNi}(\text{CN})_4$. N contributes the most below 30 meV, however C and Ni are dominant in the lowest-energy phonon band at 7 meV. Right: The calculated PDOS for each atom projected onto the x (y) and z axes. The CN stretching modes are omitted for clarity in the right panel.

The measured and calculated IR and Raman frequencies are listed in **Error! Reference source not found.**. There are 42 optic modes, of which 15 are doubly degenerate. The structure belongs to the $4/mmm$ Laue class (D_{4h} point group) and therefore the principle of mutual exclusion applies. This results in 13 IR and 13 Raman frequencies along with 16 silent modes; $\Gamma_{\text{optic}} = 4A_{1g} + 2A_{1u} + 2A_{2g} + 5A_{2u} + 2B_{1g} + 5B_{1u} + 5B_{2g} + 2B_{2u} + 7E_g + 8E_u$.

Table 3: Measured and calculated vibrational frequencies (cm^{-1}) from IR and Raman data

Γ	IR active (13)		Raman active (13)			Silent (16)				
	$5A_{2u}$	$8E_u$	$4A_{1g}$	$2B_{1g}$	$7E_g$	$2A_{1u}$	$2A_{2g}$	$5B_{1u}$	$5B_{2g}$	$2B_{2u}$
Calculated	197	56	202	154	73	186	98	145	176	125
	266	138	490	335	109	416	321	241	221	412
	458	199	548		178			472	490	
	588	240	2239		327			590	547	
	2197	460			349			2214	2237	
		465			541					
		584			2206					
		2194								
Measured	573, 2190		152, 172, 207, 324, 2197, 2214							

Having established that phonon calculations at equilibrium volume reproduced our measurements well, further calculations at varying volume were undertaken to extract mode Grüneisen parameters along with thermal properties of the ordered structure under the QHA. The calculated linear thermal expansion coefficients are $\alpha_a = -21.2 \times 10^{-6} \text{ K}^{-1}$ and $\alpha_c = +14.6 \times 10^{-6} \text{ K}^{-1}$, leading to an overall volume expansion coefficient of $\alpha_V = -26.95 \times 10^{-6} \text{ K}^{-1}$ between 200 and 400 K. This value of α_V is approximately half that measured and calculated for $\text{Zn}(\text{CN})_2$ and in contrast to the overall positive volume expansion observed for $\text{Ni}(\text{CN})_2$. However, the calculated value of α_a is more negative than the values determined for both $\text{Zn}(\text{CN})_2$ and $\text{Ni}(\text{CN})_2$ [9].

The variation of the volume thermal expansion coefficient with temperature and the contribution of phonon modes of energy E to the expansion are presented in Figures 6 and 7, respectively. The expansion coefficient decreases with temperature from 0 K, reaching its most negative value slightly below 200 K. This value remains constant up to 400 K, above which it increases slowly. The change occurring in the first 200 K is the result of increasing contribution from phonon modes at 40 meV with temperature. This behaviour is similar to that calculated for $\text{Zn}(\text{CN})_2$ - where optic modes at 40 meV, which are pure rotational RUMs, provide a large contribution to the NTE [10].

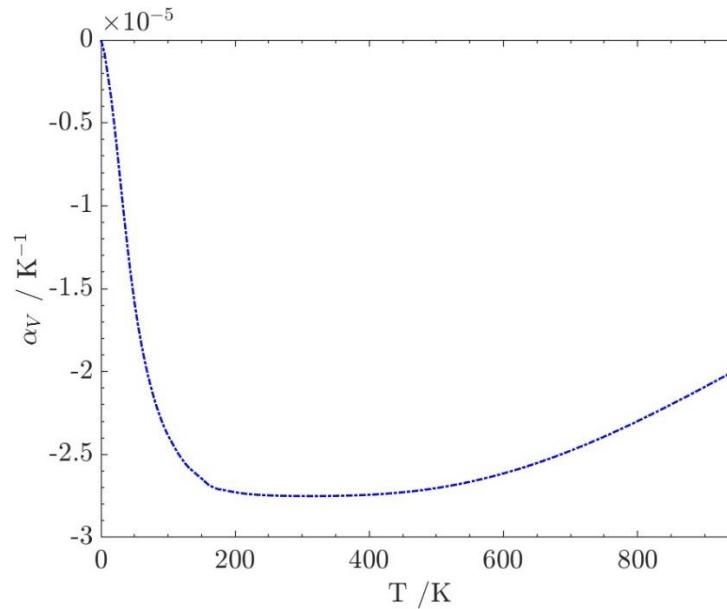


Figure 6: Volume thermal expansion coefficient, α_V , vs temperature in $\text{ZnNi}(\text{CN})_4$, calculated using the QHA.

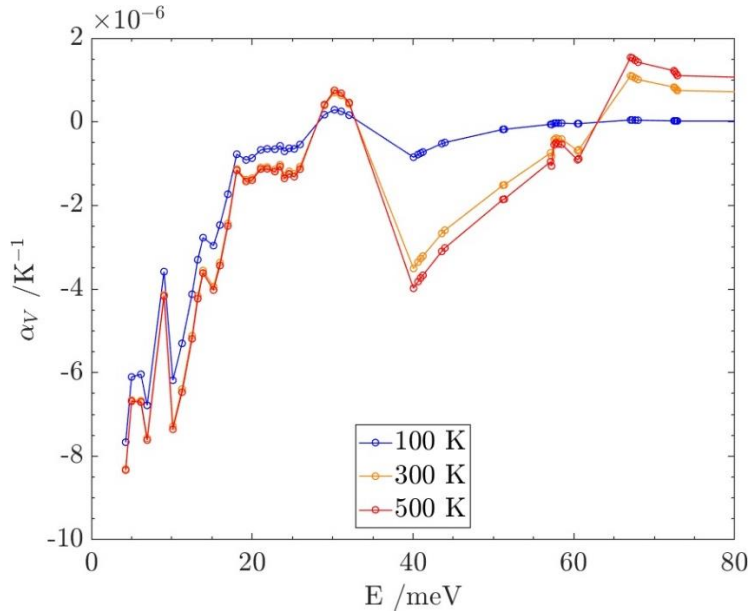


Figure 7: Contribution of modes of energy E to the thermal expansion in $\text{ZnNi}(\text{CN})_4$.

The calculated thermal ellipsoids at 300 K are shown in Figure 8. The Ni and C atoms move predominantly in the direction perpendicular to their square-planar environment, whereas the N atoms move isotropically around the bond and Zn moves very little. The MSD of each atom with temperature is shown in Figure 9. The figure also shows the contribution to the MSD with energy for each atom at 300 K, as well as the contribution projected in the x (y) and z directions averaged over all atoms.. It is clear that N has a higher amplitude of motion than C, as a result of contributions from modes between 10 and 20 meV. Similarly, the amplitude of motion of Ni is larger compared to Zn. At 7 meV, Ni even has a larger MSD than both light atoms. The motion of Ni at this energy will be in the xy plane, perpendicular to the square-planar geometry as seen in Figure 8.

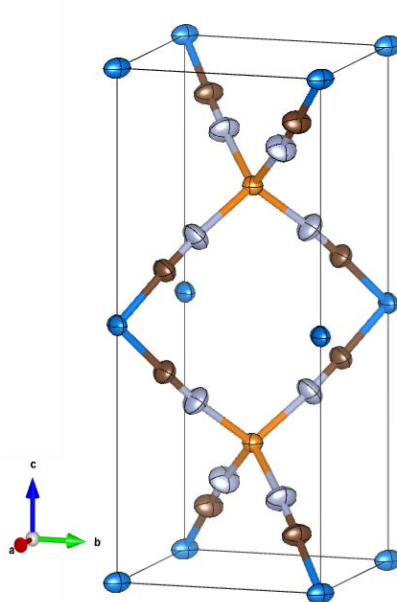


Figure 8: Relaxed structure of $\text{ZnNi}(\text{CN})_4$ with calculated thermal ellipsoids at 300K representing a 75% probability of containing the atom. The Ni atom has a large oblate spheroid indicating it moves predominantly perpendicular to its square-planar environment. In contrast, the comparatively small and perfectly spherical thermal ellipsoid of Zn indicates it moves very little. The ellipsoid for N is isotropic perpendicular to the bond compared to that of C, which has an oblate shape more similar to that of Ni.

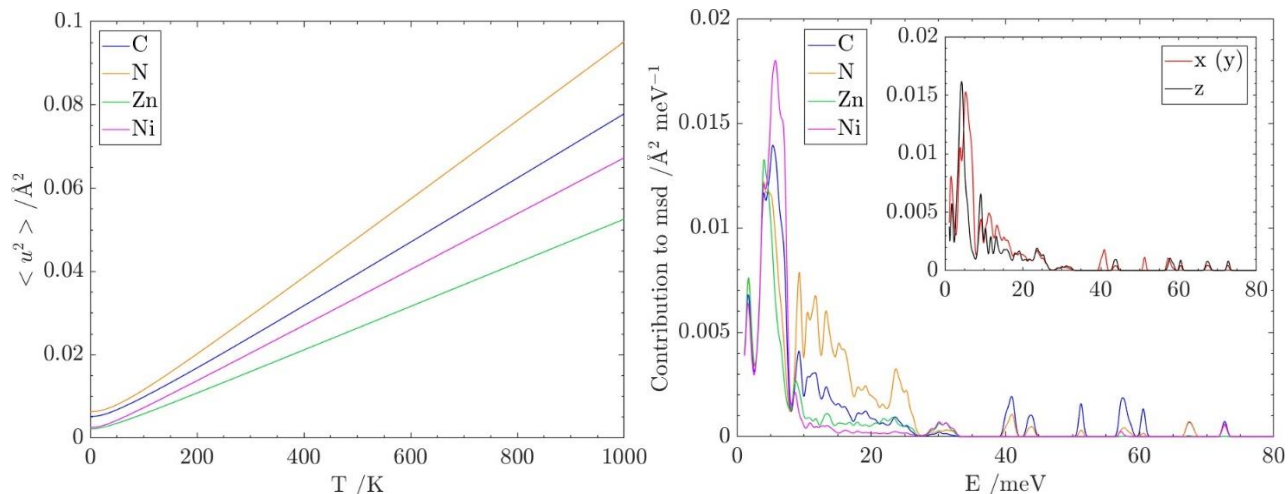


Figure 9: MSD with temperature for each atom type in $\text{ZnNi}(\text{CN})_4$ (left). This represents the average of a single atom in the unit cell. The integrand of equation 3 representing the contribution to the MSD at 300 K of phonon modes with energy, E , for each atom type (centre) and averaged over all atoms projected along the x (y) and z axes (right). Low-energy modes contribute the most to the MSDs. N has the largest amplitude of motion as a function of temperature arising from modes between 10 and 20 meV, as a result of greater freedom of movement around the Zn. Ni has a larger MSD than Zn, dominated by modes around 7 meV. At this energy, Ni has a larger amplitude of motion than even C and N. (see Figure 14).

The mode Grüneisen parameters for each phonon at q -points from a $40 \times 40 \times 20$ k -point mesh are shown in Figure 10. The range in value over the Brillouin zone decreases rapidly with energy as the modes become more localised.

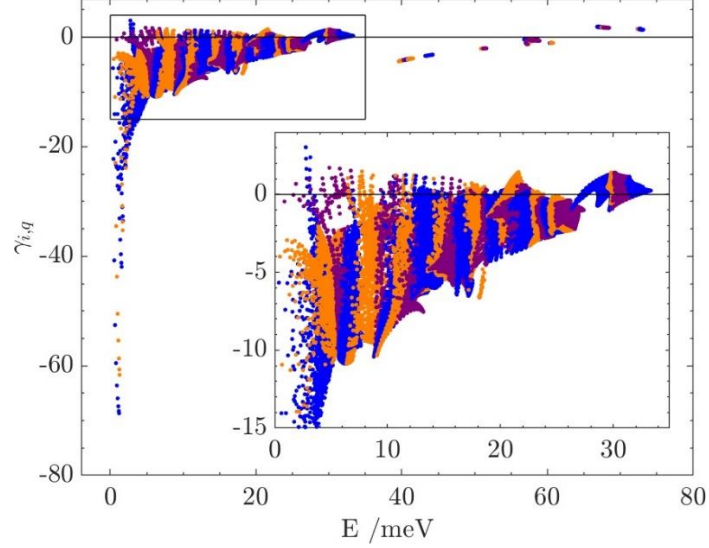


Figure 10: The calculated mode Grüneisen parameters, γ_i , at q -points from a $40 \times 40 \times 20$ k -point mesh over the whole Brillouin zone. A colour-coded illustration for neighbouring modes is used for contrast. The most negative Grüneisen parameters can be seen in the low-energy region, corresponding to the acoustic modes.

For all the high symmetry points in the Brillouin zone, there are phonon modes with negative Grüneisen parameters of ~ -9 (Table 4). However, the lowest-energy acoustic mode at the zone boundary in the Z ($0\ 0\ \frac{1}{2}$) direction has a very pronounced mode-Grüneisen-parameter value of -79.40. The eigenvectors for this mode describe an almost rigid transverse motion of both $[\text{Zn}(\text{NC})_4]$ tetrahedra in the unit cell, resulting in a transverse motion and slight twisting of the $[\text{Ni}(\text{CN})_4]$ units. The real displacement vectors for this mode are depicted in Figure 11.

Table 4: The frequencies and corresponding mode Grüneisen parameters for the two modes with the most negative Grüneisen parameter along the high symmetry point in the Brillouin zone (crystallographic point group $P4_2/mcm$). The asterisk denotes acoustic modes.

Zone Boundary	ω_i /meV	γ_i
Γ (0 0 0)	6.91, 9.06	-10.67, -9.62
Z (0 0 $\frac{1}{2}$)	1.12*, 5.71	-79.40, -10.57
R (0 $\frac{1}{2}$ $\frac{1}{2}$)	5.09*, 5.91*	-10.85, -7.71
X (0 $\frac{1}{2}$ 0)	5.91*, 6.04*	-9.46, -9.28
M ($\frac{1}{2}$ $\frac{1}{2}$ 0)	7.65*, 8.77	-7.92, -10.45
A ($\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$)	7.07*, 9.56	-9.03, -7.54

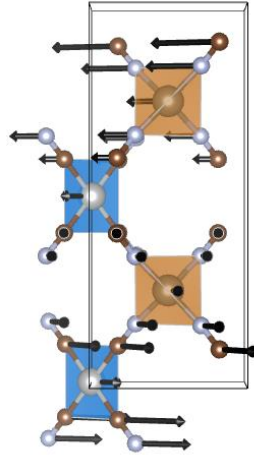


Figure 11: Schematic illustration of zone-boundary acoustic phonon mode with energy 1.12 meV, along Z (0, 0, 1/2), with the highest mode Grüneisen parameter of -79.40. The vectors represent the real displacement, however their amplitude has been exaggerated.

The calculated dispersion curves for the ordered ZnNi(CN)₄ model are presented in Figure 12 in two ways. The left-hand figure corresponds to the full dispersion relations. In the right-hand figure, a filter is applied according to the mode Grüneisen parameters highlighting which modes contribute the most to NTE.

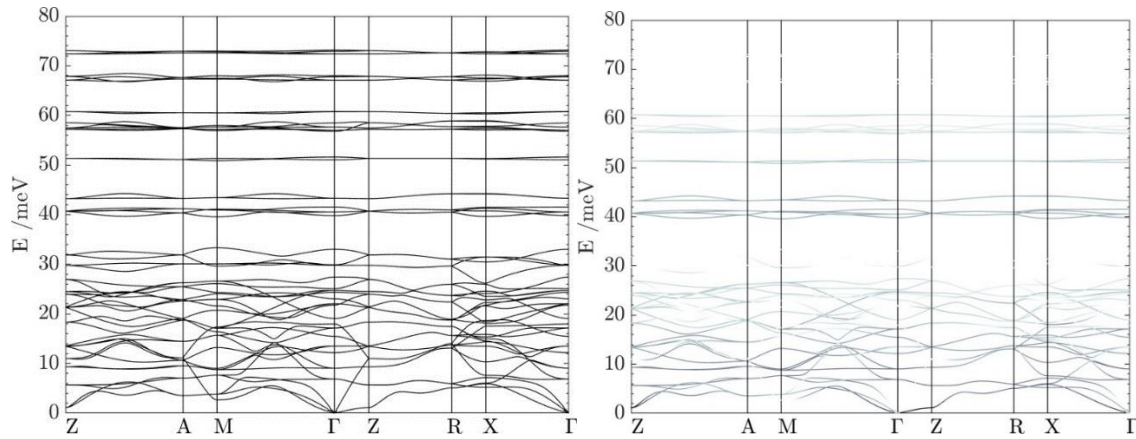


Figure 12: Left: The calculated phonon dispersion curves for ZnNi(CN)₄ along the indicated high-symmetry points (the CN stretching modes at ~280 meV are not shown). Right: The dispersion curves with grayscale colour coding according to values of the mode Grüneisen parameters. Black indicates the most negative value, whereas white represents a value ≥ 0 . The more visible the dispersion curve the more it contributes to NTE in ZnNi(CN)₄.

Figure 7, Figure 10 and Figure 12, all show that the bulk of the NTE comes from optic modes below 20 meV and around 40 meV. Analysis of mode eigenvectors reveal that the optic modes below 20 meV involve rotations and deformations where the angle between the displacement of the C and N atom is less than 90°, whereas the modes between 40 and 60 meV involve rotations and deformations where this angle is greater than 90°. Zone-centre modes that involve a perfect rotation of a unit are shown in Figure 13. A view along the *c*-axis clearly shows how the transverse or rotational motion of the CN ligand results in a decrease in the *a* lattice parameter. The modes at 12.20 and 39.81 meV represent perfect RUMs. In the former (12.20 meV),

neighbouring tetrahedral and square-planar units rotate towards one another, and in the latter (38.81 meV), they rotate in phase away from one another. The other four modes shown represent a RUM for one unit inducing a deformation in neighbouring units. Away from the zone centre, the motions described occur with different relative phases.

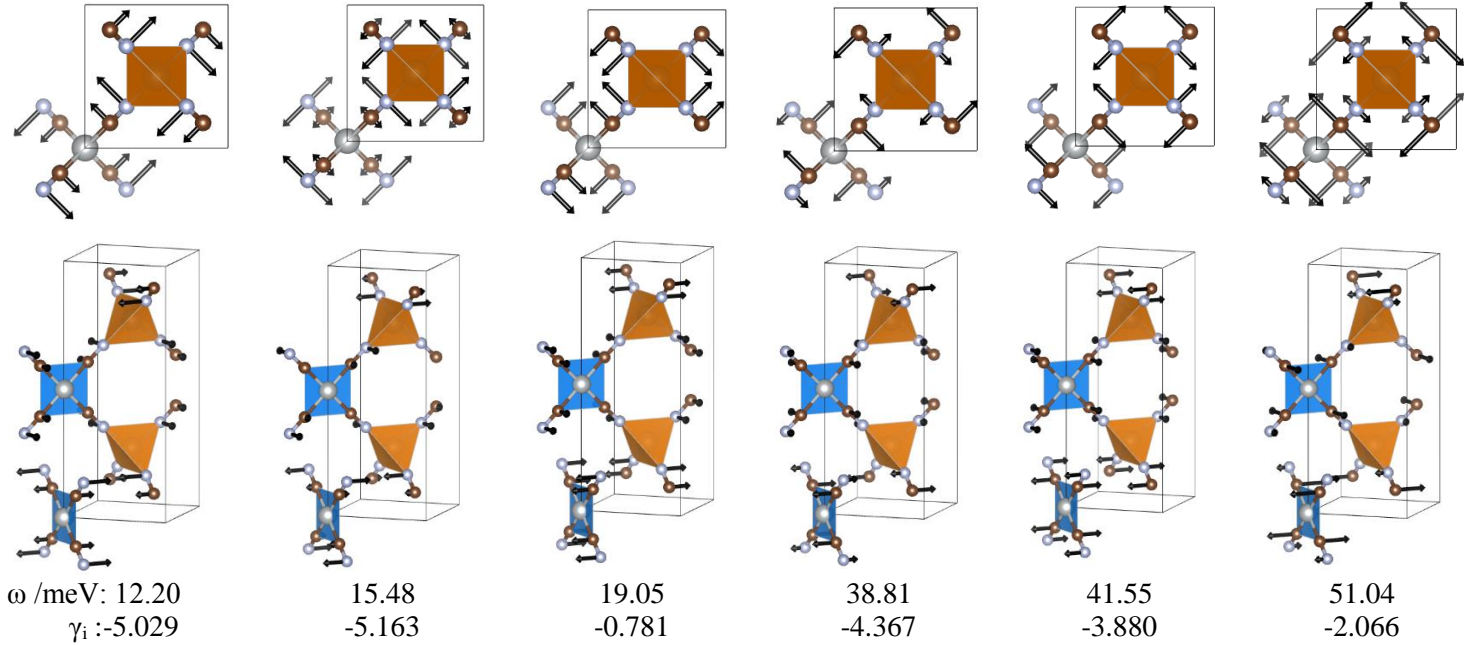


Figure 13 : Schematic illustrations of zone centre phonon modes viewed along the c -axis (top) and from the side (bottom) demonstrating how their motions shrink the ab plane,. The arrows represent the real displacement vectors of the atoms. Below each mode is the corresponding frequency and mode Grüneisen parameter. The first and fourth modes are perfect rotational RUMs. The second and sixth are RUMs for the tetrahedral units and distortions of the square planar units, whereas the third and fifth are RUMs for the square planar units and distortions of the tetrahedra.

Although the rotational RUM modes described do make an important contribution to the NTE, they are not the optic modes that contribute the most. The lowest-energy optic mode, shown at the zone centre in Figure 14, involves an undulation of the framework that is not present in $\text{Zn}(\text{CN})_2$. Due to the 2-D nature of the square-planar units, they can act as flexible connectors between two Zn metals, almost like a giant ligand. Hence, their transverse motion will also bring the neighbouring Zn ions closer together. This motion is neither a RUM for the $[\text{NiC}_4]$ or $[\text{ZnN}_4]$ units, nor for the larger tetrahedral $[\text{Zn}(\text{NCNi})_4]$ unit. This is an example of the *tension effect*, but not of a RUM.

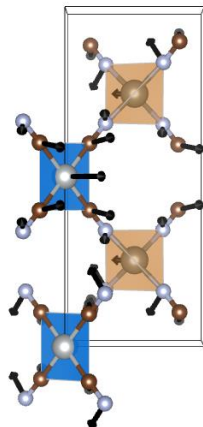


Figure 14: The lowest energy optic mode at the zone centre, which has a frequency of 6.9 meV and Grüneisen parameter of -10.67. This mode is the optic mode that contributes the most to the NTE, but it is not a RUM. The motion is possible due to the square-planar coordination of the Ni making it only constrained in two dimensions. (The lower Ni atom is moving into the plane page.)

V. Conclusion

A polycrystalline sample of $\text{ZnNi}(\text{CN})_4$ was synthesized using a precipitation method. Powder X-ray diffraction, density measurements, IR and Raman spectroscopy, and the experimentally determined atomic correlation function showed that the double interpenetrating framework structure was formed. The X-ray diffractogram contains broad peaks indicating poor crystallinity. Total energy calculations using a tetragonal model derived from published single-crystal study [14] confirm that the Zn atoms bond exclusively to the carbon end of the cyanide ligand. Bond lengths were extracted from the total atomic correlation function obtained using neutron scattering. The values obtained show those previously reported [14] are in error. Relaxation of the structure by *ab initio* methods yielded bond lengths matching those from the neutron diffraction data.

Inelastic neutron scattering was used to study the dynamics of $\text{ZnNi}(\text{CN})_4$. *Ab initio* calculations under the QHA using a tetragonal model reproduced the measured phonon spectra well, validating its use for dynamical predictions of the crystalline structure. DFT calculation at 0 K of the bulk modulus yields a similar value to that of $\text{Zn}(\text{CN})_2$, however its pressure derivative is negative. This possibly points towards a pronounced flexibility of the ordered structure, which could contribute to the broad nature of the X-ray diffraction peaks. Calculated thermal expansion coefficients predict 2-D NTE with overall volume NTE in crystalline $\text{ZnNi}(\text{CN})_4$. Analysis of the mode eigenvectors and Grüneisen parameters show that although low-energy phonons with RUM-like character do contribute to the NTE, twisted transverse motions, which are not present in $\text{Zn}(\text{CN})_2$, play a more significant role. The motions are the result of the lower constraint on the Ni atom due to its 2-D coordination geometry within a 3-D framework.

The results in this work provide further evidence that framework structures containing corner-sharing geometries are likely to contain low-energy phonon modes capable of inducing NTE. When designing a new compound capable of exhibiting anomalous thermal properties, low

structural constraints are effective, however they may have unforeseen effects on the crystallinity of the material.

Acknowledgments

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