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Impact of Heat Storage on Remote-Sensing Based Quantification of Anthropogenic Heat in Urban Environments

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Abstract

Anthropogenic heat (AH) significantly impacts urban climates. Although combining the surface energy balance (SEB) with remote sensing data (RS-SEB) is promising for AH quantification, it has been shown to yield paradoxical low AH values in urban centers. Some speculation on the causes for the underestimation has appeared in the literature; however, none has been verified or thoroughly evaluated, largely hindering the further improvement of spatial representation of AH estimated through the RS-SEB approach. Here by casting the difference in the SEB between the observed reference state and a hypothetical scenario without AH, we developed a thermal stability analysis framework to identify the primary causes. Using AH estimations from six representative US cities based on Local Climate Zone (LCZ), we find that the reduced efficiency of the pathway from AH to sensible heat flux

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near high-rise buildings results in greater heat storage, which is a primary contributor to the underestimation. This study highlights the importance of heat storage in AH quantification using remote sensing data and provides evidence for potentially correcting the bias in AH with improved heat storage modeling.

Keywords: Anthropogenic heat flux, Surface energy balance, Heat storage

1 **1. Introduction**

2 More than 55% of the global population lives in urbanized areas, but
3 account for nearly 70% of the world’s annual energy use (Quah and Roth,
4 2012). The energy consumed to sustain anthropogenic activities (e.g. trans-
5 portation, building energy and industrial processes) and human metabolism
6 have been well recognized as an important source term in the energy bud-
7 get for an urban system across multiple spatial scales (Pigeon et al., 2007;
8 Sailor and Lu, 2004; Allen et al., 2011), often denoted as the anthropogenic
9 heat (AH). As an important component of the urban surface energy balance
10 (SEB), AH impacts the urban climates non-trivially. For example, AH is an
11 important contributor to the urban heat island effect (Bohnenstengel et al.,
12 2014; Chow et al., 2014). The occurrence and spatial distribution of urban
13 precipitation are also sensitive to AH (Holst et al., 2016; Feng et al., 2012;
14 Nie et al., 2017; Zhang et al., 2018). However, accurate description of spatial
15 and temporal evolution of AH is still challenging.

16 Inventory-based approaches (e.g. (Iamarino et al., 2012; Quah and Roth,

17 2012; Sailor, 2011; Allen et al., 2011)) derived from energy-consumption data
18 have been successfully applied to quantify AH, often offering temporal profiles
19 of AH but lacking fine-grained spatial details due to data availability (Dong
20 et al., 2017). The observational-based approach (e.g. (Offerle et al., 2005;
21 Pigeon et al., 2007; Chow et al., 2014)) quantifies AH as a residual term in the
22 SEB, which is usually adopted in the urban meteorology community, when
23 other components of the SEB are directly available from observations such
24 as using flux-tower measurements. However, the term representing change in
25 heat storage in the SEB that can vary with different seasons is often neglected
26 (e.g. Chow et al. (2014)) and only neighborhood-scale AH can be obtained
27 using this method (i.e. integrated over flux footprint of tower sensors).

28 On the other hand, much finer spatial detail and wider geographical cov-
29 erage have been achieved by using remote-sensing based approaches, in which
30 different methods have been developed for mapping AH estimates for a di-
31 verse range of spatial-temporal scales (e.g. (Zhang et al., 2019; Chrysoulakis
32 et al., 2018; Kato and Yamaguchi, 2005)). One of the widely adopted meth-
33 ods considers the urban SEB and uses the easily accessible remotely sensed
34 (RS) surface temperatures from satellite platforms to quantify AH (Kato and
35 Yamaguchi, 2005), hereafter referred as the RS-SEB method. First developed
36 by Kato and Yamaguchi (2005), the RS-SEB method is based on the idea
37 that AH-induced increases in air and surface temperatures predominantly
38 raise the sensible heat flux, with only negligible effects on other terms in
39 the SEB. In essence this is to assume that all of the AH is removed from

40 the control volume by the sensible heat pathway. Later applications of the
41 RS-SEB method have unequivocally adopted this assumption (Zhou et al.,
42 2012; Wong et al., 2015). Despite reasonable spatial distribution of AH at the
43 regional-scale, finer grained studies have resulted in anomalously low values
44 of AH in parts of the urban center (Kato and Yamaguchi, 2005; Wong et al.,
45 2015; Zhou et al., 2012), contradicting both common sense and inventory-
46 based data (Zhou et al., 2012; Dong et al., 2017). This phenomenon has been
47 speculated to be caused by the shading of tall buildings causing deviations
48 in skin temperature, e.g., in Kato and Yamaguchi (2005), but no clear con-
49 sensus has been reached. Therefore, we explore here in greater depth the
50 underlying key assumption of the RS-SEB for AH quantification.

51 If we consider a typical control volume containing the top of the roughness
52 sublayer to the depth in the ground with zero diurnally averaged conductive
53 heat flux, the urban SEB with the effect of anthropogenic heating is given
54 by

$$R_n + AH = H + LE + \Delta S, \quad (1)$$

55 where R_n , ΔS , H and LE are the net all-wave radiation, net rate of change
56 in heat storage (hereafter as heat storage for brevity), and turbulent sensible
57 and latent heat fluxes, respectively. In particular, depending on the way in
58 which anthropogenic energy sources are distributed in the control volume
59 (i.e., building energy use, traffic heat exhausts and human metabolism, etc.),
60 AH may cause a non-negligible change in ΔS , which is the net energy stored

61 (or released) by all substances in the control volume (e.g. the canopy air,
62 buildings, ground, vegetation and human beings, etc.) (Oke et al., 2017). It
63 can be conjectured that the transient effect of AH on ΔS may lead to viola-
64 tion of the assumption of AH being directly converted to H in the RS-SEB
65 method. Nevertheless, few studies thus far have targeted the resolution of
66 this issue. Furthermore, the relative impacts of different urban land use and
67 land cover (LULC) types on this assumption remain relatively understudied,
68 which hampers our understanding of the reliability of the RS-SEB method
69 at the neighborhood scale within a city.

70 Motivated by the aforementioned knowledge gaps, this paper first exam-
71 ines the variation of AH estimates across different urban LULC types classi-
72 fied according to the local climate zones (LCZs) (Stewart and Oke, 2012) in
73 Section 2. Then, in Section 3 we present a new theoretical analysis frame-
74 work to examine the impact of heat storage on the RS-SEB method. Final
75 remarks and conclusions are presented in Section 4.

76 **2. AH estimation from satellite observations using the RS-SEB** 77 **method**

78 To examine the profile of AH estimates across LCZ types for a range of
79 cities, we first estimate AH with the classic RS-SEB method (Kato and Ya-
80 maguchi, 2005) for six cities in the US with contrasting sizes and background
81 climates (Chicago, Washington DC, Houston, Los Angeles, Philadelphia, and
82 Phoenix). One scene of Landsat 8 imagery under clear-sky was selected for

83 each city. Since perfectly cloudless condition within the selected domains
84 for all six cities needs to be satisfied, images from satellite overpasses in fall
85 and spring of 2017 were selected. In addition, since background climates in
86 different cities mostly affect energy use for heating and cooling in winter and
87 summer (Sailor, 2011), we avoid these two seasons and only focus on the
88 ‘baseline’ anthropogenic heat in spring and fall. The components of the
89 SEB were computed following similar procedures and methods as outlined
90 in Kato and Yamaguchi (2005), with details of the computation presented in
91 Appendix A.

92 The urban LULC types were classified according to the LCZs, which Stew-
93 art and Oke (2012) defined to be ‘regions of uniform surface cover, structure,
94 material, and human activity that span hundreds of meters to several kilome-
95 ters in horizontal scale’. The LCZ classification maps were obtained from the
96 World Urban Database and Access Portal Tools (WUDAPT) (Ching et al.,
97 2018), where LCZ types 1 to 10 (See Figures 1b and d) denote compact
98 high-rise (LCZ 1), compact mid-rise (LCZ 2), compact low-rise (LCZ 3),
99 open high-rise (LCZ 4), open mid-rise (LCZ 5), open low-rise (LCZ 6), light-
100 weight low-rise (LCZ 7), large low-rise (LCZ 8), sparsely built (LCZ 9) and
101 heavy industry (LCZ 10), respectively. The urban canopy parameters needed
102 for the computation were obtained from level-zero data products provided by
103 WUDAPT. In general, AH in a city computed from a single satellite scene is
104 not representative of the annual average. However, in the default level-zero
105 database of AH from the WUDAPT (here defined as $AH_i^{default}$ for the i^{th}

106 LCZ), $AH_i^{default}$ is the annual average value of AH are adopted from the
 107 criteria for LCZ classification (Stewart and Oke, 2012, Table 4). In fact, AH
 108 varies significantly with season, location, and level of energy consumption of
 109 an individual city (Stewart and Oke, 2012). To remove these confounding
 110 issues from the comparison, we focus on how AH^{RS-SEB} varies across LCZ
 111 within any given city. To increase the statistical power of the comparison,
 112 we compute AH^{RS-SEB} for each LCZ by averaging across all of the satel-
 113 lite image pixels corresponding to that LCZ type in a city. Therefore, the
 114 profile of AH^{RS-SEB} across LCZs would represent the persistent structural
 115 differences in energy use intensity across different LCZs. Here, instead of
 116 comparing the magnitudes of AH_i^{RS-SEB} derived from a single scene with
 117 $AH_i^{default}$ that reflects an annual average, we focus on interrogating their
 118 respective variations across the LCZs to reveal any similarity or contrast.

119 Before interrogating the LCZ dependence of AH, we look at the spa-
 120 tial distribution of the estimated AH using the RS-SEB method and the
 121 corresponding LCZ maps for Chicago and Philadelphia in Figure 1, as two
 122 examples. We note oddly low values of AH can be clearly identified in regions
 123 classified as compact high-rise (LCZ 1) and open high-rise (LCZ 4) in the
 124 downtown areas. These patterns consistently occur in other selected cities
 125 and are in stark contrast to the spatial distributions of AH estimated using
 126 inventory-based approach (Chow et al., 2014; Pigeon et al., 2007; Roberts
 127 et al., 2006). The RS-SEB based AH estimates for all cities were averaged by
 128 LCZ type (AH_i^{RS-SEB}) and are presented alongside the inventory estimates

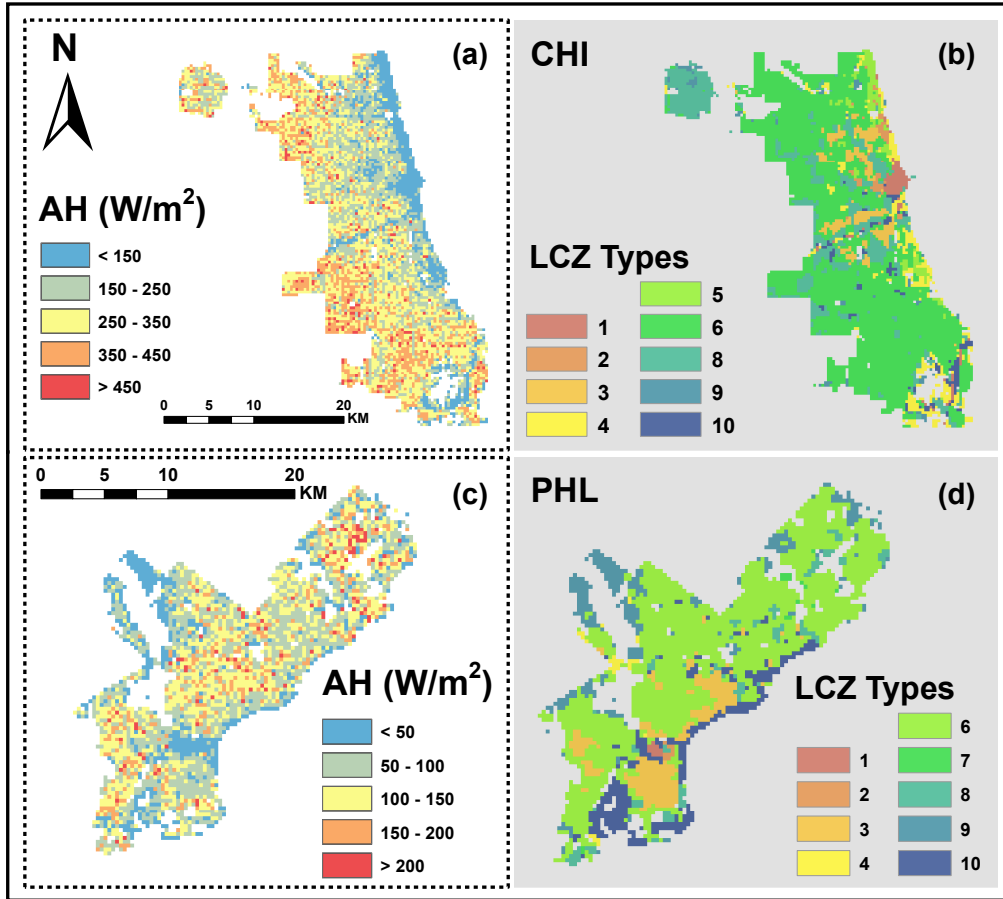


Figure 1: Two examples of the selected cities (Chicago, 20170915, 16:35 UTC and Philadelphia, 20171002, 15:40 UTC) AH results (a, c) and LCZ classifications (b, d) (1: compact high-rise; 2: compact mid-rise; 3: compact low-rise; 4: open high-rise; 5: open mid-rise; 6: open low-rise; 7: light-weight low-rise; 8: large low-rise; 9: sparsely built; 10: heavy industry)

129 of $AH_i^{default}$ in Table 2. The magnitudes of AH_i^{RS-SEB} vary significantly
 130 across the cities, as expected to reflect the city-specific AH characteristics.
 131 Our interest here is in variability of AH across LCZ type for a given city,
 132 and the extent to which the shape of such an AH-LCZ profile is consistent
 133 across different cities. The high-rise LCZ's show lower AH values ($AH_1^{default}$,

134 $AH_4^{default}$) than the low-rise LCZ's ($AH_3^{default}$, $AH_6^{default}$) across the range
 135 of cities, as apparent in the puzzling spatial pattern noted in Figure 1. It
 136 is common to have actual AH values up to several hundreds of $\text{W}\cdot\text{m}^{-2}$, es-
 137 pecially in central urban areas during daily peak hours (Wong et al., 2015;
 138 Zhou et al., 2012). We also note that magnitudes of AH_i^{RS-SEB} in some
 139 LCZs such as LCZ 8 (large low-rise) and LCZ 9 (sparsely built) in Table 1
 140 are large. This is likely related to the heat storage change (ΔS) being mod-
 141 elled as $C_g R_n$ (See Appendix A.2), where the traditional fraction taken from
 142 the literature of $C_g = 0.7$ has recently been questioned as being too large
 143 (e.g. (Oke et al., 2017, Fig. 6.12)). However, instead of focusing on tuning
 144 ΔS in the RS-SEB method, we re-examine the underlying assumption of this
 145 method and thus use the same value of C_g as that in Kato and Yamaguchi
 146 (2005) for consistency.

147 Figure 2 shows the LCZ dependence of AH_i^{RS-SEB} normalized by the
 148 respective city averaged values at the observation time (AH_{mean}^{RS-SEB}) (solid
 149 markers, left y-axis). $AH_i^{default}$ is normalized by $AH_{mean}^{default}$, which is the
 150 default AH weighted by the area fractions of LCZs in each city and aver-
 151 aged across all studied cities, $\overline{AH_i^{default} / AH_{mean}^{default}}$ (open circles, right y-axis).
 152 Here, we are particularly interested in LCZ 1-6 as they represent two cate-
 153 gories of urban construction density: compact (LCZ 1, 2 and 3) and open
 154 (LCZ 4, 5 and 6), where the mean building height decreases with increas-
 155 ing LCZ number within each category (i.e. 1 to 3, and 4 to 6). Across the
 156 studied cities, the magnitudes of $AH_i^{RS-SEB} / AH_{mean}^{RS-SEB}$ generally increase

Table 1: AH^{RS-SEB} across LCZs in different cities and $AH^{default}$ (WUDAPT) (unit: W/m²)

ineB3	CHI	DC	HOU	LA	PHL	PHX	WUDAPT
ineB3 LCZ 1	28.82	81.01	24.64	185.53	-36.87	182.02	175
LCZ 2	111.00	132.30	102.69	/	24.83	/	37.5
LCZ 3	272.49	176.39	/	380.82	104.72	376.24	37.5
LCZ 4	131.58	/	39.26	/	2.41	211.43	25
LCZ 5	94.17	104.85	92.36	278.93	/	282.03	12.5
LCZ 6	297.47	114.69	161.17	345.50	107.52	389.06	12.5
LCZ 7	/	/	/	460.85	91.64	364.16	17.5
LCZ 8	271.18	173.45	139.11	370.48	123.45	362.19	25
LCZ 9	267.50	27.58	55.12	300.33	45.59	357.79	5
LCZ 10	220.79	/	53.57	307.07	52.20	310.41	350
ineB3							

Note: CHI – Chicago (20170915, 16:35 UTC); DC – District of Columbia (20170923, 15:46 UTC); HOU – Houston (20170406, 16:50 UTC); LA – Los Angeles (20171015, 18:28 UTC); PHL – Philadelphia (20171002, 15:40 UTC); PHX – Phoenix (20171003, 18:04 UTC).

157 with decreasing building height in each category, in stark contrast to the
158 decrease of $\overline{AH_i^{default}} / \overline{AH_{mean}^{default}}$ (solid circles). These results are consistent
159 with previous findings that low values of AH occur in parts of the urban cen-
160 ter (where taller buildings are likely to be found) (Wong et al., 2015; Zhou
161 et al., 2012; Kato and Yamaguchi, 2005). These RS-SEB results run counter
162 to the tendency for taller to imply more energy consumption per unit ground
163 area, as seen in the inventory data. Here we further demonstrate that the
164 RS-SEB method leads to low AH values in both dense and open urban con-
165 struction density, which suggests a cause beyond the proposed shading effect
166 of buildings (Kato and Yamaguchi, 2005). Now, in the following section, we
167 proceed to more deeply examine our conjecture about the role played by the

168 net change in heat storage.

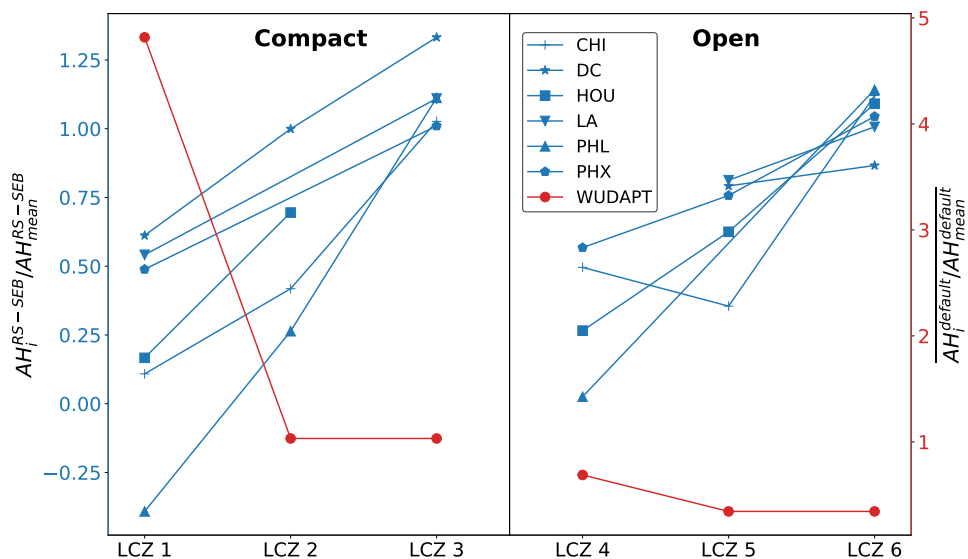


Figure 2: Variation of $\frac{AH_i^{RS-SEB}}{AH_{mean}^{RS-SEB}}$ (Blue lines and left Y axis) and $\frac{AH_i^{default}}{AH_{mean}^{default}}$ (red lines and right Y Axis) across different LCZs. LCZs 1-3 (LCZs 4-6) are characterized by compact (dense) urban density with descending mean building height (i.e., decreasing volume of built materials per unit area from LCZ 1 (LCZ 4) to LCZ 3 (LCZ 6)).

169 3. The impact of AH on heat storage in the SEB

170 To understand the reason for the systematic low values of AH in LCZs
 171 characterized by high-rise buildings, we re-examine the underlying assumption
 172 of the RS-SEB method – that AH completely causes an increase in
 173 sensible heat flux. When integrated over time scales far exceeding one day,
 174 ΔS , the net rate of change in heat storage becomes much smaller than other

175 terms in the SEB, and the underlying assumption becomes reasonable. How-
 176 ever, on sub-daily time scales, especially for a snapshot in time as with remote
 177 sensing, the partitioning of instantaneous AH into other components in the
 178 SEB may be significant (Hanna et al., 2011; Roberts et al., 2006). Here
 179 we consider two scenarios: the first scenario (Case No-Humans) represents
 180 a generic urban surface without any human energy use (e.g., metabolism,
 181 indoor energy use, transportation, industry, etc.); the second scenario (Case
 182 With-Humans) is the same as Case No-Humans, except for the presence of
 183 human activities (i.e., anthropogenic energy sources). Components of the
 184 SEB in Case With-Humans thus differ from those in Case No-Humans only
 185 due to the effects of AH. The SEB for Case With-Humans applied to the
 186 three-dimensional control volume indicated in Figure 3a can be written as

$$R_n + R_{na} + AH = \Delta S + \Delta S_a + LE + LE_a + H + H_a, \quad (2)$$

187 and the corresponding SEB for Case No-Humans is $R_n = \Delta S + LE + H$,
 188 where the subscript ‘a’ denotes the anthropogenically-induced perturbation
 189 to each base component. The effect of advection on the SEB is neglected.
 190 Although the anthropogenic latent heat flux can also be significant in urban
 191 areas especially from cooling systems in summer (Sailor, 2011; Moriwaki
 192 et al., 2008), for the selected data in spring and fall, the direct anthropogenic
 193 emission of water vapor is not considered. However, the potential thermally-
 194 induced change to LE from AH is still considered via LE_a . The difference in

195 SEB between these two scenarios is

$$AH = \Delta S_a + LE_a + H_a - R_{na}. \quad (3)$$

196 The commonly adopted assumption after Kato and Yamaguchi (2005) is
197 $AH \approx H_a$, with R_{na} , ΔS_a , and LE_a assumed to be negligible. If the tur-
198 bulent fluxes are measured, such as by using eddy-covariance measurements,
199 then AH can be unequivocally computed from Equation 2, as the control
200 volume contains all sources of anthropogenic heat emissions, provided $\Delta S +$
201 ΔS_a can be accurately determined, which is a known conundrum in urban
202 SEB studies (Roberts et al., 2006). However, viewing from the satellite’s
203 perspective in Figure 3a, the remotely sensed skin temperature T_s is used
204 to model the SEB components for a two-dimensional surface projection (See
205 Figure 3b), in which T_s encodes critical information about the partitioning of
206 total available energy from both natural and anthropogenic sources among
207 respective components (Wang et al., 2011; Yang and Wang, 2014). In other
208 words, the anthropogenic heat sources in the three-dimensional control vol-
209 ume act to alter the skin temperature T_s with modulation by the heat transfer
210 processes (i.e. radiation, convection and conduction), which critically depend
211 on the specific details of how the anthropogenic heat sources are distributed.

212 From the perspective of energy dissipation in the surface energy budget
213 (Bateni and Entekhabi, 2012) for a generic surface, the total available energy
214 is dissipated via sensible, latent, ground heat fluxes and outgoing longwave

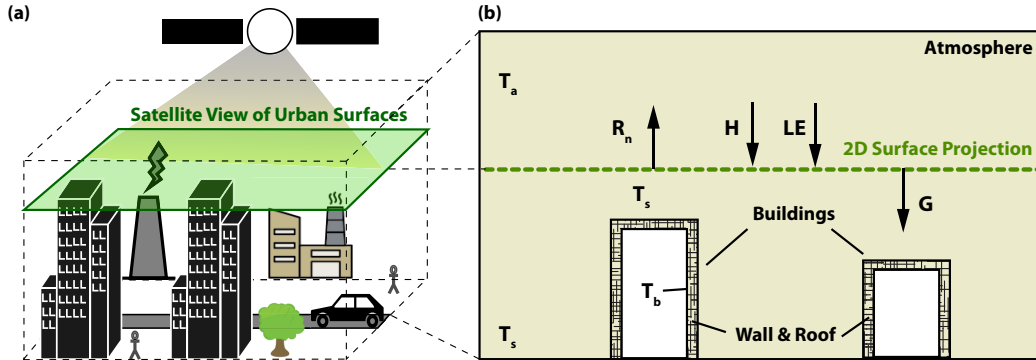


Figure 3: (a) Schematics of a three-dimensional control volume and a two-dimensional surface projection viewed from the satellite. (b) Surface energy budget in the two-dimensional projected surface, which does not explicitly contain sources of anthropogenic heat emissions. However, the three temperatures components (the skin temperature T_s , the inner building wall temperature T_b and the air temperature T_a) are already modified by sources of anthropogenic heat emissions. T_s retrieved from the satellite represents an effective surface temperature from all surfaces including the ground and roofs.

215 radiation. Partitioning of total available energy depends on the relative effi-
 216 ciencies of dissipation via these pathways (Bateni and Entekhabi, 2012; Sun
 217 et al., 2013). Insight into the partitioning of AH can be gained by applying
 218 the force-store approach (Garratt, 1994) to the skin temperature T_s for ur-
 219 ban surfaces (Swaid, 1995; Oke et al., 1991; Johnson et al., 1991; Miao et al.,
 220 2006) (Figure 3b), followed by a stability analysis of the SEB (Bateni and
 221 Entekhabi, 2012). The procedures are outlined briefly here and details of the
 222 derivation are presented in Appendices B and C.

223 First, for a generic urban surface without being influenced by anthro-
 224 pogenic heating (Figure 3b), the change in heat storage ΔS (c.f. Equation
 225 1) is equal to the conductive heat flux at the material surface (Sun et al.,
 226 2017), G , where G is constrained by the surface energy balance given by

227 $G = R_n - H - LE$. We assume that for this material surface under consid-
228 eration, the net effect of human activities (i.e. anthropogenic heating) mani-
229 fests itself by perturbing the thermal boundary conditions of the conductive
230 heat transfer process. Specifically, the building interior wall temperature T_b
231 (Johnson et al., 1991; Oke et al., 1991) and the air temperature T_a are altered,
232 where the deviations are denoted as δT_a and δT_b . T_s is subsequently altered
233 and the change is denoted as δT_s . The increase of air temperature by AH is
234 due to direct heat discharge from traffic and industry processes. Assuming
235 that in the selected spring and fall seasons, there is no indoor cooling by air
236 conditioning, the increase in the interior wall temperature is then solely due
237 to lighting, electrical appliances and other human activities. The perturbed
238 temperatures for this material surface then lead to modified surface energy
239 balance, thus the change in G due to anthropogenic heating can be denoted
240 as $\delta G = \delta R_n - \delta H - \delta LE$.

241 Then, the temporal evolution of the material surface temperature T_s can
242 be studied using the force-restore approach, which has been applied in the
243 urban context (Johnson et al. 1991; Oke et al. 1991), where the restoring
244 temperature is the interior building wall temperature T_b . The new devel-
245 opment here is to extend the force-restore approach to a stability analysis
246 framework (Bateni and Entekhabi, 2012), which reveals the difference in tem-
247 poral evolution of T_s between the cases of No-Humans and With-Humans.
248 The rate of change of T_s is given by an ordinary differential equation for Case

249 No-Humans:

$$\frac{dT_s}{dt} = \frac{\omega^{1/2}}{P} G(t) - \omega (T_s - T_b); \quad (4)$$

250 and for Case With-Humans:

$$\frac{d(T_s + \delta T_s)}{dt} = \frac{\omega^{1/2}}{P} (G(t) + \delta G(t)) - \omega (T_s + \delta T_s - (T_b + \delta T_b)), \quad (5)$$

251 where ω is the principal diurnal frequency corresponding to the principal
252 Earth rotation frequency: $\frac{1}{24 \times 3600} \text{ s}^{-1}$; P is the thermal inertia of the surface
253 material with units $\text{J} \cdot \text{m}^{-2} \cdot \text{K}^{-1} \cdot \text{s}^{-1/2}$, calculated from WUDAPT database.
254 The time evolution of δT_s , the resultant change in T_s due to perturbation by
255 AH, is given by Equation 5 - Equation 4 as:

$$\frac{d\delta T_s}{dt} = \frac{\omega^{1/2}}{P} (\delta G) - \omega (\delta T_s - \delta T_b), \quad (6)$$

256 where δG , the change to G caused by anthropogenic heat emissions, can be
257 substituted using the relation $\delta G = \delta R_n - \delta H - \delta LE$. Since the net short
258 wave radiation is not impacted by δT_s and δT_a , δR_n is given by the change
259 in longwave radiation (LW) (i.e., $\delta R_n = \delta LW$), Equation 6 becomes

$$\frac{d\delta T_s}{dt} = \frac{\omega^{1/2}}{P} (\delta LW - \delta H - \delta LE) - \omega (\delta T_s - \delta T_b). \quad (7)$$

260 Applying the bulk parameterizations for sensible and latent heat fluxes
261 and a linearization of the Stefan-Boltzmann relation for the longwave radia-

262 tion, Equation 7 becomes

$$\frac{d\delta T_s}{d\tau} = - \left(1 + \frac{r_a}{r_o} + \beta \frac{\delta}{\gamma} + \frac{r_a}{r_g} \right) \delta T_s + Q', \quad (8)$$

263 where τ is t normalized by $Pr_a/\sqrt{\omega}\rho c_p$ and the full expressions for $\frac{r_a}{r_o}$, $\beta \frac{\delta}{\gamma}$,
 264 $\frac{r_a}{r_g}$ and Q' can be found in Appendix B. The negative coefficient on δT_s
 265 reflects the dissipative nature of the system towards the equilibrium state
 266 δT_s^* in the long time limit, which is $\delta T_s^* = \frac{Q'}{1 + \frac{r_a}{r_o} + \beta \frac{\delta}{\gamma} + \frac{r_a}{r_g}}$. The right hand
 267 side of Equation 8 indicates that the rate at which the system reaches its
 268 long time limit equilibrium is dependent on the four pathways, with the
 269 relative efficiencies of outgoing longwave radiation, latent heat flux and net
 270 rate change of heat storage at the surface relative to sensible heat flux given
 271 by $\frac{r_a}{r_o}$, $\beta \frac{\delta}{\gamma}$ and $\frac{r_a}{r_g}$, respectively. For example, $\frac{r_a}{r_g}$ denotes the relative efficiency
 272 of G to H in dissipating energy, where r_a is the aerodynamic resistance and
 273 r_g is the surface conductive heat flux resistance given by:

$$r_g = \frac{\rho C_p}{P\sqrt{\omega}}. \quad (9)$$

274 It is worth noting that Oke et al. (2017, in Eq. 6.4)) defines the ratio
 275 between thermal inertia of the urban surface materials, $\mu_g = P/\sqrt{2}$, and
 276 that of the air, μ_a , which indicates the sensible heat sharing between the
 277 urban surface materials and the turbulent air. However, here $\frac{r_a}{r_g}$ signifies the
 278 relative importance of heat storage change compared to sensible heat flux
 279 in contributing to the observed T_s given the net available energy from both

280 radiation and anthropogenic heating. For the usual assumption underlying
 281 the RS-SEB method to be valid, the term $\frac{r_a}{r_g}$ should be much smaller than
 282 one. A large value of $\frac{r_a}{r_g}$ indicates that AH results in non-negligible change
 283 in the net rate change of heat storage, invalidating this assumption. Thus,
 284 we examine $\frac{r_a}{r_g}$ across LCZ types 1-6 (Figure 4). Figure 4a compares $\frac{r_a}{r_g}$ and
 285 gridded AH normalized by the difference between maximum and minimum
 286 values in each city (Chicago and Philadelphia as examples are shown in
 287 Figure 4a). Relatively high values of $\frac{r_a}{r_g}$ are found in areas with a relatively
 288 low amplitude of AH, which usually overlap with the high-rise LCZ types. An
 289 ensemble average of the LCZ-specific values of $\frac{r_a}{r_g}$ and AH^{RS-SEB} across the
 290 sample of cities is considered (Figure 4b), where for LCZ type $i = 1 - 6$ they
 291 are denoted as $\overline{\frac{r_a}{r_g i}}$ and $\overline{AH_i^{RS-SEB}}$. Figure 4b indicates distinctly opposite
 292 trends across the LCZs. Details of $\frac{r_a}{r_g i}$ are further illustrated in Table 2 for
 293 each selected city. Generally, for a given degree of urban surface compactness
 294 summarized by the LCZ types (e.g., compact high, medium and low-rise
 295 buildings in LCZs 1-3, respectively), $\frac{r_a}{r_g}$ decreases with decreasing building
 296 height, in contrast to variation of AH across the LCZ types. The intra-city
 297 differences are mainly due to thermal inertia P (e.g. Values of P in LCZ 4-6
 298 are 1.04×10^3 , 0.98×10^3 and 0.89×10^3 $\text{J}\cdot\text{m}^{-2}\cdot\text{K}^{-1}\cdot\text{s}^{-1/2}$, respectively), while
 299 the inter-city differences can be attributed to different aerodynamic resistance
 300 r_a . For example, r_a in Chicago ranges from 20-30 $\text{s}\cdot\text{m}^{-1}$ in the selected
 301 day; while in Houston, r_a ranges from 60-70 $\text{s}\cdot\text{m}^{-1}$. These results indicate
 302 that for urban surfaces characterized by high and dense building fractions,

303 heat storage is a significant pathway for anthropogenic heat. Therefore, the
 304 key assumption that $AH \approx H_a$ in the RS-SEB method is not applicable in
 305 urban land surfaces where the anthropogenic energy source is more effectively
 306 partitioned into G . A simple parameterization for G as a fraction of R_n will
 307 not account for the partitioned AH, and therefore can lead to consistent
 308 underestimation of AH and the results should be regarded as AH partitioned
 into sensible heat.

Table 2: Means of r_a/r_g in selected LCZs

	LCZ 1	LCZ 2	LCZ 3	LCZ 4	LCZ 5	LCZ 6
ineB3						
ineB3 CHI	0.146	0.133	0.084	0.121	0.113	0.078
DC	0.158	0.147	0.091	/	0.128	0.089
HOU	0.369	0.351	/	0.383	0.323	0.184
LA	0.223	/	0.129	/	0.164	0.110
PHL	0.280	0.229	0.174	0.232	/	0.150
PHX	0.214	/	0.118	0.217	0.165	0.114
ineB3						

309

310 4. Conclusion

311 Remote sensing is an important emerging technique in AH quantification
 312 and estimation of urban surface energy energy fluxes (Chrysoulakis et al.,
 313 2018). The effects of AH intertwined with other components of the SEB
 314 impose significant challenges to quantify changes in the SEB due to anthro-
 315 pogenic energy emissions (i.e., the urban function)(Oke et al., 2017). The
 316 non-negligible change of heat storage term in the SEB caused by addition
 317 of AH becomes important on sub-daily time scales, which critically impact

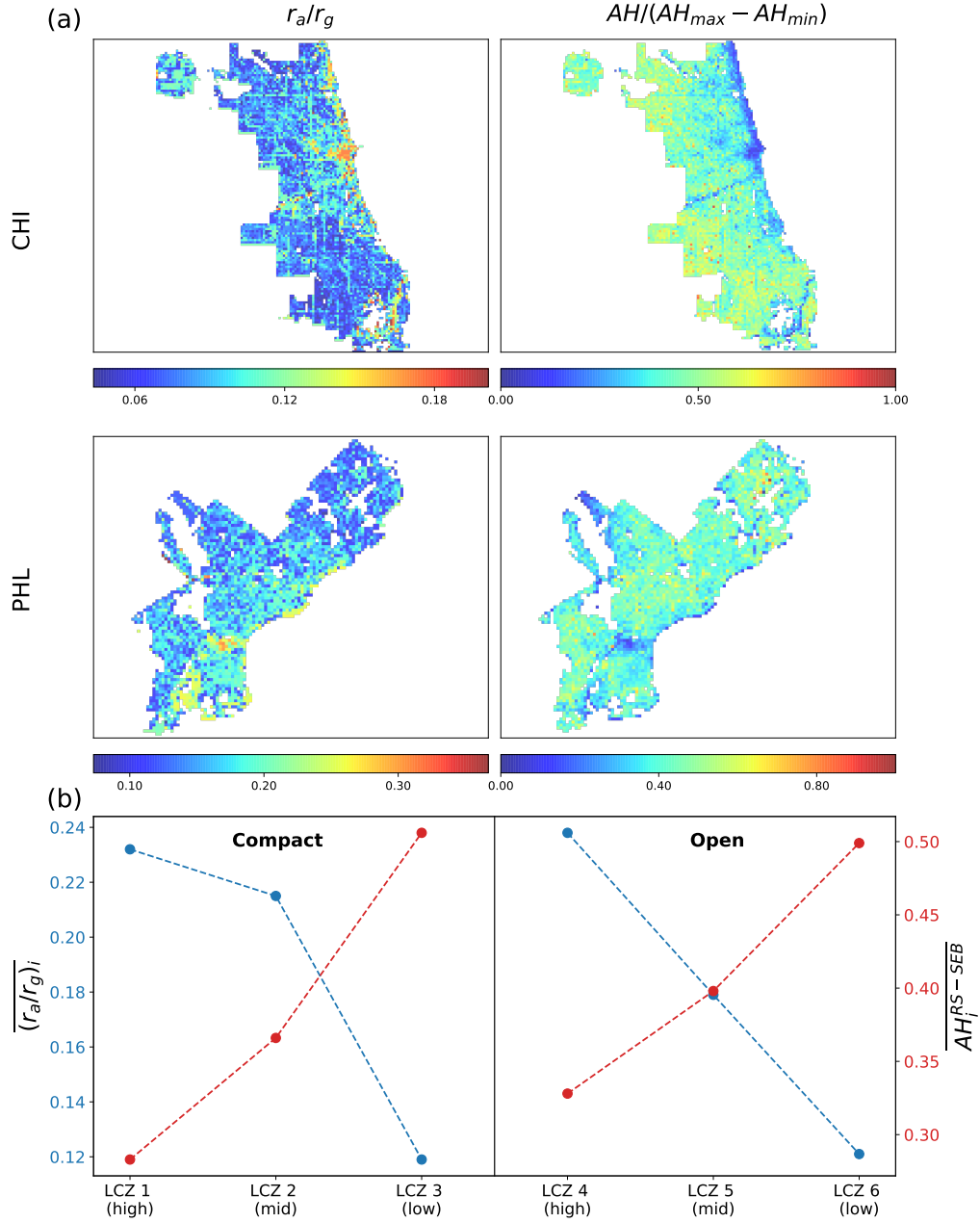


Figure 4: (a) Left column: Energy partitioning efficiencies of heat storage relative to the sensible heat flux in Chicago (CHI) and Philadelphia (PHL). Right column: pixel-wise AH normalized with the difference between maximum AH and minimum AH in respective cities. (b) $\overline{(r_a/r_g)_i}$ and $\overline{AH_i^{RS-SEB}}$; $\overline{(r_a/r_g)_i}$ and $\overline{AH_i^{RS-SEB}}$ for LCZ type i , where $i=1, 2, 3, 4, 5, 6$, averaged over the ensemble of cities.

318 the quality and reliability of AH estimated by the RS-SEB method. The
319 implication of AH-induced change in heat storage is accessed in this study
320 using satellite observations of the land surface temperature combined with
321 analytical investigation under the LCZ classification framework.

322 Leveraging level-zero data from the WUDAPT, we estimated LCZ-type-
323 specific AH in six US cities from Landsat 8. The resultant maps of AH and
324 the corresponding statistics indicate that LCZs with high-rise buildings (i.e.,
325 LCZ 1 and 4) are more inclined to have lower values of AH than those char-
326 acterized by low-rise buildings (i.e., LCZ 3 and 6), regardless of the built-up
327 density, which is opposite to the patterns found in WUDAPT reference values
328 adopted from the LCZ classification criterion (Stewart and Oke, 2012). The
329 discrepancy highlights the importance of AH-induced change in heat stor-
330 age, especially in LCZs with high volume of built materials per unit area.
331 Thus, the assumption of the RS-SEB method, which proposes AH does not
332 alter other components of the SEB except for the sensible heat flux (Kato
333 and Yamaguchi, 2005), can be violated in these LCZs. This implies that on
334 sub-diurnal time scales, the high thermal inertia of building materials causes
335 high heat storage, thus the time lag between building energy consumption
336 and surface temperature increment that is detectable by the remote sensing
337 instruments can significantly deteriorate the reliability of AH computed from
338 the RS-SEB method. It is also noteworthy that the inventory-based method
339 can be affected by this phenomena, since the time lag between energy con-
340 sumption and conversion to anthropogenic sensible heat flux is neglected

341 (Sailor, 2011), introducing uncertainty in deriving the sub-diurnal tempo-
342 ral profile of AH. Subsequent stability analysis of the SEB equation indicates
343 that the efficiency of energy partitioning between sensible heat and heat stor-
344 age given by the ratio of the resistance factors ($\frac{r_a}{r_g}$) is critical in identifying
345 areas prone to errors in AH using the RS-SEB method.

346 In light of the emergence of databases for urban LULC representations
347 (e.g., the WUDAPT (Ching et al., 2018)) and the promising results of using
348 satellite observations to quantify urban surface fluxes (Chrysoulakis et al.,
349 2018), there is a great potential for integrating earth observations into quan-
350 tification of AH with a unified platform of urban LULC database. With
351 relatively straightforward data acquisition, the RS-SEB method can poten-
352 tially be extended to cities worldwide and coupled with numerical weather
353 and climate models for city-specific AH profiles. However, the significant im-
354 pact of AH on heat storage is a key determining factor for its applicability,
355 especially in urban core areas (e.g. LCZ 1 and LCZ 4) with high ratio of $\frac{r_a}{r_g}$.
356 It is recommended that for neighborhoods with a high ratio of $\frac{r_a}{r_g}$, alterna-
357 tive methods to estimate AH such as the inventory method may complement
358 the RS-SEB method. Although overcoming the deficiency of this method
359 is beyond the scope of this study, future research on remote-sensing-based
360 quantification of AH will benefit from improving the representation of the
361 heat storage term (Lindberg et al., 2020; Hrisko et al., 2021) when applying
362 the RS-SEB method. In addition, it implies that AH-induced change in other
363 components of the urban SEB should be cautiously assessed, especially the

364 time-lag between AH and sensible heat for evaluating the impact of AH on
365 time-dependent urban climate phenomena such as precipitation (Holst et al.,
366 2016; Feng et al., 2012; Nie et al., 2017; Zhang et al., 2018).

367 **Description of author’s responsibilities**

368 Zhou Yu: Formal analysis, Method, Writing- Original draft, review and
369 editing; Leiqiu Hu: Method, Writing - Review and editing; Ting Sun: Method,
370 Writing -Review and editing; John Albertson: Method, Writing -Review and
371 editing; Qi Li: Conceptualization, Method, Writing - Original draft, review
372 and editing.

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377 Landsat 8 products can be freely ordered through United States Geological
378 Survey (USGS): <https://earthexplorer.usgs.gov/>. 1-min weather sta-
379 tion data are provided by the Automated Surface Observing System (ASOS):
380 <ftp://ftp.ncdc.noaa.gov/pub/data/asos-onemin/>. Information regard-
381 ing local climate zone (LCZ) classification maps and related surface descrip-
382 tors are available from the World Urban Database and Access Portal Tools
383 (WUDAPT) level 0 database: <http://www.wudapt.org/>.

384 **Appendix A. AH quantification using the RS-SEB method**

385 First, all data from external sources are listed here:

386 Satellite products: Landsat 8 level 1 and level 2 (surface reflectance)
387 images at Chicago (20170915), District of Columbia (20170923), Houston
388 (20170406), Los Angeles (20171015), Philadelphia (20171002) and Phoenix
389 (20171003).

390 Meteorological observations: wind speed and air temperature from ASOS
391 1-min data corresponding to the time of satellite passing. The observation
392 site is the local airport at each city.

393 Atmospheric correction parameters (atmospheric transmission, effective
394 bandpass upwelling radiance and effective bandpass downwelling radiance)
395 required in the retrieval of land surface temperature are calculated by a tool
396 from NASA (atmcorr.gsfc.nasa.gov/), using the mid-latitude summer mode.

397 LCZ-specific urban canopy parameters (e.g. zero-plane displacement height,
398 plan area density, etc.) are from the level 0 data provided by the World Urban
399 Database and Access Portal Tools (WUDAPT).

400 We adopt the framework of Kato and Yamaguchi (2005) to estimate AH,
401 which is briefly outlined here. First, sensible heat flux due to radiant heat
402 balance is denoted as H_n , which can be calculated as the residual of the SEB
403 equation where R_n the net radiation is the energy input:

$$H_n = R_n - G - LE \tag{A.1}$$

404 Secondly, both H_n and the increase in sensible heat flux due to AH, which is
 405 denoted as H_{as} , contribute to the total sensible heat flux H :

$$H_n + H_{as} = H \quad (\text{A.2})$$

406 Therefore, $H_{as} = R_n - G - LE - H$, where R_n , G , LE and H can be
 407 calculated from parameterizations using remotely-sensed surface tempera-
 408 ture. Although H_{as} is not equivalent to AH, under their assumption that the
 409 influence of temperature rise (i.e., increase in both air and surface tempera-
 410 tures due to AH) is only non-negligible for sensible heat in this framework,
 411 $H_{as} = AH$. Next we outline how each component in the SEB equation is
 412 computed. In general, procedures similar to their study are adopted and
 413 whenever appropriate, adaptations of the method to urban land use data
 414 provided by the WUDAPT will be described.

415 *Appendix A.1. Net Radiation (R_n)*

$$\begin{aligned} R_n &= R_{L\downarrow} - R_{L\uparrow} + R_{S\downarrow} - R_{S\uparrow} \\ &= \varepsilon_a \sigma T_a^4 - [\varepsilon_s \sigma T_s^4 + (1 - \varepsilon_s) R_{L\downarrow}] + (1 - \alpha) R_{S\downarrow} \\ &= \varepsilon_s \varepsilon_a \sigma T_a^4 - \varepsilon_s \sigma T_s^4 + (1 - \alpha) G_{SC} \cos \theta d_r \tau \end{aligned} \quad (\text{A.3})$$

416 where ε_s is surface emissivity and ε_a is atmospheric emissivity. T_s and T_a
 417 stand for surface temperature and air temperature (K). T_a obtained from the

418 local airport in each city is assumed to be representative of the entire study
 419 area. This simplification is justified because as reported in a study (Craw-
 420 ford et al. 2018) that estimates heat flux from remotely-sensed land surface
 421 temperature, unevenly distributed air temperature in cities and non-uniform
 422 installation of sensors can introduce uncertainty in spatial interpolation of
 423 the air temperature. Furthermore, the spatial variability of air temperature
 424 above the urban canopy layer is much less than that of remotely-sensed land
 425 surface temperature. Therefore, they opted for using a single reliable air
 426 temperature measurement for flux estimation. α is surface albedo, calcu-
 427 lated on top of band-wise surface reflectance (Wang et al. 2016). σ is the
 428 Stefan-Boltzmann Constant ($5.67 \times 10^{-8} \text{ W} \cdot \text{m}^{-2} \cdot \text{K}^{-4}$). G_{SC} is the Solar
 429 Constant: $1367 \text{ W} \cdot \text{m}^{-2}$. θ is the zenith angle of observation. d_r is the Earth-
 430 Sun distance. θ and d_r are included in the Landsat 8 level 1 product. τ
 431 is the air transmissivity provided by the Atmospheric Correction Parameter
 432 Calculator of NASA.

433 *Appendix A.2. Ground Heat (G)*

434 Ground heat flux can be considered to be proportional to net radiation:

$$G = C_g R_n \tag{A.4}$$

435 where C_g is the determining coefficient. For urban lands, a universal value
 436 of 0.7 is used (Kato and Yamaguchi, 2005).

$$H = \rho C_p \frac{T_s - T_a}{r_a} \quad (\text{A.5})$$

438 where ρ is air density and C_p is specific heat capacity of air. The land surface
 439 temperature T_s , is an alternative of aerodynamic temperature (T_{aero}) for its
 440 easier access. r_a refers to aerodynamic resistance.

441 A pixel-wise modeling of r_a is introduced on three parameters below in-
 442 stead of taking rule-of-thumb values against different land-use types:

443 • **zero-plane displacement height d**

444 This is defined as the height at which zero wind speed is achieved due
 445 to the appearance of obstacles like buildings, trees, etc. It is approxi-
 446 mately two thirds of the height of overlying obstacles on natural sur-
 447 faces. Combining the model from wind-tunnel experiments (Macdonald
 448 et al., 1998) and urban morphological data, we specify its calculation
 449 on every individual urban pixel as below:

$$\frac{d}{H} = 1 + A^{-\lambda_p}(\lambda_p - 1) \quad (\text{A.6})$$

450 where H is the mean height of obstacles, replaced by mean building
 451 height within a grid. λ_p is the plan area density. A is a simulated
 452 constant, which is 4.43 for staggered obstruction arrays under urban
 453 settings (Macdonald et al. 1998). The values of H and λ_p are obtained

454 from the level 0 data in WUDAPT and Oke et al. (2017), respectively
 455 (Table A.3).

Table A.3: H and λ_p values from WUDAPT

ineB3	LCZ 1	LCZ 2	LCZ 3	LCZ 4	LCZ 5	LCZ 6	LCZ 7	LCZ 8	LCZ 9	LCZ 10
ineB3 H	37.5	17.5	6.5	37.5	17.5	6.5	3	6.5	6.5	10
λ_p	0.5	0.55	0.55	0.3	0.3	0.3	0.75	0.4	0.15	0.25
ineB3										

456 *Appendix A.3.1. Wind speed u_z*

457 Wind speed data are from ASOS and nearby automatic weather sta-
 458 tions from Weather Underground (wunderground.com) serve as back-
 459 ups only if data of certain days are missing. Wind speed at each urban
 460 pixel is extrapolated from the weather station value using the reference
 461 height scaling method (Crawford et al., 2018; Wieringa, 1986), where a
 462 neutral stability is assumed in this study. This reference height scaling
 463 method shown in equations below first interpolates the measured wind
 464 speed U to a reference height z_{ref} to obtain U_{ref} , where z_{ref} is assumed
 465 to be 200 m, indicating a level high enough for the logarithmic wind
 466 profile to be valid. Then, U_{ref} is interpolated to 1.5 times the height
 467 of mean obstacle (building) height H at each urban grid to obtain u_z ,
 468 such that bulk aerodynamic method for turbulent fluxes parameteriza-
 469 tion are subsequently applied uniformly across all urban grids at $1.5H$,
 470 which is regarded as near top of the urban roughness sublayer, where
 471 the inertial sublayer with a logarithmic wind profile starts. Although

472 the demarcation of inertial sublayer can vary depending on the under-
 473 lying surface roughness, $1.5H$ seems to be reasonable in computing the
 474 aerodynamic resistance as shown in Crawford et al. (2018).

$$U_{ref} = U_{obs} \frac{\ln\left(\frac{z_{ref}-d_{obs}}{z_{0,obs}}\right)}{\ln\left(\frac{z_{m,obs}-d_{obs}}{z_{0,obs}}\right)} \quad (\text{A.7})$$

$$u_z = U_{ref} \frac{\ln\left(\frac{z_m-d}{z_{0m}}\right)}{\ln\left(\frac{z_{ref}-d_{obs}}{z_{0,obs}}\right)} \quad (\text{A.8})$$

476 d_{obs} is the displacement height at the observational site; $z_{m,obs}$ and $z_{0,obs}$
 477 are the height of wind (momentum) sensor and the roughness length for
 478 momentum at the observational site, respectively. The necessary urban
 479 parameters for the above interpolation at local airports can be obtained
 480 through Davenport classification of effective terrain roughness (Stewart
 481 and Oke, 2012; Davenport et al., 2000) and WUDAPT classification of
 482 local climates. Each observational site at the local airport is located
 483 in the WUDAPT LCZ classification map, where LCZs 8 and 10 are
 484 found as the dominant types for sites. Thus, $H = 10$ m, $\lambda_p = 0.55$, and
 485 the computed displacement height $d_{obs} = 8.0$ m. Furthermore, building
 486 layouts at each local airport are visually inspected in the Google Map,
 487 which then are classified as 'Rough' in Davenport classes with $z_{0,obs} =$
 488 0.25 m according to the tabulated value.

489 *Appendix A.3.2. roughness length for momentum (z_{0m}) and heat (z_{0h})*

490 First, the roughness length (z_{0m}) at each pixel is computed following the
 491 relation $z_{0m} = 1/10H$ as implemented in Grimmond and Oke (1999).
 492 Second, the heat roughness length (z_{0h}) is computed using the kB^{-1}
 493 relation (Crawford et al., 2018; Li et al., 2020):

$$\ln \frac{z_{0m}}{z_{0h}} = kB^{-1}, \quad (\text{A.9})$$

in which

$$kB^{-1} = \beta(Re_*)^{0.25} - 2.0,$$

494 follows the theoretical derivation in (Brutsaert, 1982), where Re_* , the
 495 roughness Reynolds number is $\frac{z_{0m}u_*}{\nu}$, u_* being the friction velocity and
 496 ν being the kinematic viscosity ($1.46 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$). The empirical
 497 constant β varies according to different surface types (Kanda et al.,
 498 2007), here it is modeled with respect to vegetation cover (Crawford
 499 et al., 2018), given by $\beta = 0.87e^{-0.997FVC}$, where FVC is the fractional
 500 vegetation cover.

501 The equation for the bulk aerodynamic resistance r_a is :

$$r_a = \frac{\ln \left(\frac{z_m - d}{z_{0m}} \right) \ln \left(\frac{z_m - d}{z_{0h}} \right)}{k^2 u_z}. \quad (\text{A.10})$$

502 where z_m equals to 1.5 times mean building height, at which height bulk
 503 aerodynamic method for turbulent fluxes parameterization applies.

504 *Appendix A.4. Latent Heat (LE)*

$$LE = \frac{\rho C_p}{\gamma} \frac{e_s - e_a}{r_s + r_a}, \quad (\text{A.11})$$

505 where γ is the psychrometric constant (approximately $0.66 \text{ hPa} \cdot \text{K}^{-1}$); e_s is
506 saturated water vapor pressure and e_a is actual water vapor pressure (hPa);
507 r_s is the stomatal resistance ($\text{s} \cdot \text{m}^{-1}$). For typical urban area, a reference
508 value of 200 for r_s is used (Zhang et al., 2003).

509 **Appendix B. Stability analysis of the SEB using the force-restore**
510 **approach**

511 Details of stability analysis of the SEB equation where the force-restore
512 approach is adopted are outlined in this section. In subsequent derivations,
513 the symbol δ indicates the change of some quantity of interest caused by
514 anthropogenic heat.

515 Change of net longwave radiation is comprised of the change of incoming
516 longwave energy with its outgoing counterpart subtracted:

$$\begin{aligned} \delta LW_{\downarrow} &= \varepsilon_a \sigma (T_a + \delta T_a)^4 - \varepsilon_a \sigma T_a^4 \\ &\approx \varepsilon_a \sigma T_a^4 + 4\varepsilon_a \sigma \delta T_a T_a^3 - \varepsilon_a \sigma T_a^4 \\ &= 4\varepsilon_a \sigma \delta T_a T_a^3 \end{aligned} \quad (\text{B.1})$$

$$\begin{aligned}
\delta LW_{\uparrow} &= \varepsilon_s \sigma (T_s + \delta T_s)^4 - \varepsilon_s \sigma T_s^4 + (1 - \varepsilon_s) \delta LW_{\downarrow} \\
&\approx \varepsilon_s \sigma T_s^4 + 4\varepsilon_s \sigma \delta T_s T_s^3 - \varepsilon_s \sigma T_s^4 + (1 - \varepsilon_s) \delta LW_{\downarrow} \quad (\text{B.2}) \\
&= 4\varepsilon_s \sigma \delta T_s T_s^3 + 4(1 - \varepsilon_s) \varepsilon_a \sigma \delta T_a T_a^3
\end{aligned}$$

$$\delta LW = \delta LW_{\downarrow} - \delta LW_{\uparrow} = 4\varepsilon_s \varepsilon_a \sigma \delta T_a T_a^3 - 4\varepsilon_s \sigma \delta T_s T_s^3 \quad (\text{B.3})$$

517 where ε_s and ε_a are surface and air emissivity, respectively; σ is the Stefan-
518 Boltzmann Constant; T_a and T_s are air temperature and surface temperature
519 (K).

520 Change of δH is attributed to the change of surface temperature and air
521 temperature:

$$\begin{aligned}
\delta H &= \rho C_p \frac{(T_s + \delta T_s) - (T_a + \delta T_a)}{r_a} - \rho C_p \frac{T_s - T_a}{r_a} \\
&= \rho C_p \frac{\delta T_s}{r_a} - \rho C_p \frac{\delta T_a}{r_a} \quad (\text{B.4})
\end{aligned}$$

522 where r_a is the aerodynamic resistance ($\text{s}\cdot\text{m}^{-1}$); ρ is the density of air ($\text{g}\cdot\text{m}^{-3}$);
523 C_p is specific heat capacity of air at a constant pressure ($\text{J}\cdot\text{g}^{-1}\cdot\text{K}^{-1}$).

524 The difference of latent heat is calculated as below, assuming little influ-

525 ence of human activities on actual air humidity (q_a):

$$\begin{aligned}
\delta LE &= \frac{\beta \rho L}{r_a} (q_s^*(T_s + \delta T_s) - q_a) - \frac{\beta \rho L}{r_a} (q_s^*(T_s) - q_a) \\
&= \frac{\beta \rho L}{r_a} (q_s^*(T_s + \delta T_s) - q_s^*(T_s)) \\
&\approx \frac{\beta \rho L}{r_a} \left. \frac{\partial q_s^*}{\partial T_s} \right|_{T_s} \delta T_s
\end{aligned} \tag{B.5}$$

526 where β is a parameter related to moisture availability, L is the specific latent
527 heat of vaporization and q_s^*/q_a represents the function for saturated specific
528 humidity/air humidity at given temperature.

529 Substitute Equation B.5 and Equation B.4 in the main text with the
530 above items:

$$\begin{aligned}
\frac{d\delta T_s}{dt} &= \frac{\omega^{1/2}}{P} \left(4\varepsilon_s \varepsilon_a \sigma \delta T_a T_a^3 - 4\varepsilon_s \sigma \delta T_s T_s^3 - \rho C_p \frac{\delta T_s}{r_a} + \rho C_p \frac{\delta T_a}{r_a} - \frac{\beta \rho L}{r_a} \left. \frac{\partial q_s^*}{\partial T_s} \right|_{T_s} \delta T_s \right) \\
&\quad - \omega (\delta T_s - \delta T_b) \\
&= \frac{\omega^{1/2}}{P} \left(-4\varepsilon_s \sigma T_s^3 - \frac{\rho C_p}{r_a} - \frac{\beta \rho L}{r_a} \left. \frac{\partial q_s^*}{\partial T_s} \right|_{T_s} - \omega \right) \delta T_s \\
&\quad + \frac{\omega^{1/2}}{P} \rho C_p \frac{\delta T_a}{r_a} + 4 \frac{\omega^{1/2}}{P} \varepsilon_s \varepsilon_a \sigma \delta T_a T_a^3 + \omega \delta T_b
\end{aligned} \tag{B.6}$$

After rearrangement of Eq. B.6, where:

$$\tau = \frac{\omega^{1/2}}{P} \frac{\rho C_p}{r_a} t$$

$$r_o = \frac{\rho C_p}{4\varepsilon_s \sigma T_s^3}$$

$$r_g = \frac{\rho C_p}{P\omega^{1/2}}$$

$$\delta_q = \frac{dq_s^*}{dT_s}$$

$$\gamma = \frac{\omega^{1/2} C_p}{L}$$

$$Q' = \frac{\rho C_p}{r_a} (4\varepsilon_s \varepsilon_a \sigma T_a^3 \delta T_a + \frac{\omega^{1/2}}{P} \delta T_a + P\omega^{1/2} \delta T_b)$$

531 We get:

$$\frac{d\delta T_s}{d\tau} = - \left(1 + \frac{r_a}{r_o} + \beta \frac{\delta_q}{\gamma} + \frac{r_a}{r_g} \right) \delta T_s + Q' \quad (\text{B.7})$$

532 Solution to Eq. B.7 is:

$$\delta T_s(\tau) = c_1 e^{-\frac{r_a}{r_o}\tau} e^{-\tau} e^{-\beta \frac{\delta}{\gamma}\tau} e^{-\frac{r_a}{r_g}\tau} + \frac{Q'}{\frac{r_a}{r_g} + 1 + \beta \frac{\delta}{\gamma} + \frac{r_a}{r_g}} \quad (\text{B.8})$$

533 where c_1 is a constant.

534 **Appendix C. Computation of r_a/r_g**

535 r_a is obtained as aforementioned in the estimation of sensible heat flux.

536 The LCZ-specific r_g is given by $P\sqrt{\omega}$, where ω is a frequency parameter
 537 here at the diurnal scale: $\frac{1}{24 \times 3600} \text{ s}^{-1}$ and P is thermal inertia ($\text{J} \cdot \text{m}^{-2} \cdot \text{K}^{-1} \cdot \text{s}^{-1/2}$):

$$P = \sqrt{\frac{Ck}{2}} \quad (\text{C.1})$$

538 where C is heat capacity ($\text{J} \cdot \text{m}^{-3} \cdot \text{K}^{-1}$) and k is thermal conductivity ($\text{J} \cdot$
 539 $\text{m}^{-1} \cdot \text{s}^{-1} \cdot \text{K}^{-1}$). Here P is defined with a prefactor 2 following that in Bateni

540 et al. (2012), which is different from that without the prefactor 2 in Goward
541 (1981); Oke et al. (2017); Wang et al. (2010). Nevertheless, difference in the
542 definition of thermal inertia does not change the variation of $\frac{r_a}{r_g}$ the LCZs.

543 The retrieval of thermal inertia (P) is based on the heat capacity (C) and
544 thermal conductivity (k) data from LCZ look-up tables. Such thermal prop-
545 erties for three elements (roof, wall and road) constituting urban surfaces
546 are provided across ten LCZ types (Table C.4). In addition, such properties
547 for moist soil (in non built-up area) are from Bateni and Entekhabi (2012).
548 The average water content of clay and sand is assumed to be 0.27, based on
549 which volumetric heat capacity is $2.6 \times 10^6 (Jm^{-3}K^{-1})$ and heat conductiv-
550 ity is $1.35 (Wm^{-1}K^{-1})$. A representative thermal inertia is calculated from a
551 weighted assignment of thermal inertia values of the three major urban com-
552 positions. The weight for each LCZ type is decided according to the ratio
553 of surface area between the roof, wall, road and soil (buildings are simplified
554 as cuboids with square basis and four-sided walls). For example, building
555 fraction in LCZ 1 is 50%, which could be approximated to the roof fraction.
556 Consequently, due to the full urbanization in this LCZ class, road surfaces
557 account for the rest of 50%. Meanwhile, the total wall surfaces are ten times
558 to the roof surface, given average building height is 37.5 meters and average
559 building width is 15 meters ($\frac{15 \times 37.5 \times 4}{15 \times 15} = 10$). As a result, the ratios among
560 road, roof, wall and soil are 1 : 1 : 10 : 0, based on which those weighted
561 thermal parameters are calculated.

Table C.4: Thermal properties (heat capacity C_i in $Jm^{-3}K^{-1} \times 10^6$ and thermal conductivity k_i in $Jm^{-1}s^{-1}K^{-1}$) and fraction of urban surface type i across LCZs, where i refers to roof, wall, road and soil.

ineB3	C_{roof}	C_{wall}	C_{road}	k_{roof}	k_{wall}	k_{road}	roof (%)	wall (%)	road (%)	soil (%)
ineB3 LCZ 1	1.8	1.8	1.75	1.25	1.09	0.77	8.33	83.33	8.33	0
LCZ 2	1.8	2	1.5	1.25	1.45	0.62	17.19	68.75	12.5	1.56
LCZ 3	1.44	2.05	1.63	1	1.25	0.69	21.24	61.39	13.51	3.86
LCZ 4	1.8	2	1.54	1.25	1.45	0.64	12.45	58.51	14.52	14.52
LCZ 5	1.8	2	1.5	1.25	1.45	0.62	16.30	45.65	21.74	16.30
LCZ 6	1.44	2.05	1.47	1	1.25	0.6	17.24	42.53	20.11	20.11
LCZ 7	2	0.72	1.38	2	0.5	0.51	32.75	56.33	4.37	6.55
LCZ 8	1.8	1.8	1.8	1.25	1.25	0.8	29.41	26.47	33.09	11.03
LCZ 9	1.44	2.56	1.37	1	1	0.55	10.79	28.06	10.79	50.36
LCZ 10	2	1.59	1.49	2	1.33	0.61	17.61	29.58	21.13	31.69
ineB3										

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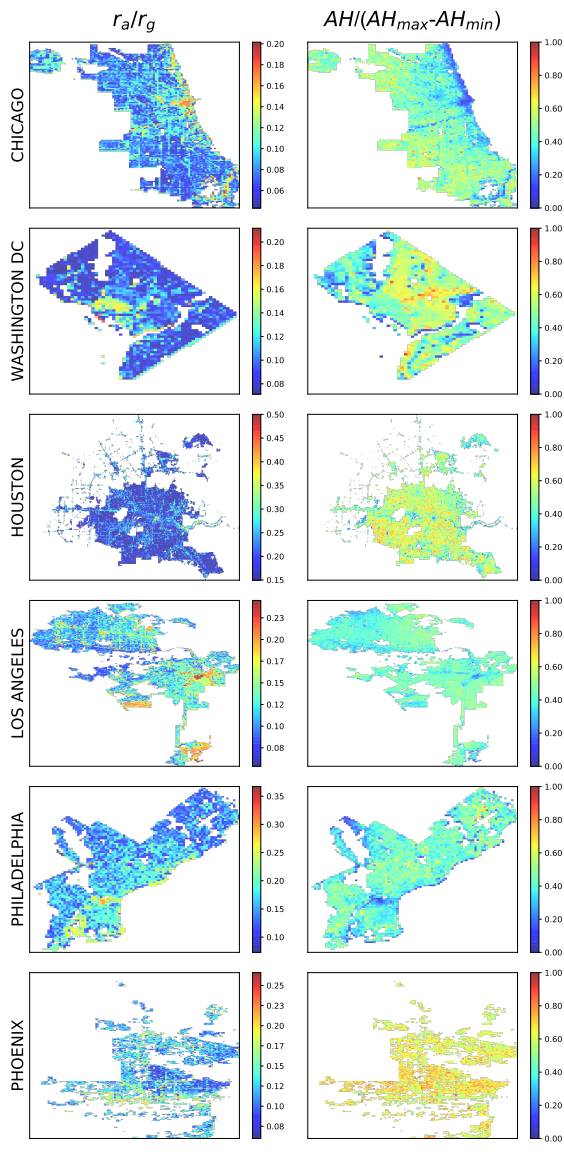


Figure C.5: Six cities: Energy partitioning efficiencies between sensible and storage heat in contrast with scaled AH