

The future of sea ice modelling: where do we go from here?

Article

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The future of sea ice modelling: where do we go from here?



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- PURITY
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Towards defining a cutting-edge future for sea ice modelling: An international
workshop
What: An international workshop for sea ice model developers and expert users to discuss the
future of sea ice modelling
When : 23-26 September 2019
Where: Laugarvatn, Iceland
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1. Introduction and motivation for the workshop

46 Earth System Models (ESMs) include a sea ice component to physically represent sea ice changes and impacts on planetary albedo and ocean circulation (Manabe & Stouffer, 1980). 47 48 Most contemporary sea ice models describe the sea ice pack as a continuum material, a principle 49 laid by the AIDJEX (Arctic Ice Dynamics Joint EXperiment) group in the 1970s (Pritchard, 50 1980). Initially intended for climate studies, the sea ice components in ESMs are now used 51 across a wide range of resolutions, including very high resolutions more than 100 times finer 52 than those they were designed for, in an increasingly wide range of applications that challenge 53 the AIDJEX model foundations (Coon et al., 2007), including operational weather and marine 54 forecasts. It is therefore sensible to question the applicability of contemporary sea ice models to these applications. Are there better alternatives available? Large advances in high 55 56 performance computing (HPC) have been made over the last few decades and this trend will 57 continue. What constraints and opportunities will these HPC changes provide for contemporary 58 sea ice models? Can continuum models scale well for use in exascale computing?

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To address these important questions, members of the sea ice modelling community met in September 2019 for a workshop in Laugarvatn, Iceland. Thirty-two sea ice modelling scientists from 11 countries across Europe and North America attended, spanning 3 key areas: (i) developers of sea-ice models; (ii) users of sea-ice models in an ESM context; (iii) users of seaice models for operational forecasting and (re)analyses. The workshop was structured around 2 key themes:

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Scientific and technical validity and limitations of the physics and numerical approaches
 used in the current models

69 2. Physical processes and complexity: bridging the gap between weather and climate70 requirements

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For each theme, 5 keynote speakers were invited to address the motivating questions and
stimulate debate. Further details can be found in the Supplementary Material.

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2. Key points and outcomes from the sea ice modelling workshop

75 Continuum models remain a useful tool for sea ice simulation

76 Sea ice consists of moving, growing or melting, often interlocked, irregular pieces of ice, which 77 can vary in size from a few meters up to tens of kilometres (*floes* and *plates*, see WMO, 1970; 78 Hopkins et al., 2004). In models, the representation of sea ice is divided into one-dimensional 79 thermodynamic processes such as growth and melt, and two-dimensional, horizontal ice 80 dynamics involving ice drift, deformation and transport. To describe the evolution of sea ice at 81 scales of ~100 km over days to months, the AIDJEX group proposed a framework based on an 82 isotropic, plastic continuum approach (Coon et al., 1974), whose validity relies upon statistical 83 averages taken over a large number of floes (Gray and Morland, 1994; Feltham, 2008). 84 Assuming that sea ice behaves as a plastic material at scales of ~100 km and beyond, a viscous-85 plastic rheology (VP: Hibler, 1979; followed by its elastic formulation EVP: Hunke and 86 Dukowicz, 1997) offered physically reasonable and numerically affordable solutions to 87 represent sea ice dynamics. The continuum approach, as well as the (E)VP framework, have 88 since been adopted in virtually all ESMs (IPCC, 2013). The sea ice modelling community now 89 has several decades of experience using these continuum models.

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Many studies demonstrate the ability of the continuum (E)VP models to reasonably simulate
key properties of the sea ice: the large-scale distribution of sea ice thickness, concentration and

circulation (e.g., Kreyscher et al., 1999); relationships between sea ice concentration, thickness
and velocity (Docquier et al., 2017); long-term trends in winter sea ice velocity (Tandon et al.,
2018). With modifications for grounded ridges and tensile strength, continuum models are also
able to realistically simulate the distribution of Arctic land-fast ice — the motionless fields of
sea ice attached to the coast or seabed (e.g., Lemieux et al., 2015; 2016).

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99 However, the core assumptions of the continuum theory are appropriate only for large-scale sea 100 ice evolution, where model grid-cells contain a representative sample of floes. With the increase 101 in available computational resources over the last few decades, several sea ice model 102 configurations have grid-cell sizes of ~1-10 km. This is particularly true for short-range 103 forecasting applications and regional modelling studies, which tend to use such resolutions 104 because the Rossby radius in high-latitude waters can be close to 1 km (Holt et al., 2017). At 105 these resolutions, the continuum assumption likely breaks down (Coon et al., 2007; Feltham, 106 2008).

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Nevertheless, even at kilometric resolution, continuum-based sea ice models continue to be useful. Early evaluations with synthetic aperture radar estimates of drift and deformation (Kwok and Cunningham, 2002) challenged continuum sea ice models' representation of spatiotemporal deformation, particularly in terms of localization and intermittency (Girard et al., 2009; Kwok et al. 2008). However, simulations at kilometric resolutions (effective 10 km) reconcile the model results with observations for many drift and deformation feature statistics at these resolutions (Hutter and Losch, 2020).

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Solver convergence also impacts simulated deformation statistics (Lemieux et al., 2012) and
Linear Kinematic Features (LKFs) within the ice pack (Koldunov et al., 2019). However, as the

spatial resolution is increased in VP continuum-based models, the numerical solution of the sea ice momentum equation is increasingly difficult to obtain due to the strong nonlinearity of the problem. Despite recent nonlinear solver developments (e.g. Losch et al., 2014; Kimmritz et al., 2017; Mehlmann and Richter, 2017), obtaining a fast and numerically converged solution remains a challenge. Another issue is that VP continuum models overestimate the prevalence of large intersection angles between LKFs, which might be fixed by amending the rheological formulation (Hutter and Losch, 2020; Ringeisen et al., 2019).

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126 Alternative rheological formulations have also been proposed to address shortcomings of the 127 VP rheology; the Elastic-Anisotropic-Plastic (EAP) and Maxwell-Elasto-Brittle (MEB) 128 rheologies were discussed at the workshop. The EAP rheology (Wilchinsky and Feltham, 2006) 129 introduces a new state variable, the structure tensor, that tracks the history of past fracture 130 events and allows the orientation of these fractures to evolve at the sub-grid level due to 131 mechanical failure and melting or refreezing. In contrast, isotropic models either assume sub-132 grid-cell cracks do not exist or are isotropically distributed. The EAP model produces realistic 133 scaling of sea ice deformation in idealised configurations and has shown promising results for 134 simulation of the basin-scale sea ice thickness distribution (Tsamados et al., 2013; Heorton et 135 al, 2018). The MEB rheology (Dansereau et al., 2016) is a damage-propagation model, different 136 from the plastic-flow approach taken by VP and EAP, simulating failure by tracking strain-137 induced damage, which gives a high degree of stress localisation. To preserve the localised 138 fields produced by the MEB rheology, the neXtSIM model uses a continuum Lagrangian 139 formulation in which the mesh moves with the ice (Rampal et al., 2016). MEB-based models 140 reproduce some sea ice processes as emergent properties (ice bridges, ridges, land-fast ice; 141 Dansereau et al., 2017), as well as ice drift and spatio-temporal deformation statistics (Rampal 142 et al., 2019).

In summary, despite their reliance on hypotheses that can become invalid at spatial resolutions typically used in modern ESM systems, these continuum-based sea-ice models cannot be readily invalidated using observation-based metrics, and remain useful for large-scale, and low resolution, modelling of sea ice.

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149 Discrete Element Modelling: a promising avenue for the future

Discrete Element Models (DEMs) have long been used to model granular, discontinuous materials, including ice floes (e.g., Hopkins et al., 2004; Hopkins and Thorndike, 2006). By their very nature, DEMs are well suited to modelling sea ice, which - particularly around the ice edge - consists of many individual ice floes.

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Historically, DEMs have not been used to model sea ice within global climate models or forecasting systems because, relative to continuum sea ice models, they require extensive computational resources. However, with increases in available HPC resources, DEMs are becoming relatively more affordable and may actually be more suitable for future HPC architectures, although the uncertainties here are substantial.

160 The relatively large computational cost of DEMs also means that the sea ice modelling 161 community has little experience with these models, and several unresolved issues currently 162 present an obstacle for DEMs to be used for large-scale sea ice modelling. These include how 163 physical processes fundamental to floe evolution, such as pressure ridging, floe aggregation or 164 floe splitting, can be represented in a DEM framework. Current approaches to model 165 initialisation and data assimilation also need to be rethought. Therefore, a considerable amount 166 of time and development is needed before DEMs become usable by a large community. The 167 workshop participants felt that DEMs are not presently able to satisfy the two-pronged criteria 168 - both advanced enough and affordable - required to replace the continuum models used within 169 operational forecasting and climate modelling systems. However, DEMs present a promising 170 approach for future sea ice modelling, which should be explored further. In particular, DEMs 171 would be particularly appealing for operational forecasting applications that require models to 172 reproduce sea ice behaviour on fine spatio-temporal scales. In this regard, a possible future 173 avenue could be a regional DEM nested within a global continuum model.

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175 Navigating the model complexity spectrum: finding the right amount of complexity

The issue of model complexity is complicated and was discussed at length at the workshop. Here we take the term "model complexity" as synonymous with "number and level of detail of the model's parameterisations of physical processes". Although there were advocates for including more complexity and for using more simplified models, the general feeling was that present-day continuum models capture the most important physical processes, in principle. However, the representation of certain key processes is uncertain due to missing observational constraints.

regional forecasts, process understanding), a large spectrum of different levels of complexity is warranted for sea ice modelling, from highly complicated to heavily simplified models. Although several physical processes were identified whose representation was considered crude or even missing in contemporary sea ice models (e.g. snow physics, wave-ice interactions, ridging processes, and intricate atmosphere-ice-ocean coupling/interactions), the impact of their absence from a model is hard to predict. In favour of more simplicity: simple models are cheaper to run and easier to use, debug, and tune, and their output is easier to understand because the likelihood of complex, nonlinear interactions is lower. Also, when considering the climate models participating in CMIP5 (44 distinct models), there is no systematic difference between the projections made by high- or low-complexity models. This suggests that sea ice sensitivity is likely related to the way key processes are treated, and that the simulated evolution of sea ice may depend more on the atmospheric and oceanographic forcing than on the complexity of the sea ice code itself. In favour of complexity: more sophisticated physical formulations are important for improved process understanding, to allow models to simulate changes in ice physics in different climate regimes, and to improve short-term predictions, particularly where there is a need to provide a detailed description of the sea ice state.

In summary, the appropriate physical complexity required strongly depends on the specific model application. Workshop participants recommend that modellers select the most appropriate tool for the job at hand, and complexity should not be used 'blindly' - it is important to understand why one is including the chosen level of complexity. Code modularity is a good way to allow sea ice models to satisfy varying demands in terms of scientific complexity.

The overall conclusion was that, given the diversity of model uses (e.g. climate projections,

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208 HPC requirements cause uncertainty (constraints and opportunities) for future sea ice model

209 *code structure and optimisation*

Current continuum formulations of sea ice dynamics require relatively high levels of communication between processor domains within the rheology and advection calculations. This can make sea ice components a bottleneck in coupled systems, as they tend to scale poorly with increasing HPC resources due to sea ice's localization on the globe. The thermodynamic components, however, rely on one-dimensional 'column' formulations that require very little cross-domain communication, allowing them to scale well with increasing HPC resources.

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HPC resource constraints have historically favoured continuum models, with DEMs being too expensive to run. However, DEMs have the potential to scale better on newer, heterogeneous HPC architectures such those using Graphical Processing Units (GPUs). DEMs benefit from a natural domain decomposition via aggregates of floes, which can be moved to GPUs for Lagrangian and thermodynamic calculations requiring less bandwidth for communication with processors handling other parts of the domain.

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Whether current continuum sea ice models will be able to take full advantage of the resources available on future exascale HPC machines is currently an active area of research. Much of the uncertainty comes from not knowing the form future exascale HPC systems might take, and the fact that the efficiency of the sea ice model component is not likely to be a priority of those people choosing the HPC resources at large modelling centres.

In summary, the jury remains out on whether continuum models will be a viable choice for future HPC architectures and whether DEMs may become more favourable in the future. The answers to these questions will partly depend on the design of future exascale HPC systems, and on the continuum framework's ability to produce sensible looking results for very high resolution simulations (say <100m).

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236 Community involvement plays an important role for sea ice model development, but current 237 practices could be improved

238 Engagement of the broad sea ice modelling community has been crucial for sea ice model 239 development, especially for large community codes such as CICE (Hunke et al., 2020) and 240 SI³/LIM (Rousset et al., 2015). Community involvement can bring considerable model 241 advances by allowing many different research and operational groups to contribute new model 242 functionality and physics, as well as thoroughly testing the code in diverse applications. 243 However, it is important to have well defined long-term plans and to communicate these 244 effectively, so that the wider community can efficiently contribute to the scientific direction of 245 the model while maintaining a streamlined and relevant code base.

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Although engagement of the wider community has been hugely beneficial for the evolution of
large-scale sea ice models, there is scope for even better integration of community activities
within the development process.

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One area of potential collaboration involves common model evaluation tools. Having common
outputs and model diagnostics, such as those defined by the SIMIP community for CMIP6
(Notz et al., 2016), facilitates multi-model evaluation and comparison studies. However it was

felt that community tools, such as ESMValTool (Righi et al., 2020) and MET (Newman et al.,
2019), could be better utilised for evaluation of sea ice models.

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Another area that could benefit from community involvement is assessing the models at a process level, for instance by formulating idealised case studies for model inter-comparison (e.g., wind blowing on an ice pack in a rectangular domain). It was also felt that standard metrics are required against which to compare the models with each other and with observations, and to ascertain how well models capture the leading-order physical processes. For example, a standard metric for measuring the performance of model thermodynamics at leading order would be useful.

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3. Summary and recommendations

265 Continuum sea ice models have been applied close to the presumed limits of their validity for 266 many years, yet they remain compatible with current observations. The resolution requirements 267 for sea ice models varies considerably depending on the application (e.g. large ensembles, 268 paleo-climate simulations, short-range forecasting), and therefore continuum models will likely 269 remain useful for many years to come. Meanwhile, it is highly desirable to explore the potential 270 of DEMs. These models are expected to be more physically faithful at the highest resolutions 271 envisioned for sea ice in ESMs, provided they incorporate all the required processes. DEMs 272 may also prove more efficient for some new computer architectures. Such perspectives 273 highlight the need for the sea ice modelling community to have a clear and consistent vision of 274 the future evolution of HPC systems.

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Sea ice models are used for many different purposes and therefore benefit from modularity,
which allows the activation or exclusion of parameterisations and code features. Thus, users
can adjust model complexity to fit their specific application.

Considering limited human resources among core sea ice modelling groups, engagement of the
wider community has proven a very efficient way to advance large-scale sea ice models.
However, there is still scope for further integration of the wider community in model
development activities.

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An important feature of the Laugarvatn sea ice modelling workshop was the open minded, friendly and respectful atmosphere in which very different views were exchanged. The workshop successfully brought together model developers and users of sea-ice models for Earth-system modelling, operational forecasting and (re)analyses.

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International sea ice modelling workshops such as this foster collaboration and community engagement in the field of sea ice modelling. A recommendation from this workshop is that the exercise should be repeated every 2-3 years to maintain community engagement, exchange cutting-edge ideas, and reinforce collaborative momentum.

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299 References

Coon, M. D., Maykut, G. A., Pritchard, R. S., Rothrock, D. A., Thorndike, A.S.: Modeling the pack
ice as an elastic-plastic material. AIDJEX Bulletin 24, 1–105, 1974.

- 303 Coon, M., Kwok, R., Pruis, M., Levy, G., Sulsky, D., and Schreyer, H. L.:. AIDJEX assumptions
- 304 revisited and found inadequate. Journal of Geophysical Research 112, C11S90,
- 305 doi:10.1029/2005JC003393, 2007.
- 306
- 307 Dansereau, V., Weiss, J. Saramito, P., Lattes, P. A Maxwell-elasto-brittle rheology for sea ice
- 308 modelling. *The Cryosphere*, Copernicus, 10, pp.1339-1359, 2016.
- 309
- 310 Dansereau, V., Weiss, J., Saramito, P., Lattes, P., and Coche, E.: Ice bridges and ridges in the
- 311 Maxwell-EB sea ice rheology, The Cryosphere, 11, 2033–2058, <u>https://doi.org/10.5194/tc-11-2033-</u>
- 312 <u>2017</u>, 2017.
- 313
- 314 Docquier, D., Massonnet, F., Barthélemy, A., Tandon, N. F., Lecomte, O., and Fichefet, T.:
- 315 Relationships between Arctic sea ice drift and strength modelled by NEMO-LIM3.6, The Cryosphere,
- 316 11, 2829–2846, <u>https://doi.org/10.5194/tc-11-2829-2017</u>, 2017.
- 317
- 318 Feltham, D. L.: Sea Ice Rheology. Annual Review of Fluid Mechanics 40, 91–112.
- 319 <u>https://doi.org/10.1146/annurev.fluid.40.111406.102151</u>, 2008.
- 320
- 321 Girard, L., Weiss, J., Molines, J., Barnier, B., and Bouillon, S.: Evaluation of high-resolution sea ice
- 322 models on the basis of statistical and scaling properties of Arctic sea ice drift and deformation. Journal
- 323 of Geophysical Research 114. <u>https://doi.org/10.1029/2008JC005182</u>, 2009.
- 324
- 325 Gray, J. M. N. T., and Morland, L. W.: A two-dimensional model for the dynamics of sea ice.
- 326 Philosophical Transactions of the Royal Society of London. Series A: Physical and Engineering
- 327 Sciences 347, 219–290. <u>https://doi.org/10.1098/rsta.1994.0045</u>, 1994.
- 328
- 329 Hibler, W.D.: A dynamic thermodynamic sea ice model. Journal of Physical Oceanography 9, 815–
- 330 846, 1979.

3	3	1
\mathcal{I}	J	T

332	Heorton, H. D. B. S., Feltham, D. L., and Tsamados, M.: Stress and deformation
333	characteristics of sea ice in a high-resolution, anisotropic sea ice model. Philosophical
334	Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences, 376
335	(2129), https://doi.org/10.1098/rsta.2017.0349, 2018.
336	
337	Holt, J., Hyder, P., Ashworth, M., Harle, J., Hewitt, H. T., Liu, H., New, A. L., Pickles, S., Porter, A.,
338	Popova, E., Allen, J. I., Siddorn, J., and Wood, R.: Prospects for improving the representation of
339	coastal and shelf seas in global ocean models, Geosci. Model Dev., 10, 499-523,
340	https://doi.org/10.5194/gmd-10-499-2017, 2017.
341	
342	Hopkins, M.A., Frankenstein, S., and Thorndike, A.S.: Formation of an aggregate scale in Arctic sea
343	ice. Journal of Geophysical Research 109, C01032, 2004.
344	
345	Hopkins, M.A., and Thorndike, A.S.: Floe formation in Arctic sea ice. Journal of Geophysical
346	Research 111, C11S23. https://doi.org/doi:10.1029/2005JC003393, 2006.
347	
348	Hunke, E.C., and Dukowicz, J.K.: An elastic-viscous-plastic model for sea ice dynamics. Journal of
349	Physical Oceanography 27, 1849–1867, 1997.
350	
351	Hunke, E., et al.: CICE-Consortium/CICE: CICE Version 6.1.1 (Version 6.1.1), Zenodo,
352	http://doi.org/10.5281/zenodo.3712304, March 2020.
353	
354	Hutter, N., and Losch, M.: Feature-based comparison of sea ice deformation in lead-permitting sea ice
355	simulations. The Cryosphere 14, 93–113, <u>https://doi.org/10.5194/tc-14-93-2020</u> , 2020.
356	

- 357 IPCC, 2013. Climate Change 2013: The Physical Science Basis. Contribution of Working Group I to
- 358 the Fifth Assessment Report of the Intergovernmental Panel on Climate Change, Stocker, T.F., D. Qin,
- 359 G.-K. Plattner, M. Tignor, S.K. Allen, J. Boschung, A. Nauels, Y. Xia, V. Bex and P.M. Midgley. ed.
- 360 Cambridge University Press, Cambridge, UK and New York, USA.
- 361
- 362 Kimmritz, M., Losch, M., and Danilov, S.: A comparison of viscous-plastic sea ice solvers with and
- 363 without replacement pressure. Ocean Modelling 115, 59–69,
- 364 <u>https://doi.org/10.1016/j.ocemod.2017.05.006</u>, 2017.
- 365
- 366 Koldunov, N. V., Danilov, S., Sidorenko, D., Hutter, N., Losch, M., Goessling, H., et al.: Fast EVP
- 367 solutions in a high- resolution sea ice model, Journal of Advances in Modeling Earth Systems, 11,
- 368 1269–1284. <u>https://doi.org/10.1029/2018MS001485</u>, 2019.
- 369
- 370 Kreyscher, M., Harder, M., Lemke, P., and Flato, G.M.: Results of the Sea Ice Model Intercomparison
- 371 Project: Evaluation of sea ice rheology scheme for use in climate simulations. Journal of Geophysical
- 372 Research 105, 11,299–11,320, 1999.
- 373
- 374 Kwok, R., and Cunningham, G.F.: Seasonal ice area and volume production of the Arctic Ocean:
- 375 November 1996 through April 1997. Journal of Geophysical Research 107, 8038,
- 376 <u>https://doi.org/doi:10.1029/2000JC000469</u>, 2002.
- 377
- 378 Kwok, R., Hunke, E.C., Maslowski, W., Menemenlis, D., and Zhang, J.: Variability of sea ice
- 379 simulations assessed with RGPS kinematics. Journal of Geophysical Research: Oceans 113.
- 380 https://doi.org/10.1029/2008JC004783, 2008.
- 381
- 382 Lemieux, J.-F., Knoll, D.A., Tremblay, B., Holland, D.M., and Losch., M.: A comparison of the
- 383 Jacobian-free Newton-Krylov method and the EVP model for solving the sea ice momentum equation

- with a viscous-plastic formulation: A serial algorithm study. Journal of Computational Physics 231, 5926–5944. http://dx.doi.org/10.1016/j.jcp.2012.05.024, 2012. Lemieux, J.-F., Tremblay, L.B., Dupont, F., Plante, M., Smith, G.C., and Dumont, D.: A basal stress
- 387
- 388 parameterization for modeling landfast ice. Journal of Geophysical Research: Oceans 120, 3157–3173.
- 389 https://doi.org/10.1002/2014JC010678, 2015.
- 390

385

386

- 391 Lemieux, J.-F., Dupont, F., Blain, P., Roy, F., Smith, G.C., and Flato, G.M.: Improving the simulation
- 392 of landfast ice by combining tensile strength and a parameterization for grounded ridges. Journal of
- 393 Geophysical Research: Oceans 121, 7354–7368. https://doi.org/10.1002/2016JC012006, 2016.
- 394
- 395 Losch, M., Fuchs, A., Lemieux, J.-F., and Vanselow, A.: A parallel Jacobian-free Newton-Krylov
- 396 solver for a coupled sea ice-ocean model. Journal of Computational Physics 257, 901–911.
- 397 https://doi.org/10.1016/j.jcp.2013.09.026, 2014.
- 398
- 399 Manabe, S., and Stouffer, R.J.: Sensitivity of a Global Climate Model to an Increase of CO₂
- 400 Concentration in the Atmosphere. Journal of Geophysical Research 85, 5529–5554, 1980.
- 401
- 402 Mehlmann, C., and Richter, T.: A modified global Newton solver for viscous-plastic sea ice models.
- 403 Ocean Modelling 116, 96–107. https://doi.org/10.1016/j.ocemod.2017.06.001, 2017.
- 404
- 405 Newman, K., Jensen, T., Brown, B., Bullock, R., Fowler, T., and Gotway, J. H.: Model Evaluation
- 406 Tools Version 8.1.2 User's Guide, Developmental Testbed Center Boulder, Colorado,
- 407 https://dtcenter.org/sites/default/files/community-code/met/docs/user-
- 408 guide/MET Users Guide v8.1.2.pdf, October 2019 (last accessed 16th march 2020)
- 409
- 410 Notz, D., Jahn, A., Holland, M., Hunke, E., Massonnet, F., Stroeve, J., Tremblay, B., and
- 411 Vancoppenolle, M.: The CMIP6 Sea-Ice Model Intercomparison Project (SIMIP): understanding sea

- 412 ice through climate-model simulations, Geosci. Model Dev., 9, 3427–3446,
- 413 <u>https://doi.org/10.5194/gmd-9-3427-2016</u>, 2016.
- 414
- 415 Pritchard, R.S.: Sea Ice Processes and Models. Proceedings of the Arctic Ice Dynamics Joint
- 416 Experiment International Commission on Snow and Ice Symposium. University of Washington Press,
- 417 Seattle, Washington, WA, 1980.
- 418
- 419 Rampal, P., Bouillon, S., Ólason, E., and Morlighem, M.: neXtSIM: a new Lagrangian sea ice model,
- 420 The Cryosphere, 10, 1055–1073, <u>https://doi.org/10.5194/tc-10-1055-2016</u>, 2016.
- 421
- 422 Rampal, P., Dansereau, V., Olason, E., Bouillon, S., Williams, T., Korosov, A., and Samaké, A.: On
- 423 the multi-fractal scaling properties of sea ice deformation. The Cryosphere 13, 2457–2474.
- 424 https://doi.org/10.5194/tc-13-2457-2019, 2019.
- 425
- 426 Righi, M., Andela, B., Eyring, V., Lauer, A., Predoi, V., Schlund, M., Vegas-Regidor, J., Bock, L.,
- 427 Brötz, B., de Mora, L., Diblen, F., Dreyer, L., Drost, N., Earnshaw, P., Hassler, B., Koldunov, N.,
- 428 Little, B., Loosveldt Tomas, S., and Zimmermann, K.: Earth System Model Evaluation Tool
- 429 (ESMValTool) v2.0 technical overview, Geosci. Model Dev., 13, 1179–1199,
- 430 <u>https://doi.org/10.5194/gmd-13-1179-2020</u>, 2020.
- 431
- 432 Ringeisen, D., Losch, M., Tremblay, L.B., and Hutter, N.: Simulating intersection angles between
- 433 conjugate faults in sea ice with different viscous–plastic rheologies. The Cryosphere 13, 1167–1186.
- 434 <u>https://doi.org/10.5194/tc-13-1167-2019</u>, 2019.
- 435
- 436 Rousset, C., Vancoppenolle, M., Madec, G., Fichefet, T., Flavoni, S., Barthélemy, A., Benshila, R.,
- 437 Chanut, J., Levy, C., Masson, S., and Vivier, F.: The Louvain-La-Neuve sea ice model LIM3.6: global
- 438 and regional capabilities, Geosci. Model Dev., 8, 2991–3005, <u>https://doi.org/10.5194/gmd-8-2991-</u>
- 439 <u>2015</u>, 2015.

441	Tandon, N.F., Kushner, P.J., Docquier, D., Wettstein, J.J., and Li, C.: Reassessing Sea Ice Drift and Its
442	Relationship to Long-Term Arctic Sea Ice Loss in Coupled Climate Models. Journal of Geophysical
443	Research: Oceans 123, 4338–4359, 2018.
444	
445	Tsamados, M., Feltham, D.L. and Wilchinsky, A.: Impact of a new anisotropic rheology on simulations
446	of Arctic sea ice. Journal of Geophysical Research, 118 (1). pp. 91-107. ISSN 2169-9291,
447	doi:10.1029/2012JC007990, 2013.
448	
449	Wilchinsky, A.V., and Feltham, D.L.: Modelling the rheology of sea ice as a collection of diamond-
450	shaped floes, J. Non-Newtonian Fluid Mechanics, 138, 22-32, 2006.
451	
452	WMO Sea-ice Nomenclature, Terminology, Codes and Illustrated Glossary. World Meteorological
453	Organisation, Geneva. WMO/OMM/BMO 259, TP 145, 1970.
454 455	

