150 million years of sustained increase in pterosaur flight efficiency

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1   **150 million years of sustained increase in pterosaur flight efficiency**

2   Chris Venditti[1*], Joanna Baker[1], Michael J. Benton[2], Andrew Meade[1] and Stuart

3   Humphries[3*]

4   **Affiliations:**

5   [1]School of Biological Sciences, University of Reading, Reading RG6 6BX, United

6   Kingdom.

7   [2]School of Earth Sciences, University of Bristol, Life Sciences Building, Tyndall

8   Avenue, Bristol BS8 1TQ, United Kingdom.

9   [3]School of Life Sciences, University of Lincoln, Joseph Banks Laboratories, Green

10   Lane, Lincoln LN6 7DL, United Kingdom.

11

12   *Correspondence to c.d.venditti@reading.ac.uk and shumphries@lincoln.ac.uk.

13   **Summary**

14   *The long-term accumulation of biodiversity has been punctuated by*

15   *remarkable evolutionary transitions that allowed organisms to exploit new*

16   *ecological opportunities. Mesozoic flying reptiles – the pterosaurs – which*

17   *dominated the skies for over 150 million years (myr) were the product of one*

18   *such transition. The ancestors of pterosaurs were small and likely bipedal*

19   *early archosaurs[1], which were certainly well adapted to terrestrial locomotion.*

20   *Pterosaurs diverged from dinosaur ancestors in the Early Triassic (~245 myr*

21   *ago, Ma), and yet their first fossils come 25 myr later, in the Late Triassic.*

22   *Thus, in the absence of proto-pterosaur fossils, it is difficult to study how*

23   *flight first evolved in this group. Our aim here is to study the evolutionary*

24 **dynamics of pterosaurs' adaptation to a new locomotory medium. The earliest**

25 **known pterosaurs took flight and subsequently appear to have become**

26 **capable and efficient flyers. However, it seems clear that transitioning between**

27 **forms of locomotion[2,3] - from terrestrial to volant – challenged early pterosaurs**

28 **by imposing a steep energetic hill to climb, thus requiring flight to provide**

29 **some offsetting fitness benefits. Using novel phylogenetic statistical methods**

30 **and biophysical models combined with information from the fossil record, we**

31 **detect an evolutionary signal of natural selection acting to increase flight**

32 **efficiency over millions of years. Our results show that there was still**

33 **significant room for improvement in terms of efficiency after the appearance of**

34 **flight. However, in the Azdarchoidea[4], a clade exhibiting gigantism, we test the**

35 **hypothesis that there was a decreased reliance on flight[5-7] and find evidence**

36 **for reduced selection on flight efficiency in this clade. By combining**

37 **biophysical models and phylogenetic statistical methods with the fossil**

38 **record, we offer a blueprint to study functional and energetic changes through**

39 **geological time objectively at a far more nuanced level than has ever before**

40 **been possible.**

41

42 In order to determine how pterosaurs' propensity for flight changed during their

43 evolutionary history, we calculated two indices of flight performance using a

44 biophysical model of powered and gliding flight[8-10]. Firstly, we used an efficiency of

45 flight index (kg m J^{-1}), that is the inverse of the cost of transport[10], CoT^{-1} (see

46 Methods and Table S1 for the flight model parameterization). The CoT (J $kg^{-1}m^{-1}$) is

47 the metabolic energy required to move a unit mass a unit distance at the least

48 energetically expensive travel speed. Secondly, we calculated a sinking rate[10], V_z (m

49 s^{-1}, see Methods) valid for gliding. A low sinking rate allows for longer travel

50 distances per glide, but also for climbing in updrafts where sinking rate must be

51 lower than the rate at which air rises from the ground. Both CoT^{-1} and V_z were

52 calculated using published estimates of mass[11,12], wingspan[13], wing area[11,12], and

53 projected frontal area[12]. The dataset we use in this paper has mass and wing area

54 estimates for 16 species of pterosaur[11] (Table S2, Methods). Although an alternative

55 dataset of mass and wing area estimates is available for 12 species[12], the two

56 datasets cannot be combined owing to considerable differences in the approaches of

57 each paper to body mass estimation (and the fact that the two datasets overlap).

58 However, our results are qualitatively the same using mass and wing area estimates

59 from each of the two datasets in isolation, and so here we only report the results

60 from one dataset[11]. We use published frontal areas[12] and wingspans[13] (see Methods

61 for details).

62   Studying the changes in CoT^{-1} and V_z through time can inform us about how

63 evolutionary changes such as natural selection have acted on flight performance

64 throughout the course of pterosaur evolution. The lack of proto-pterosaurs in the

65 fossil record means that it is currently impossible to be sure how the pterosaurs

66 initially overcame the energetic hill necessary to achieve flight. Our aim is to study

67 the evolutionary dynamics of pterosaurs' adaptation to a new locomotory medium.

68 The earliest known pterosaur fossils indicate they were able to fly[14]. If during their

69 150 myr of evolution their flight performance and efficiency did not improve or

70 decrease we would expect to see no trend in CoT^{-1} and V_z over time (Figure 1a). We

71 might however expect that after the start of a transition involving a change in the

72 defining medium of locomotion (i.e. from terrestrial to volant), species would be

73 relatively energetically inefficient at moving in the new environment. Thus, over time

74 they would become more efficient. In this case, we would expect flight efficiency

75 (CoT^{-1}) to increase through time and sinking rate (V_z) to decrease (Figure 1b). We

76 would expect the opposite (a decrease in CoT^{-1} and an increase in V_z over time) if

77 flight performance reduced over time (Figure 1c).

78 In order to study the evolution of flight (including calculation of the flight

79 performance indices), it is necessary to account for shared ancestry owing to

80 phylogeny. Several phylogenetic trees for pterosaurs exist in the literature [e.g. 1,15,16],

81 but none of these provides well-justified estimates of the uncertainty among species

82 relationships and divergence dates. To account for phylogenetic and temporal

83 uncertainty in our analyses we constructed a Bayesian dated posterior sample of

84 phylogenetic trees for 128 pterosaurs using published character state data[15] (Figure

85 2, Supplementary Data 1, and see Methods).

86 Wingspan is strongly associated with pterosaur morphologies. We find

87 wingspan explained 97% (range of the posterior distribution, 95–98%) of the

88 variation in mass, 97% (96–98%) of the variation in wing area, and 75% (71–87%) of

89 the variation in frontal area. Then using a phylogenetic prediction method[18] we

90 derived a posterior distribution of imputed masses, projected frontal area and wing

91 area for a further 59 species of pterosaurs based on the results of the phylogenetic

92 regression analyses and our phylogenetic tree (Table S2). Our use of Bayesian

93 phylogenetic methods means we integrate our analyses over all phylogenetic

94 (topology and divergence dates) and model uncertainties. Thus, based on our

95 imputations, we calculated a posterior distribution of 1000 CoT^{-1} and 1000 V_z

96 estimates for use in our analyses of flight performance through time (see Methods).

97 Our final set of analyses used information from 75 species, including the uncertainty

98   from imputed values that span the majority of the phylogenetic diversity of all known

99   pterosaurs (Figure 2a).

100   While CoT^{-1} is an efficiency index related to the amount of energy needed to

101   travel a given distance, independently of how long it takes, we do expect it to

102   correlate with mass[19]. It is energetically cheaper for a large animal to move a given

103   mass over a particular distance than for a small animal to travel the same distance[20]

104   (Figure 2b). Sinking rate is similarly affected by mass (Figure 2c) and reflects the

105   relationships we know for birds and bats (Supplementary Information).

106   This relationship with mass means that we need to simultaneously consider

107   mass and its evolutionary association with flight performance in our analyses of flight

108   efficiency and sinking rate through time. With this in mind, pterosaurs have been

109   reported to conform with the well-known Cope's rule[13] – a phenomenon where

110   species increase in size through geological time. The most compelling evidence for

111   this is derived from analyses reporting an increase in wingspan from ~150 Ma to the

112   end of the Cretaceous (~66 Ma) coincident with the origin of birds (Avialae)[13].

113   However, such a trend could emerge as a consequence of increased flight efficiency

114   rather than increase in body size *per se.* Animals with a larger wingspan for their

115   mass are likely to be more efficient flyers[9]. We find using a phylogenetic regression

116   model that accounts for the uncertainty in our inferred tree and our estimates of

117   species masses, frontal area and wing area (see Methods), that pterosaur size did

118   increase significantly through time. In addition, a model that allows the rate of mass

119   increase through time to differ before and after the origin of the birds fits significantly

120   better than a model without such an inflection. In line with earlier conclusions[13], we

121   find that there is no significant increase in size until ~150 Ma ($p_x = 0.59$). From that

122   point the average pterosaur grew significantly from 0.60 kg to 6.05 kg (proportion of

123   the posterior distribution that crosses zero, $p_x = 0.02$), a ~10-fold increase in size,

124   over 65 million years.

125   Turning now to flight performance, there is a growing body of evidence

126   indicating that the Azhdarchoidea had strong terrestrial affinities[5-7,21] (cf. [22]). Here the

127   Azhdarchoidea are considered to comprise the common ancestor and all

128   descendants of *Tapejara, Quetzlcoatlus,* and *Dsungaripterus*[1] (posterior nodal

129   support = 0.83 in our phylogeny). Evidence suggests that azhdarchoid pterosaurs

130   had relatively inflexible necks[7], left tracks indicating terrestrial proficiency[5], and

131   possessed other adaptations associated with ground-dwelling generalist foraging

132   (reviewed[6,7]). Dsungaripterids (the most basal azdharchoids in our phylogeny, Figure

133   2) are reported to have been wading foragers[14,21] feeding on hard-shelled organisms

134   at water margins[23]. Given the terrestrial tendencies in the Azhdarchoidea compared

135   to what we know about other pterosaurs, we might expect diminished reliance on

136   flight, leading to the expectation that they might have differed from other pterosaurs

137   in the selection pressures for adaptations associated with flight and locomotion.

138   Thus, in our analyses we test whether the evolution of flight performance through

139   time in the Azhdarchoidea is distinct from other pterosaur species.

140   Applying phylogenetic regression to flight efficiency through time we find that,

141   even after accounting for mass, efficiency increased significantly ($p_x = 0.00$, Figure

142   3a–c) in non-azdarchoid pterosaurs. However, in contrast to our finding for mass,

143   there is no significant effect associated with the arrival of birds ($p_x = 0.47$). Early

144   pterosaurs (<200 Ma) had an average efficiency of 0.29 kg m J^{-1} but by 70 Ma they

145   were greater than 50% more efficient (CoT^{-1}= 0.51 kg m J^{-1}). Congruently we find

146   that sinking rate (after accounting for mass) for non-azdarchoid pterosaurs reduced

147   from 0.80 m s^{-1} to 0.50 m s^{-1} over the course of the 150 myr of their evolutionary

148   history (Figure 3d–f). In contrast, azdarchoids exhibited no change in efficiency or

149   sinking rate from origin to extinction.

150   Our results show that, save for azdarchoids, following their transition to volant

151   locomotion, the pterosaurs exhibited a sustained increase in flight efficiency over 150

152   myr until their extinction. To achieve this, natural selection acted to decouple the

153   evolution of body size and wingspan (Figure 3g–i) to sculpt these enigmatic

154   creatures from what might have been inefficient flyers that took to the air for only

155   short spells, to creatures that could fly long distances over extended periods. At their

156   origin, some ~147 Ma, 85 myr after the origin of crown pterosaurs, azdarchoids had

157   a slightly lower flight efficiency and higher sinking rates compared with their

158   contemporaries – and showed no temporal trends in either trait until their eventual

159   extinction (Figure 3a–f). This reduced pattern of flight efficiency is also borne out in

160   analyses of gross morphology - azdarchoids arose with short wings for their size,

161   and maintained this condition until their final demise.

162   Our approach demonstrates the power of combining biophysical models and

163   phylogenetic statistical methods with the fossil record to understand the evolution of

164   flight in pterosaurs. In doing so we offer a blueprint to study functional and energetic

165   changes objectively through geological time at a far more nuanced level than has

166   ever before been possible.

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222

223 **Figure 1: Hypothesised scenarios of the evolutionary trajectory of flight**

224 **performance metrics through time**. a) No relationship between flight performance

225 metrics and time would indicate no directional change in flight ability through time. b)

226 An increase in efficiency through time and a reduction in sinking rate would

227 demonstrate a general tendency for selection favouring increased flight performance

228 as the pterosaurs radiated. c) A decrease in efficiency and an increase in sinking

229 rate would imply a reduction in flight performance through time. The branches of the

230 phylogenetic trees are coloured by hypothesised magnitudes of efficiency (green)

231 and sinking rate (blue).

232

233 **Figure 2: Pterosaur phylogeny and the relationship of flight performance**

234 **metrics with mass**. a) Density diagram [17] showing the uncertainty in our

235 phylogenetic reconstruction for pterosaurs (n=128, see Methods for details).

236 Superimposed is the maximum clade credibility tree and triangle points indicate

237 species for which we have published data on mass, wing area, frontal area, and

238 wingspan. Circle points indicate species for which we have wingspan only. Red

239 denotes azdarchoids. b) The relationship between flight efficiency and mass (n=75),

240   with our mean phylogenetic imputations plotted with standard deviations shown by

241   the green ellipses. c) The relationship between sinking rate and mass (n=75), with

242   our mean phylogenetic imputations plotted with standard deviations shown by the

243   blue ellipses.

244

245   **Figure 3: Flight performance through time.** Summary plots for each of our three main

246   traits of interest (efficiency, a–c; sinking rate, d–f; wingspan, g–i). A phylogeny of the species

247   included in each analysis (a, d, g) is shown with branches shaded by reconstructed trait

248   values; Azdarchoidea is highlighted in red. Trait data are shown plotted against time (b, e, h)

249   where all species with imputed values are represented by circles – excepting wingspan data

250   which is all from published sources. Points are coloured by species' body mass and

251   azdarchoid species are outlined in red. The posterior distribution of model predictions for

252   each trait against time (c, f, i) shows how these traits evolved during pterosaur history.

253   These relationships demonstrate that – after accounting for size – pterosaurs continually

254   increased their efficiency (c) and wingspan (i) whilst there was a continual reduction in

255   sinking rate (f) through time (grey lines, median in black). This applies to all pterosaurs

256   except azhdarchoids (pink lines, median in red) which show no significant trends – although

257   they do have relatively short wings for their mass (i).

258

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260

261

Methods

Phylogenetic Inference

All morphological data were obtained from a published phylogenetic character matrix[15]. However, we retained only discrete morphological characters, excluding the continuously varying characters, and treating all ordered characters as unordered, resulting in a total of 220 discrete morphological characters coded for 128 pterosaur species.

We constructed a posterior sample of time-calibrated phylogenetic trees for pterosaurs using the birth-death serial-sampling model[24,25] as implemented in BEAST v2.4[26] allowing for simultaneous estimation of both the topology and divergence times. For each species, we tip-dated using the midpoint of the stratigraphic age representing the first appearance of each species using published time intervals[1,13,15]. The origin of the birth-death process was estimated from a uniform prior distribution ranging from the age of the youngest species in the tree (*Eudimorphodon rosenfeldi*) up to an arbitrary upper limit of 350 Ma.

Owing to the lack of information about speciation and extinction rates in the pterosaur literature we took a conservative approach by placing a wide uninformative prior distribution (uniform ranging between 0 and infinity) on both the effective reproductive number (the birth-death ratio) and the "become uninfectious rate" (total death rate). Similarly, we placed an uninformative uniform prior between 0 and 1 on the sampling proportion. Together, these parameters enable direct estimation of birth-death rates throughout the phylogenetic tree[24].

We modelled rate heterogeneity across lineages using an uncorrelated relaxed morphological clock[27]. We placed an exponential prior (mean = 1) on the mean of the lognormal distribution from which the branch-wise clock rates are drawn,

287   and a gamma prior (α = 0.5396, β = 0.3819) on the standard deviation. Characters

288   were partitioned on the basis of the number of discrete states, and we applied Lewis'

289   Markov k (Mk) model of morphological character evolution[28] across all partitions,

290   estimating a shared gamma shape parameter (Γ_4)[29] using an exponential prior

291   distribution with mean = 1.

292   The MCMC chain was run for one billion iterations, sampling every 100,000

293   iterations after convergence. To produce the posterior sample of 1,000 phylogenetic

294   trees used in the main analyses, we randomly sampled 1,000 iterations from this

295   chain, ensuring that all parameters had an effective sample size of >500, calculated

296   using Tracer v1.6[30]. We ensured that all parameters that were estimated using a

297   uniform uninformative prior (origin, effective reproductive number, become

298   uninfectious rate, and the sampling rate) returned a posterior distribution of

299   estimates that differed from the prior. The analysis was repeated multiple times to

300   ensure convergence was reached. All chains were inspected visually using Tracer

301   v1.6[30].

302   The full sample is visualized in Figure 2a as a density tree produced in R[31]

303   using functions available in the package phangorn[17], and is available to download in

304   nexus format as Supplementary Data 1 of this article.

305   *Imputation of pterosaur measurements*

306   To calculate our efficiency index (see below) we required mass, frontal area and

307   wing area for adult pterosaur species. Estimates for mass and wing area are

308   available for N=16 species from Witton [11] and N=12 species from Henderson [12] (see

309   Table S2). For frontal area values are taken from Henderson [12] (N = 12, though see

310   below). Independently for each of the two datasets, we used the phylogenetic

311   method outlined in[18] to impute a posterior sample of 1000 estimates of mass, frontal

312   area and wing area for a total of N = 75 species. We obtained wingspans for

313   additional species from[13] (a list of species used is found in Table S2) and used each

314   morphological trait's relationship with wingspan (i.e. a phylogenetic regression of

315   each trait against wingspan) to impute species-specific values. As a part of this

316   procedure, we also imputed frontal area for the N=7 species in the Witton [11] dataset

317   which did not have data in Henderson [12] (see Table S2).

318   *Flight energetics model*

319   Animal powered flight energetics, while perhaps kinematically different for bats, birds

320   and pterosaurs, are still ultimately constrained by physics. It has previously been

321   demonstrated that it is possible to infer flight performance of pterosaurs using

322   biophysical models of flight in combination with metabolic scaling estimates from

323   birds[8]. Here we used an actuator-disc based model owing to the pedigree of this

324   approach and because more complex wake dynamics models and computational

325   approaches are particularly difficult to parameterize, requiring a number of kinematic

326   parameters such as wingbeat frequency that are impossible to infer from fossil

327   material. We used a modified version of Pennycuick's Flight model (v1.25)[9] that we

328   developed from earlier work[8] and implemented in Matlab®[32], and which includes

329   published parasite power estimates[33]. Flight performance is estimated based on

330   morphological measurements such as body mass, wingspan and wing area (Table

331   S1) and the model produces a U-shaped power-to-airspeed relationship, from which

332   a minimum power speed (V_{mp}) can be calculated. This V_{mp} is the least energetically

333   expensive flight speed and so provides a useful proxy for efficiency[10] when

334   incorporated into the CoT.

335   We used the model to estimate the metabolic and mechanical power required

336   for powered (flapping) flight given information on a minimal set of morphological

337   traits and estimates of physiology, as well as aerodynamic constants (Table S1). The

338   intersection of the power curve with an animal's available metabolic power (P_{BMR},

339   calculated from mass and estimated basal metabolic rate, BMR) allows us to

340   characterise flight ability[9,34]. Consistent with current thought[35,36], and in line with

341   previous studies[8], we assume that pterosaurs had a BMR similar to that of birds.

342   *Estimation of energetic efficiency*

343   A number of energetic efficiency measures exist[10] but one useful proxy is the inverse

344   of the mass specific Cost of Transport (CoT, the energy required to move a unit

345   mass a unit distance, independent of the time taken to do so). We estimate CoT as

346     $P_{BMR}/(V \times M)$ where V is the least energetically expensive travel speed (i.e. V_{mp}) and

347   other parameters are as in Table S1.

348   For species with available data (Table S2) we produced a single estimate of

349   CoT^{-1} using the inverse of the above formula. For each of the species for which we

350   imputed mass, frontal area and wing area (Table S2 and above), we use the full

351   sample of our imputed values to produce a posterior sample of 1000 estimates of

352   CoT^{-1}.

353   As formulated, CoT accounts for mass. However, as energy efficiency

354   appears to increase with body size[19,20] we included size in our regression model of

355   CoT^{-1} through time (main text and see below) to account for this.

356   *Estimation of sinking rate*

357   Sinking rate while gliding (V_z) was calculated as $D \times V_{mp} / M \times g$ (where D is the total

358   aerodynamic drag resulting from the addition of the induced, parasite and profile

359   drags) and assuming a linear wingspan reduction (see[34]).

360   *Phylogenetic regression models testing temporal trends in mass and efficiency*

361   To test the evolutionary trajectories of pterosaur mass and measures of flight

362   efficiency through time we use phylogenetic generalized least squares[37,38] multiple

363   regression models in a Bayesian framework. We assessed the significance of

364   regression parameters using the proportion of the posterior distribution that crosses

365   zero, p_x, where we consider $p_x < 0.05$ as significant. In addition to the 16 species for

366   which we have single estimates of body mass, V_z and CoT^{-1} from[11] (or N = 12

367   from[12]), in all our models we include the full set of posterior estimates of both body

368   mass and CoT^{-1} for all species for which the data are imputed (Table S2). These

369   values are sampled in proportion to their probability during the running of the MCMC

370   chain. This allows us to incorporate information about the variance of our

371   imputations, avoiding problems associated with summarizing the posterior

372   distribution into a single point estimate.

373

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Author Contributions

All authors contributed to all aspects of this research.

Author Information

[1]School of Biological Sciences, University of Reading, Reading RG6 6BX, United Kingdom.

[2]School of Earth Sciences, University of Bristol, Life Sciences Building, Tyndall Avenue, Bristol BS8 1TQ, United Kingdom.

[3]School of Life Sciences, University of Lincoln, Joseph Banks Laboratories, Green Lane, Lincoln LN6 7DL, United Kingdom.

 *Correspondence to c.d.venditti@reading.ac.uk and shumphries@lincoln.ac.uk.

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Data Availability Statement

The phylogeny we generated in this study (presented in Figure 2a) is included as Supplementary Information (Supplementary Data File 1) with this article. No other data was generated or analysed during the current study. All data used are available from published sources and are cited in the main text where appropriate.

Software and Code

All analyses in this research were conducted using readily available, published programs and are cited in the text. Version numbers of the programs we used are as follows: Tracer v1.6. (2015), MATLAB v9.2 (2017), R v3.4.4 (2017), BEAST 2 (2014), BayesTraits v3 (2018).